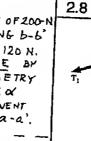


GIVEN: COMPONENT OF 200-N FORCE ALONG 6-6" MUST BE 120 N. DETERMINE BY TRIGONOMETRY (a) ANGLE & (b) COMPONENT

ALONG a-a'.



GIVEN: RESULTANT & OF I, AND I MUST BE YERTICAL AND Tz = 1000 1b. FIND (a) T, : (b) R



(a) USING TRIANGLE RULE AND LAW OF SINES! sin a _ sin 450 120 H . 200 H Sin \(= 0.41426

X = 25.1°

(b) B=180-45°+25.1°=109.9°

T,= IDDOID

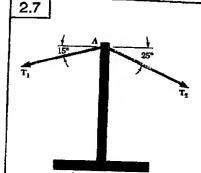
TRIANGLE RULE AND LAW OF SINES! $\frac{T_1}{\sin 65^\circ} = \frac{100016}{\sin 75^\circ} = \frac{R}{\sin 40^\circ}$

(a) SOLVING FOR TI:

T, = (1000 16) 310.65 = 938.28 16, 7 = 938 16

(b) SOLVING FOR R:

R=(1000 16) Sin 40° = 665.46 16, R= 665 16



GIVEN: RESULTANT R OF I AND I MUST BE VERTICAL AND T, = 800 16 FIND:

(a) T_2

(b) R

2.9

GIVEN: RESULTANT R OF THE TWO FORCES MUST BE HORIZONTAL AND P= 35 N. FIND: (a) ANGLE of

TRIANGLE RULE:

(a) LAW OF SINES! $\frac{\sin \alpha}{50 \, \text{N}} = \frac{\sin 25^{\circ}}{35 \, \text{N}}$ Since = 50 N Sin 25

(b) R

SIN Q = 0.60374 , &= 37.14°

(b) B = 180°-25°-37.14° = 117.86°

LAW OF SINES!

$$\frac{R}{\sin \beta} = \frac{35N}{\sin 25^{\circ}}$$

 $R = (35 \text{ N}) \frac{\sin 117.86^{\circ}}{50.25^{\circ}} = 73.218 \text{ N}$

R=73,2 N

TRIANGLE RULE AND LAW OF SINES :

$$\frac{T_1}{\sin 65^{\circ}} = \frac{T_2}{\sin 75^{\circ}} = \frac{R}{\sin 40^{\circ}}$$
8001b = T_2 R

 $\frac{8001b}{\sin 65} = \frac{T_2}{\sin 75} = \frac{R}{\sin 90}$

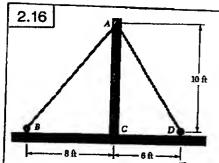
(a) SOLVING FOR Tz;

$$T_2 = (800 \text{ B}) \frac{\sin 75^\circ}{\sin 65^\circ} = 852.6 \text{ 16}$$

T = B53 b

(6) SOLVING FOR R:

R=567 16



GIVEN:

TAB = 120 Ib

TAD = 40 Ib

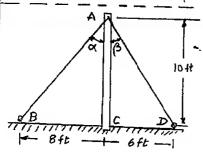
FIND:

RESULTANT R

OF THE PORCES

EXERTED AT A

BY AB AND AD



 $\alpha = 38.66^{\circ}$ $\tan \beta = \frac{6}{10}$ $\beta = 30.96^{\circ}$

 $\tan \alpha = \frac{9}{10}$

T_{AB}=1201/37

FROM FORCE TRIANGLE:

W OF COSINES: $R^{L} = (120)^{1} + (40)^{2} - 1 (120)(40) \cos 110.38^{4}$ = 14,100 + 1600 - 9600(-0.34824) $R^{2} = 19,343$ R = 139.09 [b]LAW OF SINES

R= 139,116 7 67.0°





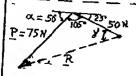
GIVEN;

P = 75 N , $\alpha = 50^{\circ}$ FIND:

RESULTANT R OF

THE TWO FORCES

SHOWN.

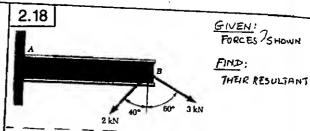


FROM FURCE TRIANGLE: LAW OF COSINES: R2=(75)2+(50)-2(15)50)(06105° = 5625+ 2500-7500(-025882) R2=10066 R=100.33 N

LAW OF SINES: $\frac{\sin \delta}{75N} = \frac{5 \text{ in 105}^6}{100,33N}$ $\sin \delta = 0.72206 \quad \delta = 46.22^6$

R = Y - 25" = 46.22"- 25" = 21.22"

R = 100,3 N. 721.2



2kN 74 146 B R 180 R 60° 3kN FROM FURCE TRIANGLE:

LAW OF COSINES:

R^2 = (2) + (3) - 2(2)(3) cos By

R' = 10,916

R = 3.304 KN

LAW OF SINES:

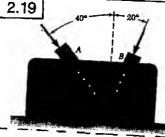
Sin BO

2-11

2-11

36.59

 $\beta = 180^{\circ} - (80^{\circ} + 36.59^{\circ}) = 63.41^{\circ}$ $\phi = 180^{\circ} - (\beta + 50^{\circ}) = 66.59^{\circ}$ $R = 3.30 \text{ kM} = 66.6^{\circ}$



GIVEN:

F_A = 15kH

F_B = 10kH

FIND:

RESULTANT OF

RESULTANT OF FORCES EXERTED ON BRACKET BY MEMPTRS A AND B.



FROM FORCE TRIANGLE:

LAW OF COSINES:

R² = (15)² + (10)² - 2 (15)(10) cos 126

R¹ = 475

R = 21.794 kN

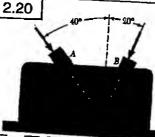
LAW OF SINES:

Sind = sin 120°

10kN 21.794kN

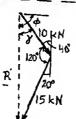
#= 50+ 8 = 50+23.41=73.41 R = 21.8 kN \$\frac{1}{2}73.40

K = 21.8 KN 5 73.4



 $\frac{GIVEN:}{F_A = 10 \text{ kn}}$ $F_B = 15 \text{ kn}$ FIND:

RESULTANT OF FORCES
EXERTED ON BRACKET
BY MEMBERS A AND B.



FROM FORCE TRIANGLE:

LAW OF COSINES:

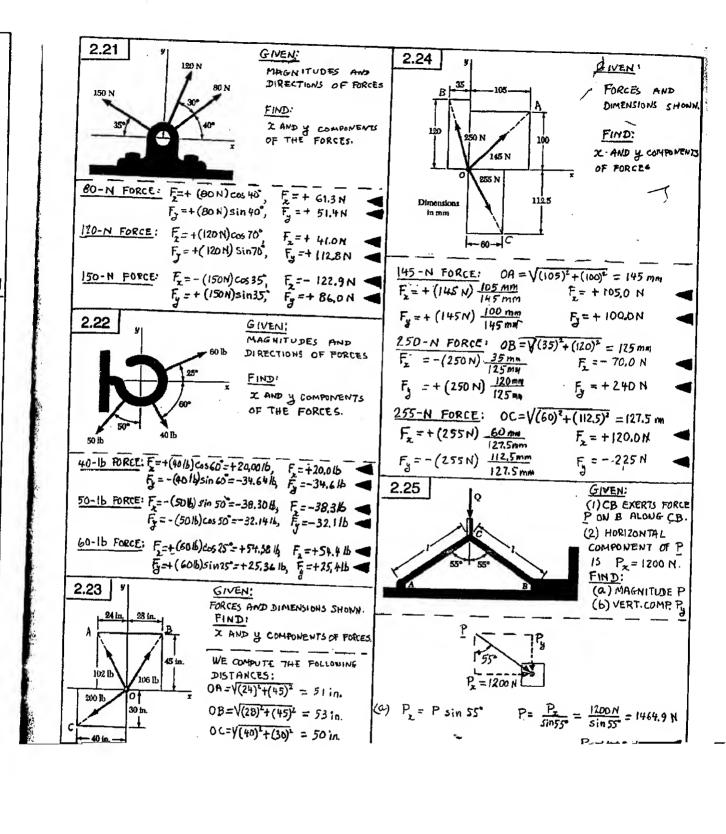
R=(10)+(15)2-2(10)(15) cos 120

R=21.794 kN

LAW OF SINES:

SIN = SIN | 20

 $\frac{\sin \delta}{15 \text{ kN}} = \frac{\sin 120}{21.794 \text{ kN}} \qquad \delta = 36.59^{\circ}$ $\frac{6}{4} = 50^{\circ} + 8 = 50^{\circ} + 36.59^{\circ} = 86.59^{\circ}$ $\frac{6}{4} = 21.8 \text{ kN} = 86.6^{\circ}$



ŒS

£7

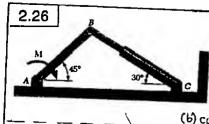
R

Ho

Ĵŧs

ET

₿.



GIVEN:

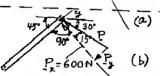
(1) FORCE P EXERTED

BY BC ON AB IS

DIRECTED ALONG BC.

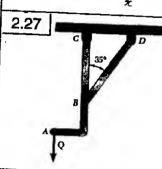
(2) COMPONENT OF P

L AB IS 600 N FIND: (a) P (b) comp. of P Along AB



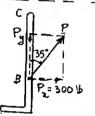
(a) $P = \frac{F_x}{\cos 15^{\circ}} = \frac{600 \text{ N}}{\cos 15^{\circ}}$ P = 621 N(b) $P_y = P_y + \tan 15^{\circ} = (600 \text{ N}) + \tan 15^{\circ}$





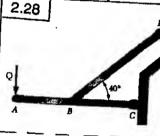
GIVEN:
(1) FORCE P EXERTED
BY 8D ON ABC 15
DIRECTED ALONG BD.
(2) HORIZ. COMPONENT
OF P 15 Px = 300 lb.

FIND: (a) MAGNITUDE P



(b) $P_x = \frac{P_z}{\tan 35^\circ} = \frac{300 \text{ ib}}{\tan 35^\circ}$

(a) $P = \frac{P_x}{\sin 35^\circ} = \frac{300 \text{ lb}}{\sin 35^\circ}$



GIVEN:

(1) FORCE P EXERTED

BY BD ON ABC IS

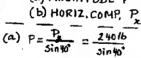
DIRECTED ALONG BD

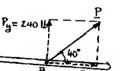
(2) VERT, COMPONENT

OF P IS P = 240 lb.

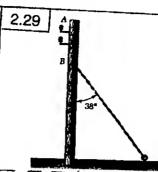
FIND:

(a) MAGNITUDE P





P = 373 lb(b) $P_2 = \frac{P_3}{\tan 40^9} = \frac{240 \text{ lb}}{\tan 40^9}$



GIVEN:

(1) FORCE PEXERIED BY 2D

ON POLE IS DIRECTED ALONG BD

(2) COMPONENT OF P 1 TO

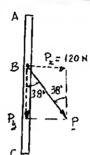
AC 15 120 N.

FIND:

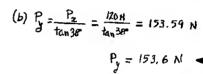
(a) MAGNITUDE P

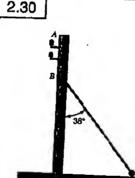
(b) COMPONENT OF P

ALONG AC.



(a) $P = \frac{P_2}{\sin 38^\circ} = \frac{120 \text{ H}}{\sin 38^\circ} = 194.91 \text{ N}$ P = 194.9 H





GIVEN:

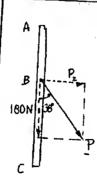
(1) FORCE PEXERTED BYBD ON POLE IS DIRECTED ALONG BD

(2) COMPONENT OF P ALDING AC IS 180 N.

FIND:

(A) NAGNITUDE P

(b) COMPONENT OF P 1 TO AC.

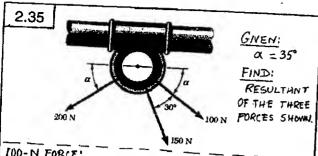


(a) $P = \frac{180N}{\cos 38^\circ} = 228.4 \text{ M}$

P= 228 N

(b) $P_2 = (180 \text{ N}) \tan 30^\circ = 140,63 \text{ N}$

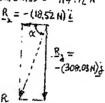
P= 140.6 N



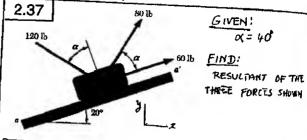


$$F_2 = -(20 \text{ N})\cos 35^\circ = -163.03 \text{ N}, \quad F_3 = -(200 \text{ N})\sin 35^\circ = -114.72 \text{ N}$$
 $F_3 = -(1852 \text{ W})^\circ$

FORCE	X COMP. (N)	A COMP.(N)
IDDN	+81.92	-57.36
150 N	+63,39	-135.95
200H	-163,83	~114.72
	R =-18.52	Ry=-308,03

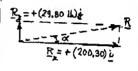


$$R = \frac{308.03 \text{ N}}{\sin 86.56} = 308.6 \text{ N}$$
 $R = 309 \text{ N} \text{ P86.6}$



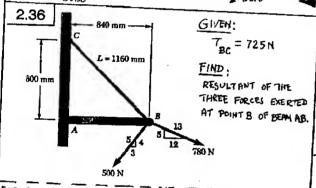
60-16 FORCE

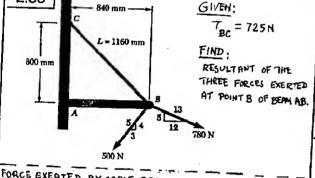
FORCE	X COMP (16)	A COME (1P)
60 lb	+56.38	+20.52
8016	+40,00	+69,28
1201	+103,92	-60.00
	Rz=+200,30	Ry=+29.80



$$tan Q = \frac{29.80 \, lb}{200.50 \, lb} \qquad \alpha = 8.462^{\circ}$$

$$R = \frac{24.80 \, \text{B}}{\sin 8.462} = 202.51 \, \text{lb} \qquad R = 203 \, \text{lb} \ll 8.46^{\circ}$$



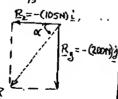


FORCE EXERTED BY CABLE BC:

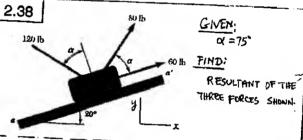
F=-(500N)= =-300N, Fy = - (500 N) 4 = -400 N 780-N FORCE:

 $F_2 = + (780N) \frac{12}{13} = + 720N$ Fy =- (780N) = = -300 N

	-	•
FORCE	X COMP. (N)	K COME (N)
TBC 725H	-525	+500
500 N	-300	+400
750 N	+720	-500
	Rx=-105	Ry = -200



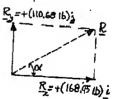
$$\tan \alpha = \frac{200N}{105N}$$
 $\alpha = 62.30$
 $R = \frac{200N}{\sin 61.30} = 225.9 N$



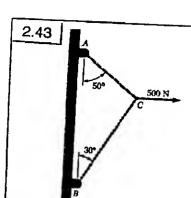
60-16 FORGE:

$$F_z = + (120 \text{ b}) \cos 5^\circ = + 119.5 \text{ b}, \quad F_y = + (120 \text{ b}) \sin 5^\circ = + 10.16 \text{ b}$$

FORCE	X COMP. (IL	y COMP. (ID)
6016	+56.38	
80 lb	-6.97	1.10
12016	+119.54	,- ,
	R=+168.95	Ry=+110.68



$$R = \frac{110.68 \text{ lb}}{5 \text{ in } 32.13^{\circ}} = 201.98 \text{ lb}$$



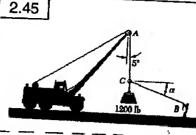
F.B. DIAGRAM

GIVEN: CABLES AC AND BC ARE LOADED AS SHOWN

FIND; (a) TENSION IN AC.

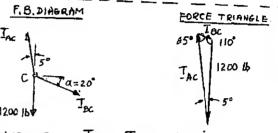
(b) TENSION IN BC.

FORCE TRIANGLE



GIVEN; a = 20° FIND: TENSION IN (a) AC (b) BC

TAC 1200 15



LAW OF SINES; TAC = TBC = 120016 (a) $T_{AC} = \frac{1200 \, b}{5in65} \sin 110^\circ = 1244,2 \, b$

TAC = 1244 16 4

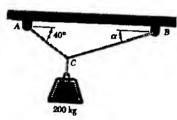
(b) $T_{BC} = \frac{1200 \, \text{B}}{2in65} \sin 5 = 115.40 \, \text{B}$

TBC = 115,4 16

LAN OF SINES: (a) $T_{AC} = \frac{500 \text{ N}}{\sin 90^{\circ}} \sin 60^{\circ} = 439.7 \text{ N}$ 7 = 440 N (b) $T_{BC} = \frac{500 \text{ N}}{\sin 80^{\circ}} \sin 40^{\circ} = 326.4 \text{ N}$ TBG = 326 N



TAC

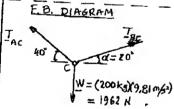


500 N

<u>GI</u>VEN (1) CABLES AC AND BC ARE LOADED AS SHOWN

FIND: TENSION IN (a) AC

(b) BC FORCE TRIANGLE



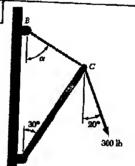


LAW OF SINES: $\frac{T_{AC}}{\sin 70^{\circ}} = \frac{T_{BC}}{\sin 50^{\circ}} = \frac{1962H}{\sin 60^{\circ}}$

(a) TAC= 1962 N Sin 70° = 2128,9 N TAC= 2,13 KN

(b) T = 1962N sin 50° = 1735,49N T = 1,735 kN ◀

2.46



GIVEN: $(1) \propto = 55^{\circ}$.

(2) BOOM AC EXERTS ON PIN C A FORCE ALONG AC.

FIND: (b) T_{BC}

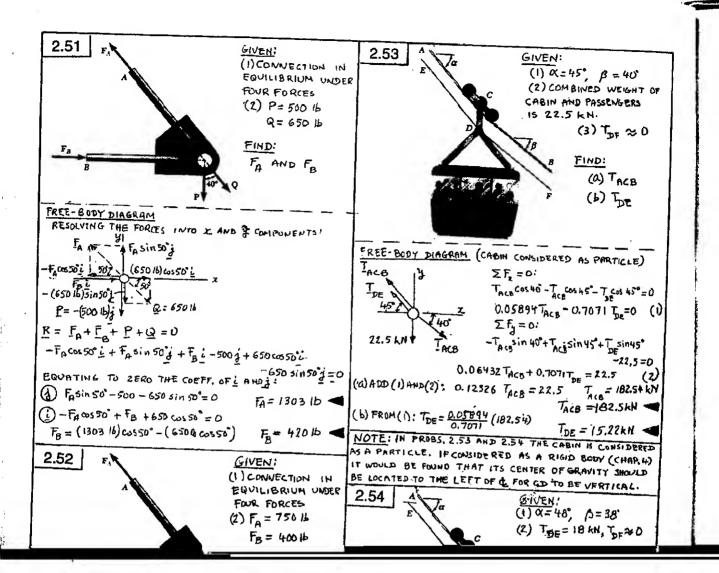
F.B. DIAGRAM

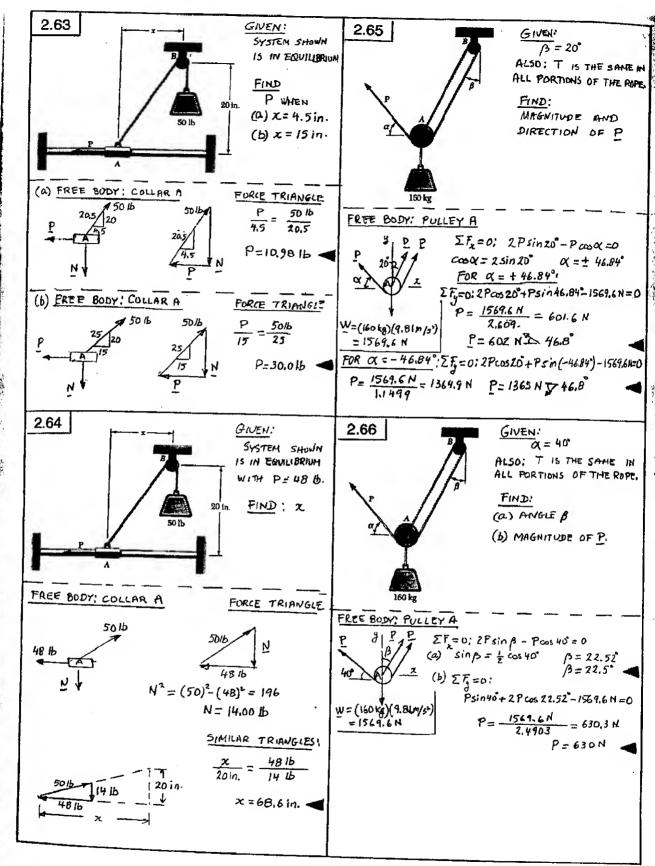
FORCE TRIANGLE

LAW OF SINES;

(a) FAC = 300 16 Sin 35° = 172,73 16 F= 172.716

(b) $T_{Bc} = \frac{3001b}{5inq\bar{5}^{\circ}} \sin 50 = 230.7 /b$ $T_{Bc} = 231 \text{ }b$





DING

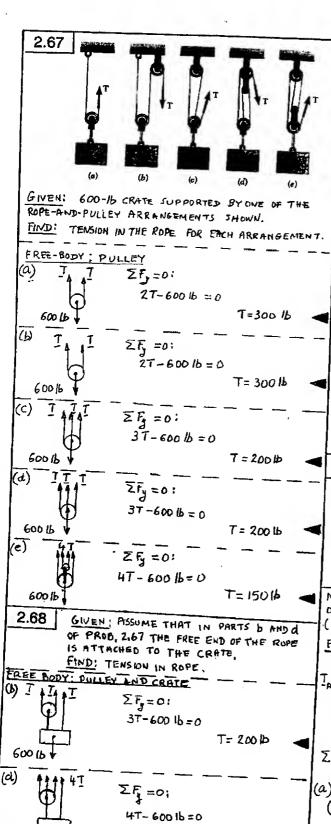
BG

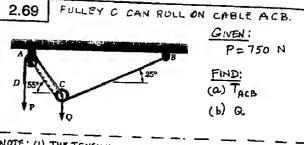
LE

962

H

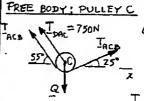
E





NOTE: (1) THE TENSION IS THE SAME IN BOTH FORTIONS OFCABLE ALB.

(2) THE TENSION IN CABLE DAG IS EQUAL TO P.



(G) ΣF, =0: TACB COS 25"- TACB COS 55" -(750 N) cos 55 = 0

TACA (cos 25° - cos 55") = 750 cos 55" TACB = 1293 N

ACB = (750 N) 0.5736 0.3327 (6) $\Sigma F_y = 0$: $(T_{ACB} + T_{DAC}) \sin 55^{\circ} + T_{ACB} \sin 25^{\circ} - Q = 0$

Q = (1293 N+ 750 N) sin 55°+(1293 N) sin 25° = 2120.0 H Q = 2220 N

2.70

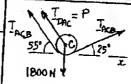
PULLEY & CAN ROLL ON CABLE ACB. GIVEN:

Q= 1800 N

EIND: (a) TACB. (b) P

NOTE: (1) THE TENSION IS THE SAME IN BOTH PORTIONS OF CABLE ACB. (2) THE TENSION IN CABLE DAC IS EQUAL TO P.

FREE BODY; PULLEY C



Σ F,=0: TACBOS 25"-TACBOSSS"-PCOS55"=0 P= TACB COS 250- COS 550
P= 0.5801 TACB (1)

IF =0: (TACB+P) sin 55° + TACB sin 25° -/800 N=0

(a) SUBSTITUTE FOR P FROM (1) INTO (2); (1.5001 sin 55° + sin 25°) TACB = 1800 N

TACA = 1048,4 N

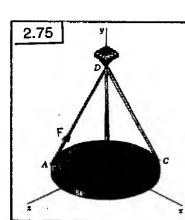
TACB = 1048 N

(b) CARRY INTO (1): P=0,5801 (1048.4N)

P = 608 N

T= 150 lb

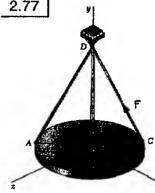
600 lb



GIVEN: (1) WIRES FORM 30 ANGLES WITH VERTICAL (2) FORCE EXERTED BY AD ON PLATE HAS COMPONENT F= 110,3N

FIND:

(a) TENSION IN AD (b) ANGLES Ox, 0, 02 THAT FORCE EXERTED AT A FORMS WITH THE COORDINATE AXES.



GIVEN: (1) WIRES FORM 30 ANGLES WITH VERTICAL (2) TENSION IN CD 15 60 lb.

FIND: (a) components of FORCE EXERTED ATC. (b) ANGLES 0, 0, 02 THAT FORCE FORMS WITH THE COORDINATE

(a)
$$F_x = F \sin 30^{\circ} \sin 50^{\circ} = 110.3 \text{ N}$$
 (GIVEN)

$$F = \frac{110.3 \text{ N}}{\sin 30^{\circ} \sin 50^{\circ}} = 287.97 \text{ N}$$

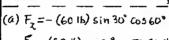
$$F = 288 \text{ N}$$

(b)
$$\cos \theta_{\lambda} = \frac{F_{x}}{F} = \frac{110.3 \text{ N}}{207.47 \text{ N}} = 0.3830 \quad \theta_{\lambda} = 67.5$$

$$F_3 = F\cos 30^\circ$$
, $\cos \theta_3 = \frac{F_3}{F} = \cos 30^\circ$. Thus: $\theta_3 = 30.0^\circ$ (b) $\cos \theta_2 = \frac{F_2}{F} = \frac{-15.00 \, lb}{60 \, lb} = -0.2500$, $\theta_2 = 104.5^\circ$

$$F_2 = -F \sin 30^{\circ} \cos 50^{\circ}$$
= - (287.97 N) \(\text{sin 30}^{\circ} \cos 50^{\circ} = -92.552 N\)
$$\cos \theta_2 = \frac{F_E}{F} = \frac{-92.552 N}{287.97N} = -0.3214$$

$$\theta_2 = 108.7^{\circ}$$



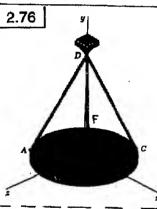
$$F_z = -(60 \text{ lb}) \sin 30^\circ \cos 60^\circ$$
 $F_z = -15.00 \text{ lb} \blacktriangleleft$
 $F_y = (60 \text{ lb}) \cos 30^\circ = 51.96 \text{ lb}$ $F_y = +52.0 \text{ lb} \blacktriangleleft$

(b)
$$\cos \theta_x = \frac{F_x}{F} = \frac{-15.001b}{601b} = -0.2500, \quad \theta_x = 104.5^\circ$$

$$\cos \theta_y = \frac{F_y}{F} = \frac{+51.96 \text{ lb}}{60 \text{ lb}} = 0.8660, \quad \theta_y = 30.0^{\circ}$$

$$\cos \theta_2 = \frac{F_2}{F} = \frac{+25.981b}{601b} = 0.9330$$
 $\theta_2 = 64.3^{\circ}$

NOTE: VALUE OBTAINED FOR By CHECKS WITH GIVEN DATA.

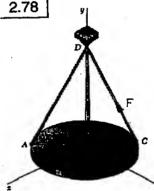


GIVEN:

(I) WIRES FURM 30° ANGLES WITH VERTICAL (2) FORCE EXERTED BY BD ON PLATE HAS COMPONENT F = -32,14N.

FIND:

(a) TENSION IN BD (b) ANGLES Ox, 07, 02 THAT FORCE EXERTED AT B FORMS WITH THE COURDINATE AXES.



GIVEN:

(1) WIRES FURH 30 ANGLES WITH VERTICAL . (2) FORCE EXERTED BY CD UN PLATE HAS COMPONENT F =- 20,0 16

FIND:

(a) TENSION IN CD. (b) ANGLES BZIBY, BA THAT FORCE EXERTED AT C PORMS WITH THE COORDINATE AXES.

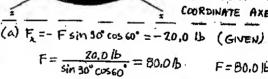
(a)
$$F_2 = -F \sin 30^{\circ}\cos 40^{\circ} = -32.14 \text{ N}$$
 (GIVEN)
 $F = \frac{32.14 \text{ N}}{\sin 30^{\circ}\sin 40^{\circ}} = 100.0 \text{ N}$ F=100.0 N

(b)
$$F_2 = -F \sin 30^\circ \cos 40^\circ$$

= - (100.0 N) $\sin 30^\circ \cos 40^\circ = -38.30 \text{ N}$

$$\cos \theta_z = \frac{F_z}{F} = \frac{-38.30 \text{ N}}{100.0 \text{ N}} = -0.3830$$
 $\theta_z = 112.5^{\circ}$ $\theta_z = F\cos 30^{\circ}$, $\cos \theta_z = \frac{F_z}{F} = \cos 30^{\circ}$. Thus: $\theta_z = 30.0^{\circ}$

$$F_y = F\cos 30$$
, $\cos \theta_y = \frac{F_y}{F} = \cos 30$, Thus: $\theta_y = 30.0^{\circ}$
 $\cos \theta_z = \frac{F_z}{F} = \frac{-32.14 \text{ N}}{100.0 \text{ N}} = -0.3214$ $\theta_z = 108.7^{\circ}$



(b)
$$\cos \theta_z = \frac{F_z}{F} = \frac{-20.01b}{\theta 0.01b} = -0.2500$$
 $\theta_z = 104.5^\circ$

$$F_y = F\cos 30$$
, $\cos \theta_y = \frac{F_x}{F} = \cos 30$. Thus: $\theta_y = 30.0^\circ$

$$\cos \theta_2 = \frac{F_2}{F} = \frac{34.641 \text{ lb}}{80.0 \text{ lb}} = 0.4330$$
 $\theta_2 = 64.3$

2.79 GNEN: F=(260N):-(320N);+(800N)k	2.83 GIVEN: F= 230N, 02= 32.5°, F3=-60N, F2>0
FIND: MAGNITUDE AND DIRECTION OF F	FIND: (a) Fx AND Fz, (b) By AND Ba
F=VF2+F2+F2=V(260)2+(320)2+(800)6, F=900N	(a) F _z = Fcos B _z = (230 N) cos 32,5° F _z = 194,0 N ◀
$F_{2} = 260 \text{N} = 0.2899$ $A = 73.26$	$F^{2} = F_{2}^{2} + F_{3}^{2} + F_{2}^{2}$: $(230 \text{ N})^{2} = (194.0 \text{ N})^{2} + (-60 \text{ N})^{2} + F_{2}^{2}$
~ F 900 m	$F_2 = +\sqrt{(230)^2 - (149)^2 - (60)^2}$ $F_2 = +108.0 \text{ N}$ (b) $\cos \theta_3 = F_3/F = -60/230 = -0.2609$ $\theta_3 = 105.1$
F 900N	100/250 - 4/1 4590 Ht
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	

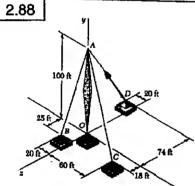
25 ft g O 20 ft 74 ft 18 ft

GIVEN: TENSION IN WIRE AB 15 525 lb.

FIND:

COMPONENTS OF
FORCE EXERTED
ON BOLT B BY
WIRE AB.

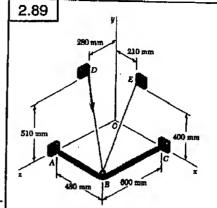
 $\overrightarrow{BA} = (20ft) \underline{i} + (100ft) \underline{j} - (25ft) \underline{k}$ $BA = \sqrt{(20)^{4} + (100)^{4} + (25)^{4}}$ BA = 105 H $F = F \underline{A}_{BA} = F \frac{BA}{BA} = \frac{525 \text{ lb}}{105 \text{ ft}} [(20ft) \underline{i} + (100ft) \underline{j} - (25ft) \underline{k}]$ $\underline{f} = (100 \text{ lb}) \underline{i} + (500 \text{ lb}) \underline{j} - (125 \text{ lb}) \underline{k}$ $F_{a} = +100 \text{ lb}, F_{a} = +500 \text{ lb}, F_{a} = -125 \text{ lb}$



GIVEN: TENSION IN WIRE AD IS 315 16.

FIND:
COMPONENTS OF
FORCE EXERTED
ON BOLT D BY
WIRE AD.

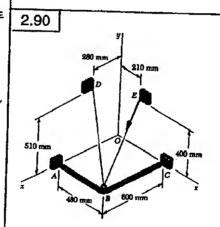
 $\overrightarrow{DA} = (20 \text{ ft}) \cdot \underbrace{i} + (100 \text{ ft}) \cdot \underbrace{j} + (74 \text{ ft}) \cdot \underbrace{k}$ $DA = \sqrt{(20)^2 + (100)^4 + (74)^2} = 126 \text{ ft}$ $\overrightarrow{F} = F \lambda_{DA} = F \cdot \overrightarrow{DA} = \frac{31576}{126 \text{ ft}} \left[(20 \text{ ft}) \cdot \underbrace{i} + (100 \text{ ft}) \cdot \underbrace{j} + (74 \text{ ft}) \cdot \underbrace{k} \right]$ $\overrightarrow{F} = (50 \text{ lb}) \cdot \underbrace{i} + (250 \text{ lb}) \cdot \underbrace{j} + (185 \text{ lb}) \cdot \underbrace{k}$ $F_z = +50 \text{ lb}, \quad F_z = +185 \text{ lb}$



GIVEN; TENSION IN CABLE DBE 15 385 N.

FIND:
COMPONENTS OF
FORCE EXERTED
BY CABLE ON D.

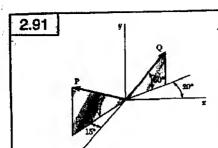
 $\widehat{DB} = (480 \text{ mm}) \widehat{L} - (510 \text{ mm}) \widehat{g} + (320 \text{ mm}) \underline{k}$ $DB = \sqrt{(480)^2 + (510)^2 + (320)^2} = 770 \text{ mm}$ $F = F \widehat{A} = F \underbrace{\widehat{DB}}_{DB} = \frac{385 \text{ N}}{770 \text{ mm}} \left[(480 \text{ mm}) \widehat{L} - (510 \text{ mm}) \widehat{g} + (320 \text{ nm}) \widehat{k} \right]$ $F = (240 \text{ N}) \widehat{L} - (255 \text{ N}) \widehat{g} + (160 \text{ N}) \widehat{k}$ $F_z = + 240 \text{ N}, \quad F_g = -255 \text{ N}, \quad F_z = +160 \text{ N}$



GIVEN:
TENSION IN
CABLE DEE
15 385 N.

FINDI COMPONENTS OF FORCE EXERTED BY CABLE ON E

EB = (270 mm) i - (400 mm) j + (600 mm) k $EB = \sqrt{(270)^2 + (400)^2 + (600)^2} = 770 \text{ mm}$ $F = F \frac{2}{EB} = F \frac{EB}{EB} = \frac{385 \text{ N}}{770 \text{ mm}} [(270 \text{ mm}) i - (400 \text{ mm}) j + (600 \text{ mm}) k].$ F = (135 N) i - (200 N) j + (300 N) k $F_z = + 135 \text{ N}, \quad F_y = -200 \text{ N}, \quad F_z = +300 \text{ N}$



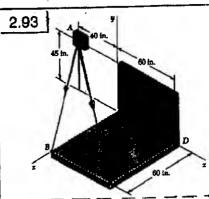
GIVEN: P=300 N. Q = 400 N

FIND MAGNITUDE AND DIRECTION OF RESULTANT OF P AND Q.

FORCE P: P=- (300N) cos 30's in 15" = - 67.24 N P=+(300N)sin 30" = + 150.00 N P2= + (300 N) Cos 30 Cos 15 = + 250.95 N P=- (67.24 N) + (150.00 N) + (250,95 N) +

FORCE Q: Q =+ (400N) cos50" cos 20" = + 241.61 N G= + (400 H) sin 50 = + 306.42 M 92 = - (400 H) cos 50 sin 20 = - 87.94 H Q = +(241,61'N) +(306.42N) j-(87.94N) k

RESULTANT: R = P+@ = (174.37 N) + (456.42 N) + + (163.01 N) + R=V(174.37)+(456.42)+(163.01) =515.07N, R=515N COSB = R2/R=(174.37 N)/(515.07N)=0.3385, 0=70.20 COSOy= Ry/R=(456.42N)/(515.07N)=0.8861, 0= 27.6° € $cos O_2 = R_2/R = (163.01N)/(515.07N) = 0.3165, \theta_2 = 71.5°$



GIVEN: TAB= 425 16 TAC = 510 16

FIND: MAGNITUDE AND DIRECTION OF RESULTANT OF FORCES AT A.

AB = (40in.) - (45 in) + (60in.) k AB=V(40)+(45)+(60)=BSin. AC = \((100) + (+5) + (60) = 125in. AZ = (100 in)i - (45 in) + (60 in.)k $F_{AB} = F_{AB} \frac{2}{2} \frac{2}{2} F_{AB} = \frac{425 / b}{85 in} [(40 in.) - (45 in) + (60 in.)]$

FAB= (200 16) = - (225 16) = + (300 16) E

FAC = FAC PAC = FAC AC = 51010 [(100in,) i-(45in,) + (60in) k] FAC= (408 16) i = (1836 13) j + (244.8 16) £

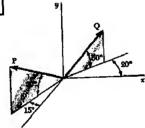
R=FAS+FAC= (608 b)i-(408.6 b)j+(544.8 b)k, R= 912.92 b R=91316

Cos 0 = Rx/R = 608/912.92 = 0.6660 cos y = Ry /R = -408. 6/912.12 = -0.4476 cos 02 = R2/R = 544.8/912.92= 0.5968

£ = 48,2°

Ba= 116.6 0 = 53.4°

2.92



GIVEN:

Q = 300 N

FIND: MAGNITUDE DIRECTION OF RESULTANT OF PAND Q.

FORCE P: P =- (400 N) cos 30 sin 15 =- 89.66 N Pu=+ (400 N) sin 30°=+ 200,00 N Pz=+ (400 N) cos 30 cos 15 = + 334.61 N P=-(81.66 N) + (200.00 N) j+(334,61N)k

MORCE Q: 0 =+ (300 N)cos 50 cos 20 =+ 181.21 N U =+ (300 N) 5in 50" = + 229,81 N Q= - (300 N) cos 50 sin 20 = -65.45 N Q=(181.21 N) i + (229.81N) j-(65.95 N) k

R=P+Q=(91.55N)i+(429.BIN)i+(268.66N)k

R=V(41.55)+(424.81)+(268.66)=515.07 N, R=515N

COS 0= Rx/R=(91.55 N)/(515.07 N) = 0,1777

cos 0, = R, /R= (429.01 N)/(5/5.07 N)= 0.8345

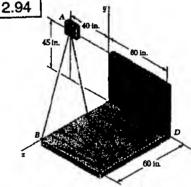
cos 0 = R /R = (268.66N)/(515.07 H)= 0,5216

P = 400 H

0,=79,8

04=33.4°

0,=58.6°



GIVEN: TAR = 510 16 TAC = 425 16

FIND:

MAGNITUDE AND DIRECTION OF RESULTANT OF FORCES AT A.

AB=(40in.) i-(45in.) ++(60in) k AB-V(40)2+(45)2+(60)2=85in. AC = (100 in) i - (45 in) j + (60 in.) k AC = V(100) + (45) + (60) = 125 in.

FAB - FB - AB - FB - AB = 510 b [(40in.) i - (45in.) i + (60in.) k]

FAR= (24016) i - (270 16) j+ (360 16) k

FAC = FAC 2 = FAC AC = 425/b ((100 in) - (45 in) + (60 in)) Far= (340 16)1-(153 16)3+(20416) k

R = FAB + FAC = (580 16) i - (423 16) j + (564 16) k, R=912.92 16 R= 913 |b

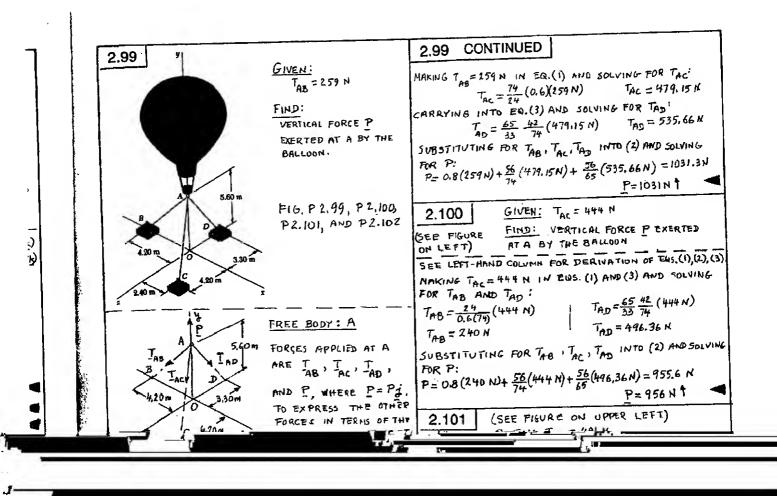
 $\cos \theta_x = R_x/R = 500/912.92 = 0.6353$

cos By = Ry/R= - 423/912,92=-0,4633

cos 0 = R /R = 564/912.92 = 0.6178

0,=117.60 กั้ว=51.8

B= 50.6°



CONTINUED 2.111

7

)

RCE

: 0

ī,ķ

<u>, ج</u>

4 K

RO:

(1)

(2)

(3)

₽D

;7 A. WE REPEAT THE LAST EUS:

(1) -160 lb+ 50 TAC - 10 TAD = 0

- 100 TAC - 100 TAD + P = 0 (2)

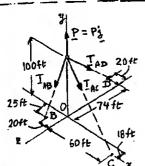
200 15 + \frac{18}{118} TAC - \frac{74}{126} TAD = 0

MULTIPLY ER.(1) BY -3, EQ.(3) BY 10,4ND ADD: (3)

TAD= 459.519 16 2480 16 - 480 TAD = 0 SUBSTITUTE INTO (1) AND SOLVE FOR TAC.

Tec = (18 (160 + 30 × 459.529) T = 458,118 16 SUBSTITUTE FOR THE TENSIONS IN (2) AND JOINE FOR P: P= 800 16+ 100 (458.118 16) + 100 (459.529 16) = 1552,94 16

WEIGHT OF PLATE = P= 1553 16 2.112 TAC = 590 16 VERTICAL FORCE P EXERTED BY TOWER ON PIN A.



FREE BODY! A IAB+I+ IAD + Pj = 0 AB = -201-100j+25#

AB = 105 ft AC = 601-1001 +18k

AC = IIB ft AD = -201-100j-74 k AD = 126 ft

TAB = TAB AB AB AB AB = (-4 1 - 20 1 + 5 K) TAB TAC = TAC 2AC = TAC AC = (60 i - 100 i + 18 k) TAC $T_{AB} = T_{AB} \, \gamma_{AB} = T_{AB} \, \frac{\overline{AB}}{AD} = \left(-\frac{20}{126} \, \dot{z} - \frac{100}{126} \, \dot{\underline{a}} - \frac{74}{126} \, \underline{k} \right) T_{AB}$

SUBSTITUTING INTO THE ER. ZF=0 AND FACTORING : j, k; (-4 TAS+ 60 TAC- 20 TAS) 6

+ (- 20 TAS - 100 TAC - 126 TAD + P) j $+\left(\frac{5}{21}T_{R8}+\frac{18}{118}T_{RC}-\frac{74}{126}T_{R9}\right)k=0$ SETTING THE COEFT. OF L, 1, K EQUAL TO ZERO:

(1)

(2)

 $\begin{array}{lll}
\bullet & \frac{20}{21} T_{AB} - \frac{100}{118} T_{AC} - \frac{100}{126} T_{AD} + P = 0 \\
\bullet & \frac{5}{21} T_{AB} + \frac{19}{118} T_{AC} - \frac{74}{126} T_{AD} = 0
\end{array}$ (3)

CONTINUED

2.112

CONTINUED MAKING TAL = 590 IB IN EQS. (1),

(1) $-\frac{4}{21}T_{AB} - \frac{20}{126}T_{AB} + 300 16 = 0$

[2') 20 TAR - 100 TAR - 500 16 + 9 =0

(3') 5 TAB - 74 TAB + 90 16 = 0

MULTPLY ER.(1') BY 5, EQ.(3') BY 4, AND ADD!

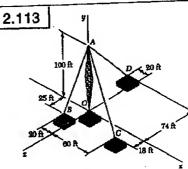
TAD = 591.818 L ~ 396 TAD + 1860 lb = 0 JUBST HTUTE INTO (1) AND SOLVE FOR THE TABE 1081.82 16

TABE 21 (300 16 - 10 x 591.818 16

TABE 7 (300 16 - 10 x 591.818 16

TABE 7 (300 16 - 10 x 591.818 16)

SUBSTITUTE FOR THE TENSIONS IN (2') AND SOLVE FOR PI P = 500 B + 20 (108182 16) + 100 (591.818 16) = 2000.00 16 WEIGHT OF PLATE = P = 2000 16



TOWER EXERTS ON A AN JOWARD VERTICAL FURCE P OF 1800 lb.

TENSION IN EACH WIRE.

SEE COLUMN ON THE LEFT FOR DERIVATION OF ESS. (1), (2), AND(3), MAKING P= 1900 Ib IN ER. (2), WE HAVE

- 4 TAB+ 60 TAC - 20 TAD = 0 (1)

-20 TAB - 100 TAC - 100 TAB + 1800 16 = D (2)

(3) $\frac{5}{21} T_{AB} + \frac{18}{110} T_{AC} - \frac{74}{116} T_{D} = 0$ MULTIPLY (1) BY -74, (3) BY 20, AND ADD:

TAC = 0,545378 TAB (4)

SUBSTITUTE INTO (1):

 $\left[-\frac{4}{71} + \frac{60}{118}(0.545378)\right]T_{AB} - \frac{80}{126}T_{AB} = 0$

0.0868347 TAB- 10 TAD = 0.547 059 TAB (5)

SUBSTITUTE FOR TAC AND TO INTO (2) AND SOLVE FOR TAB!

- 20 T AB - 100 (0.545378 TAB) - 100 (0.547059 TAB) + 1800 16 = 0

1.84814 TAB = 1800 16 TAB = 973.636 16 TAB = 974 16

SUBSTITUTING PROM (6) INTO (4):

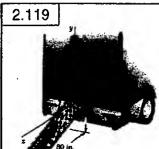
TAC = 9545378 (973.636 14) = 531,000 16

The = 531 16

SUBSTITUTING FROM (6) INTO (5);

TAD = 0,547051 (973.636 16) = 532.637 16

TAD = 533 16



GIVEN

- (1) 200-16 COUNTERWEIGHT IS IN EQUILIBRIUM UNDER FORCES EXERTED BY ROPES AND FORCE PERPENDICULAR TO CHUTE.
- (2) COORDINATES OF A,B,CARE A (0, -20 in., 40 in.) B (-40 in., 50 in., 0) c (45 in., 40 in., 0) FIND! TENSION IN EACH ROPE.

FREE BODY : COUNTERWEIGHT TAB+ TAC+W+N = 0

W=-(200 16) j N=(等+作K)N

WE NOTE THAT AB = - (40 id.) + (70in.) } - (40 in.) k AC = (45 in.) + (60 in.) 1 - (40 in.) k

TAC = TAC AT = (4 i + 12 d - 8 k) TAC

SUBSTITUTE FOR T AB, TAC, N , AND W INTO E F= 0 AND FACTOR 1, 3, 4:

(-等TAB+异TAC):+(呈TAB+异TAC+管N-20016); +(-4TAB-17TAC+16N)k=0

EQUATING TO ZERO THE COEFFICIENTS OF LILE:

(2)
$$\frac{7}{9}T_{AB} + \frac{12}{17}T_{AC} + \frac{2}{15}N - 200B = 0$$

MULTIPLY (3) BY -2 AND ADD (2):

$$\frac{15}{3} T_{AB} + \frac{28}{17} T_{AC} - 200 \ lb = 0 \tag{4}$$

MULTIPLY (1) BY 15, (4) BY 4, AND ADD:

$$\frac{247}{17}T_{AC} - 800 \, lb = 0 \qquad \qquad T_{AC} = 55.061 \, lb \qquad (5)$$

SUBSTITUTE PROM (5) INTO (1) AND SOLVE FOR TAB :

TAB = 4. 9 (55.061 16) = 65.587 B

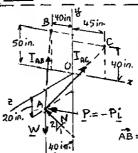
THE TENSIONS IN THE ROPES ARE



GIVEN:

(1) 200-16 COUNTER WEIGHT IS IN EBUILIBRIUM UNDER FORCES EXERTED BY THE TWO WURKERS SHOWN, BY A THIRD WORKER WHO PUSHES WITH P = - (40 b) : AND A FORCE PERPENDICULAR TO THE CHUTE. (2) COORDINATES OF A, B, CARE A (0,-20 in., 40 in.) B (-40 in., 50 in., 0)

C (45 in., 40 in., 0) FIND: TENSION IN ROPES AB AND AC.



FREE BODY; COUNTERWEIGHT $\Sigma T = 0$: TAB+ TAC+ W+P+N = D W= - (200 lb) j P=- (40 lb) i N=(學年+學片)N

WE NOTE THAT AB = - (40 in) i + (70 in.) j - (40 in)k AC = (45 in) i + (60 in) j - (40 in) k

THUS: TAG= TAB = (-4 ++7 - 4) TAB TAC= TA AC = (9 + 12 j - 8 k) TAC

SUBSTITUTE FOR TAB, TAC, N, P, AND W INTO EF=O AND

(-4 TAB+ + T TAC-40 16) ++ (7 TAB+ 17 TAC+ 2 N-20016) +(-+Tas-BTac+ LN) k=0

EQUATING TO ZERO THE COEFFICIENTS OF L. I. E.

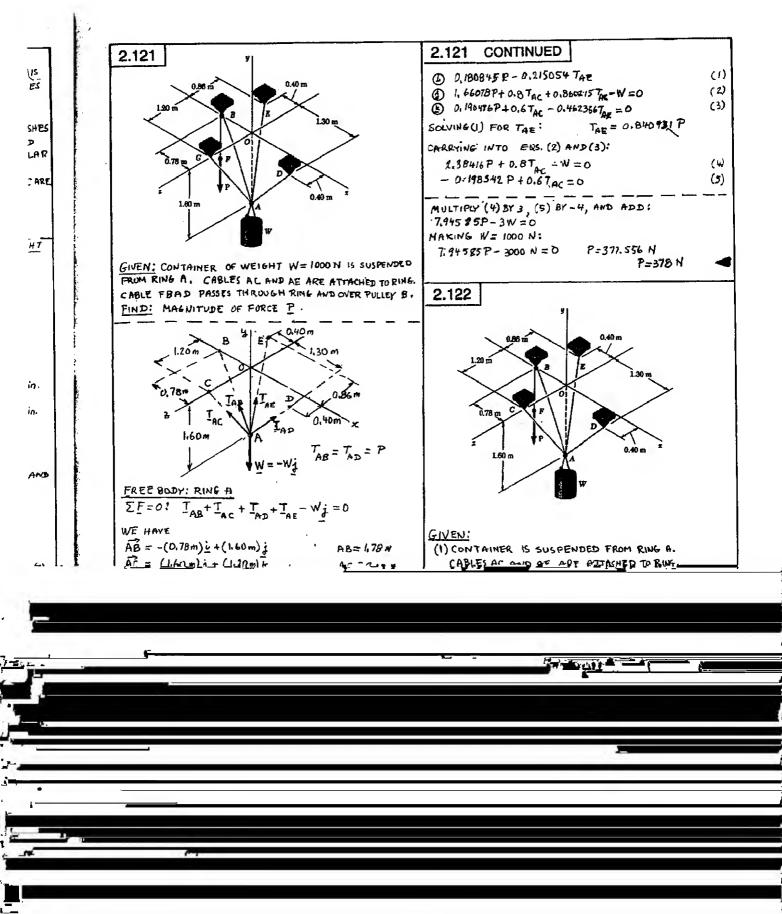
MULTIPLY (3) BY -2 AND ADD (2):

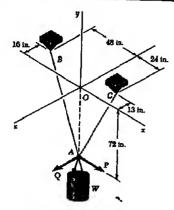
$$\frac{15}{7}T_{AB} + \frac{28}{17}T_{AC} - 200 \text{ lb} = 0 \tag{42}$$

MULTIPLY (1) BY 15, (4) BY 4, AND ADD:

SUBSTITUTE FROM (5) INTO (1) AND SOLVE FOR THE ! $T_{AB} = \frac{9}{4} \left[\frac{9}{17} (96.3563 \text{ lb}) - 40 \text{ lb} \right] = 24,777 \text{ lb}$

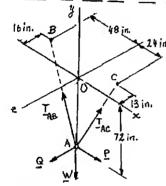
THE TENSIONS IN THE ROPES ARE





GIVEN: CONTAINER OF WEIGHT W=270 16 15 SUSPENDED FROM RING A. CABLE BAC PASSES THROUGH RING A.

FIND: P AND Q FOR EQUILIBRIUM POSITION SHOWN



FREE BODY: RING A Z = 0: WHERE PE PL

TAC =TAC (SAME TENSION T

IN BOTH PORTIONS OF CABLE) WE HAVE

 $\frac{AB}{AB} = -(48 \text{ in.}) \cdot + (72 \text{ in.}) \cdot \frac{1}{4} - (16 \text{ in.}) \cdot \frac{1}{4} + (72 \text{ in.}) \cdot \frac{1}{4} - (13 \text{ in.}) \cdot \frac{1}{4}$

AB - 88 in

$$T_{AC} = T_{AC} = T \frac{AB}{AB} = \left(-\frac{6}{11} \frac{i}{i} + \frac{9}{11} \frac{j}{i} - \frac{2}{11} \frac{k}{k} \right) T$$

$$T_{AC} = T_{AC} = T \frac{AE}{AC} = \left(\frac{24}{17} \frac{i}{i} + \frac{72}{77} \frac{j}{j} - \frac{13}{77} \frac{k}{k} \right) T$$

SUBSTITUTING FOR TAB, TAC , P. B. AND W INTO EFEO

SUBSTITUTING FOR
$$T_{AB}$$
, T_{AC} , P_{C} , Θ , AND W INT AND FACTORING L_{C} , L_{C}

SETTING THE COEFFICIENTS OF L, J, K EWORL TO ZERO AND REDUCING!

$$\begin{array}{ccc}
\textcircled{1} & -\frac{18}{77} \overrightarrow{1} + P = 0 \\
\textcircled{2} & 125 & \text{ord}
\end{array}$$

$$\frac{135}{77} T - W = 0$$
 (2)

MAKING W= 270 IL IN Ed. (2) AND SOLVING FOR T:

T= 77 (270 b) = 154.0 lb

SUBSTITUTING FORT IN EQS.(1) AND(3), WE OBTAIN P=36,016, Q=54.0 16

2.124

(SEE FIGURE ON THE LEFT) GIVEN: (1) Q = 36 16. (2) CABLE BAC PASSES THROUGH RING A.

FIND: WAND P.

SEE SOLUTION AT LEFT FOR DERIVATION OF ERS. (1), (2), (3). MAKING Q = 36 16 IN EQ. (3): T=102,667 16

- 27 T + 36 15 =0 T= 27 (36 16)

SUBSTITUTING FOR T IN EOS. (1) AND (2): - 18/77 (102,66716) + P=0

135 (102.667 16) -W = 0

P= 24.0 16

W=180.016

2.125

GIVEN: (1) COLLARS A AND B CONNECTED BY WIRE OF LENGTH 525 mm (2) P= (341 N) i (3) 4 = 155 mm

FIND:

(a) TAB

(b) Q FOR EQUILIBRIUM

 $(AB)^2 = \chi^2 + \xi^2 + \xi^2$; $(525 \, mm)^2 = (200 \, mm)^2 + (155 \, mm)^2 + 2^2$ $\frac{7}{AB} = \frac{100 \text{ mm}}{100 \text{ mm}} = \frac{155 \text{ mm}}{100 \text{ mm}} = \frac{155}{100 \text{ mm}} = \frac{$ AB = 525mm



(a) FREE BODY; COLLAR AT \(\Sigma F = 0\); Ni +Pj+Nzk+T 2 AB =0

SUBSTITUTING FOR 2 AND SETTING THE COEFF. OF & EQUAL TO ZERO:

P+ (-155 TAB)=0

MAKING P=341 N AND SOLULUS FOR TAB: TAB = 1155 N

 $T_{AB} = \frac{525}{155}(341 \text{ N})$

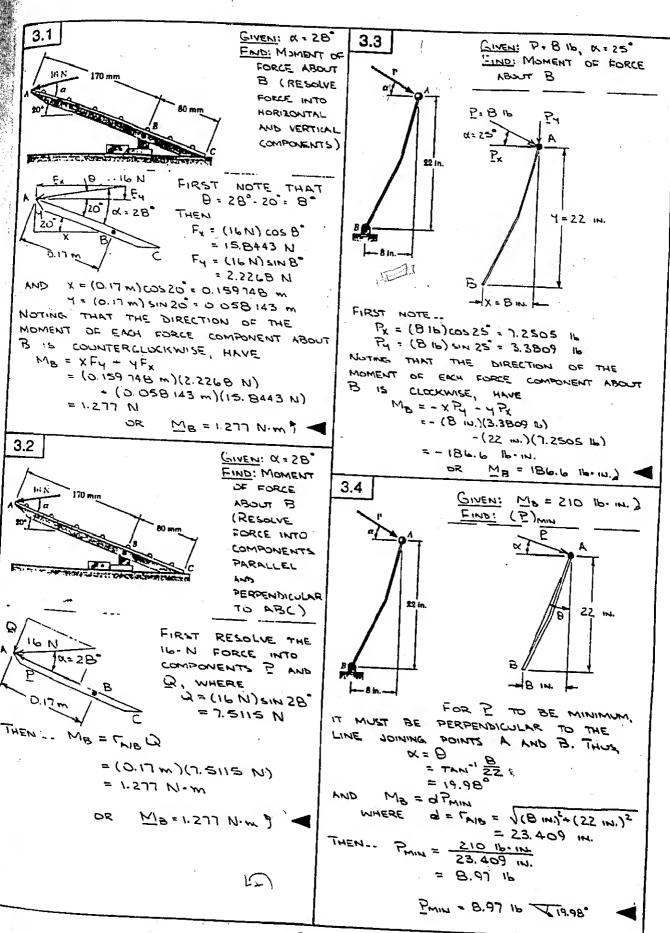
(b) FREE BODY : COLLAR B

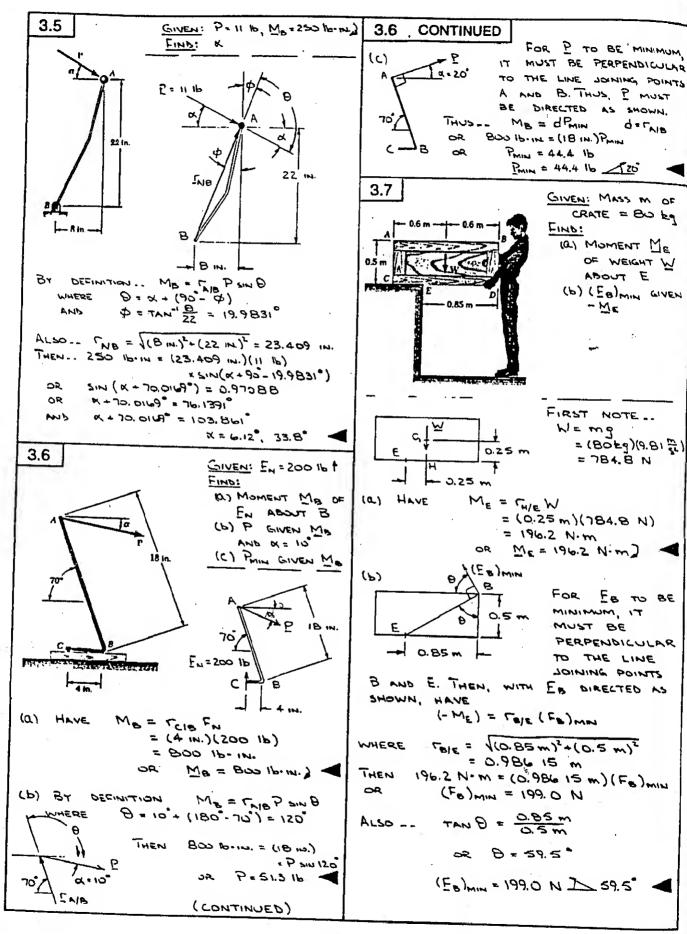
Ni + Ny j + Q K - TAB 2 AB =0 SUBSTITUTING FOR 2 AM SETTING THE COEFT OF K EQUAL TO ZERO: Q - (460 TAB) = 0

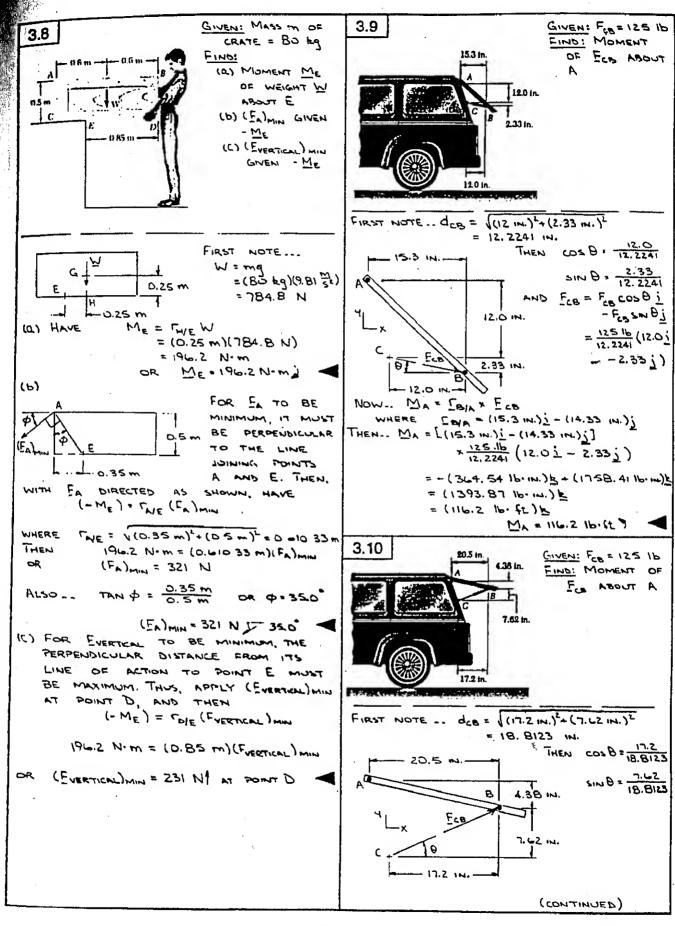
MAKING TAB = 1155 H AND SOLVING FOR Q:

Q = 460 (1155N)

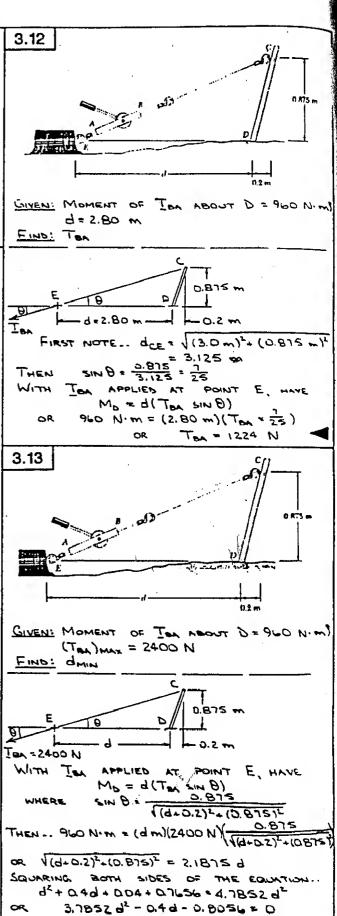
Q=1012 N







3.10 CONTINUED FCB = FCG COSD : + FCG SINB; = 125 16 18, 8123 (17.2 1 + 7.62) Now .. MA = IBIA * Eco WHERE [BIA = (20.5 IN.)] - (4.38 IN.) THEN. Mr = [(20.5 m.)i - (4.38 m.)j] x 125 1b (17.2 1 + 7.62) = (1037.95 16.1N.) 12+(500.58 16.10.) 1 = (1538.53 16.1N.) E = (128.2 16.51) = Mx = 128.2 16. 523 -3.11 0.875 m GIVEN: Top = 1040 N, d= 1.90 m. FIND! MOMENT OF TED ABOUT D; RESOLVE ICB INTO HORIZONTAL AND VERTICAL . COMPONENTS APPLIED AT (a) POINT ((b) POINT E 0.875 m - d=190 m -- X = 0.2 m FIRST NOTE .. de = 1(2.1 m) + (0.875 m)- $\cos \theta = \frac{2.1}{2.275} = \frac{12}{13}$ SIND = 0.875 = 5 THEN Tx = TcB cos 8 = (1040 N)(15) = 960 N Ty = Too SINB = (1040 N)(3) - 400 N (a) BY OBSERVATION. Mp = - XTy + YTx $M_b = (0.2 \, \text{m})(400 \, \text{N}) + (0.815 \, \text{m})(960 \, \text{N})$ = 760 N·m Mp = 760 N·m) (6) BY OBSERVATION .. Mo = dTy



(WHINUED)

= (1.90 m)(400 N)

= 760 N·m

Mo: The Nim >

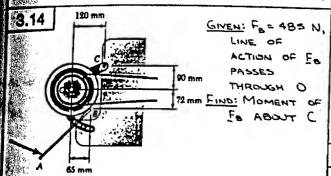
13 CONTINUED

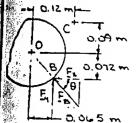
d = 0.4 = V(-0.4)=4(37852)(-0.8056)

REJECTING THE NEGATIVE ROOT

d=0.517 m

d= 517 mm





THEN COS 8 : 97 SINB. 72

Fy = Fo wn 0 = (485 N)(37) = 325 N

BY OBJERVATION. MC = - X Fy - y Fx
WHERE X = 0.12 m - 0.065 m = 0.055 m

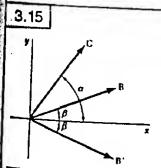
Y = 0.072 m + 0.09 m = 0.162 m

THEN MC = - (0.055 m)(360 N)

- (0.162 m)(325 N)

= -72.45 N·m

Mc = 72.5 N-m)



CIVEN: VECTORS B, B'
AND C
PROVE: SINK COBB

FIRST NOTE. B=B(cospi+ sinpj)

B'= B(cospi - SIMBI)

C = C (cosx 1 + sin a))

BY DEFINITION. $|\underline{B} \times \underline{C}| = B(\sin(x-\beta))$ (1)

1B'. C1 = BC SIN (N+B) (2)

(CONTINUED)

3.15 CONTINUED

Now Bx = B(cos Bi + smbi)
x C(cos x i + sm x i)

= BC (cosp sink - sinb cosk) (3)

AND B'x C = B(cospi - sinbi)

= BC (cosp sink + sinb cosk) = (4)

EQUATING THE RIGHT- HAND SIDES OF EQS.

(1) AND (2) TO THE MAGNITUDES OF THE

RIGHT- HAND SIDES OF EQS. (3) AND (4),

RESPECTIVELY, YIELDS...

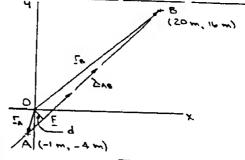
BC $sin(\alpha-\beta) = BC(cos\beta sin\alpha - sn\beta cosa)$ (S) BC $sin(\alpha-\beta) = BC(cos\beta sin\alpha + sin\beta cosa)$ (b)

 $(S)+(L) \Rightarrow \sin(k-\beta)+\sin(\alpha+\beta)=2\cos\beta\sin\kappa$ $\cos(\alpha+\beta)+\frac{1}{2}\sin(\kappa-\beta)$

3.16

GIVEN: POINTS (20m, 16 m) AND (-1 m, -4 m)

FIND: PERPENDICULAR DISTANCE &
FROM THE ORIGIN TO THE
LINE DRAWN THROUGH THE
POINTS



FIRST NOTE .. das = \(\langle 20 m - (-1m) \rangle^2 + \(\langle 1 m - (-4m) \rangle^2 + \langle 1 m - (-4m) \rangle 1 m - (-4m)

NOW ASSUME THAT A FORCE E, OF MAGNITUDE F, ACTS AT POINT A AND 12 DIRECTED FROM A TO B. THEN

WHERE LAB = TO-TA DAB

 $=\frac{29}{29}(21\frac{1}{2}+20\frac{1}{2})$

BY DEFINITION - Mo= | TA = F | = dF WHERE TA = -(1 m) 1 - (4 m) 1

THEN $M_0 = [-(1m)\underline{i} - (4m)\underline{i}] \times \frac{E}{29}(21\underline{i} + 20\underline{i})(N)$ = $\frac{E}{29}[-(20)\underline{k} + (84)\underline{k}]N \cdot m$ = $(\frac{64}{29}FN \cdot m)\underline{k}$

FINALLY .. (129 F) N. m = d(FN)

OR d= 64 m

d = 2.21 m

3.17 GIVEN: VECTORS A AND B
FIND: DUT VECTOR > NORMAL TO THE PLANE DEFINED BY A AND B WHEN (a) A = 1 + 21 - 5 & B = 41 - 71 - 5 & (b) A = 31 - 31 + 2 & B = -21 + 61 - 4 &
BY DECINITION, THE VECTOR $\underline{A} = \underline{B}$ is normal to the plane decined by $\underline{A} = \underline{A} + \underline{B}$ $\underline{\lambda} = \underline{A} + \underline{B}$
(a) Have
(b) Have 1; ; L1

(b) Have
$$\underline{A} \times \underline{B} = \begin{vmatrix} \underline{i} & \underline{j} & \underline{k} \\ 3 & -3 & 2 \end{vmatrix}$$

$$= (12 - 12)\underline{i} + (-4 + 12)\underline{j} \\
+ (18 - 6)\underline{k}$$

$$= 8\underline{j} + 12\underline{k}$$
THEN
$$|\underline{A} \times \underline{B}| = 4\sqrt{(2)^2 + (3)^2}$$

$$= 4\sqrt{13}$$

$$\vdots \quad \underline{\lambda} = \frac{1}{\sqrt{13}}(2\underline{j} + 3\underline{k})$$

GIVEN: ADJACENT SIDES P AND Q

FIND: AREA OF PARALLELOGRAM

. (a) P = -71+31-3k

OF A PARALLELOGRAM

3.18

 $\begin{array}{c|cccc}
Q & 2\frac{1}{2} + 2\frac{1}{2} + 5\frac{1}{2} \\
Q & 2\frac{1}{2} + 2\frac{1}{2} + 5\frac{1}{2} \\
Q & 2\frac{1}{2} - 2\frac{1}{2} \\
Q & 2\frac{1}{2} + 2\frac{1}{2} - \frac{1}{2}
\end{array}$ $\begin{array}{c|cccc}
AREA & A = |P & Q| \\
P & Q & = |-7 & 3 & -3| \\
2 & 2 & 5 & |
& 2 & 2 & 5 \\
\hline
P & Q & = |-7 & 3 & -3| \\
2 & 2 & 5 & |
& 2 & 2 & 5 \\
\hline
IHEN & A = \sqrt{(20)^2 + (29)^2 + (20)^2} & A = 41.0
\end{array}$ $\begin{array}{c|cccc}
P & Q & = |\frac{1}{2} & \frac{1}{2} & \frac{1}{2} \\
-2 & 5 & -1 \\
-2 & 5 & -1 \\
= (5 + 10)\frac{1}{2} + (4 + 6)\frac{1}{2} + (30 - 10)\frac{1}{2}
\end{array}$

= 151 + 101 +2012

THEN H = 5 ((3) 4 (2) 4 (4)6

3.19 GIVEN: FORCE E = 61 +41 - E ACTING AT POINT A FIND: MOMENT OF E ABOUT ORIGIN O WHEN (a) \(\Gamma_1 = -2\) + \(\frac{1}{2} + \frac{1}{2} \) + \(\frac{1}{2} \) (b) \(\Gamma_1 = -2\) + \(\frac{1}{2} + \frac{1}{2} \) + \(\frac{1}{2} \) (c) \(\Gamma_1 = -9\) - \(\frac{1}{2} + \frac{1}{2} \) + \(\frac{1}{2} \) (d) \(\frac{1}{2} = -9\) - \(\frac{1}{2} + \frac{1}{2} \) + \(\frac{1}{2} \) (e) \(\frac{1}{2} = -12\) + \(
EIND: MOMENT OF E ABOUT ORIGIN O WHEN (a) $\Gamma_A = -2i + \omega_1 + 3E$ (b) $\Gamma_A = 5i - 3j + 7E$ (c) $\Gamma_A = -9i - Uj + 1.5E$ BY DEFINITION MO = $\Gamma_A \times F$ (d) HAVE Mo = $\begin{bmatrix} 1 & 1 & E \\ -2 & 1 & 3 \end{bmatrix}$ = $\begin{bmatrix} -6 - 12 \end{bmatrix} + \begin{bmatrix} 16 - 2 \end{bmatrix} + \begin{bmatrix} -8 - 34 \end{bmatrix} E$ = $\begin{bmatrix} -18i + 1Uj - 44E \end{bmatrix}$ (b) HAVE Mo = $\begin{bmatrix} 1 & 1 & E \\ 5 & -3 & 7 \end{bmatrix}$ = $\begin{bmatrix} 3 - 28 \end{bmatrix} + \begin{bmatrix} 42 + 5 \end{bmatrix} + \begin{bmatrix} 20 + 18 \end{bmatrix} E$ = $\begin{bmatrix} 2 - 25i + 47j + 38E \end{bmatrix}$ (c) HAVE Mo = $\begin{bmatrix} -9 - 6 & 1.5 \\ -9 - 6 & 1.5 \end{bmatrix}$ = $\begin{bmatrix} 1 & 1 & E \\ -9 - 6 & 1.5 \end{bmatrix}$ = $\begin{bmatrix} 1 & 1 & E \\ -9 - 6 & 1.5 \end{bmatrix}$ NOTE: THE ANDWER TO PART C 13 AS EXPECTED SINCE Γ_A AND Γ_A ARE PROPORTIONAL (THUS, THEIR LINES OF ACTION ARE PARALLEL). 3.20 GIVEN: FORCE Γ_A SPOINT A ACTION ARE PARALLEL). GIVEN: FORCE Γ_A SPOINT A POINT A CTION OF Γ_A ACTION AT POINT A POINT A CTION OF Γ_A ACTION AT POINT A POINT A CTION OF Γ_A ACTION AT POINT A	3.19 GIVEN: FORCE E = 61 +41- & ACTING
(a) $\Gamma_{A} = -2\frac{1}{2} + \frac{1}{2} + \frac{3}{2} \frac{1}{2}$ (b) $\Gamma_{A} = -\frac{3}{2} - \frac{3}{2} + \frac{1}{2} \frac{1}{2}$ (c) $\Gamma_{A} = -\frac{9}{2} - \frac{1}{2} + \frac{1}{2} \frac{1}{2} \frac{1}{2}$ By DEFINITION $M_{0} = \Gamma_{A} \times \frac{1}{2}$ (a) Have $M_{0} = \begin{vmatrix} 1 & 1 & 1 & 1 \\ -2 & 1 & 3 & 1 \end{vmatrix}$ $= (-6-12)\frac{1}{2} + (18-2)\frac{1}{2} + (-8-34)\frac{1}{2}$ $= (-6-12)\frac{1}{2} + (18-2)\frac{1}{2} + (-8-34)\frac{1}{2}$ (b) Have $M_{0} = \begin{vmatrix} 1 & 1 & 1 & 1 \\ -3 & -3 & 7 & 1 \end{vmatrix}$ $= (3-28)\frac{1}{2} + (42+5)\frac{1}{2} + (20+18)\frac{1}{2}$ $= -25\frac{1}{2} + 47\frac{1}{2} + 38\frac{1}{2}$ (c) Have $M_{0} = \begin{vmatrix} 1 & 1 & 1 & 1 \\ -9 & -6 & 1.5 & 1 \end{vmatrix}$ $= -25\frac{1}{2} + 47\frac{1}{2} + 38\frac{1}{2}$ (c) Have $M_{0} = \begin{vmatrix} 1 & 1 & 1 & 1 \\ -9 & -6 & 1.5 & 1 \end{vmatrix}$ $= -25\frac{1}{2} + 47\frac{1}{2} + 38\frac{1}{2}$ (d) $\frac{1}{1} + \frac{1}{2} $	FIND: MOMENT OF F ABOUT ORIGIN
BY DEFINITION $M_0 = \Gamma_A * F$ (a) Have $M_0 = \begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1$	$(a) \underline{\Gamma}_{A} = -2\underline{i} + \underline{b}\underline{i} + 3\underline{k}$
(a) HAVE $M_0 = \begin{bmatrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1$	(C) IN = - 3! - C! + 1.2F
= (-6-12)i+(18-2)j+(-8-36)k = -18i+16j-44k = -25i+47j+38k = -25i+21+47j+38k = -25i+21+47j+38k = -25i+21+47j+38k = -25i+21+47j+38k = -25i+47j+38k = -25i+47j+38k = -25i+47j+38k = -25i+47j+38k = -25i+47j+38k = -25i+21+47j+38k = -25i+47j+38k = -25i+47j+38k = -25i+47j+38k = -25i+21+47j+38k = -25i+47j+38k = -25i+47j+38k = -25i+47j+38k = -25i+21+47j+38k = -25i+47j+38k = -25i+47j+48k = -25i+48k = -25i+47j+48k = -25i+48k = -25i+48k = -25i+47j+48k = -25i+47j+48k = -25i+47j+48k = -25i+47j+48k = -25i+47j+48k = -25i+47j+48k = -25i+48k = -25i+48k = -25i+48k = -25i+48k = -25i+47j+48k = -25i+48k	BY DEFINITION MO = TA * F
=-18:+16:-44 E (b) Have Mo = 1 1 E = (3-28):+(42+5):+(20+18)E = -25:+47:+38 E (c) Have Mo = -9 -6 1.5 = (6-6):+(9-9):+(-36+36)E NOTE: THE ANSWER TO PART C 18 AS EXPECTED SINCE IN AND E ARE PROPORTIONAL (THUS, THEIR LINES OF ACTION ARE PARALLEL). 3.20 Given: Force E = 2:-7:-3E ACTING AT POINT A FIND: Moment OF E ABOUT ORIGIN O WHEN (a) In = 4:-3:-5E (b) In = -8:-2:+E	6 4 -1
(b) Have $M_0 = \begin{vmatrix} \frac{1}{5} & \frac{1}{5} & \frac{1}{5} & \frac{1}{5} \\ & \frac{1}{5} & \frac{1}{5} & \frac{1}{5} \end{vmatrix} = (3-28)\frac{1}{5} + (42+5)\frac{1}{5} + (20+18)\frac{1}{5}$ $= (3-28)\frac{1}{5} + (42+5)\frac{1}{5} + (20+18)\frac{1}{5}$ $= -25\frac{1}{5} + 47\frac{1}{5} + 38\frac{1}{5}$ (c) Have $M_0 = \begin{vmatrix} \frac{1}{5} & \frac{1}{5} & \frac{1}{5} \\ -9 & -6 & 1.5 \end{vmatrix}$ $= -25\frac{1}{5} + 47\frac{1}{5} + 38\frac{1}{5}$ (d) Have $M_0 = \begin{vmatrix} \frac{1}{5} & \frac{1}{5} & \frac{1}{5} & \frac{1}{5} \\ -1 & \frac{1}{5} & \frac{1}{5} & \frac{1}{5} & \frac{1}{5} & \frac{1}{5} \\ -1 & \frac{1}{5} & \frac$	
$= -25\frac{1}{2} + 47\frac{1}{2} + 38\frac{1}{12}$ $= (6-6)\frac{1}{2} + (9-9)\frac{1}{2} + (-36+36)\frac{1}{2}$ $= (6-6)\frac{1}{2} + (9-9)\frac{1}{2} + (-36+36)\frac{1}{2}$ $= 0$ Note: The answer to part c is as $= 27 + 27 + 27 + 27 + 27 + 27 + 27 + 27 $	(b) HAVE Mo = 1 1 k 5 -3 7 6 4 -1
= (6-6)]+(9-9)]+(-36+36)E = 0 NOTE: THE ANSWER TO PART C IS AS EXPECTED SINCE IN AND IT ARE PROPORTIONAL (THUS, THEIR LINES OF ACTION ARE PARALLEL). 3.20 GIVEN: FORCE I = 21-71-3E ACTING AT POINT A FIND: MOMENT OF IT ABOUT ORIGIN O WHEN (a) IN = 41-31-5E (b) IN = -81-21+E	=-25 <u>i</u> +47j +38k
EXPECTED SINCE IN AND E ARE PROPORTIONAL (THUS, THEIR LINES OF ACTION ARE PARALLEL). 3.20 GIVEN: FORCE E = 21-71-36 ACTING AT POINT A FIND: MOMENT OF E ABOUT ORIGIN O WHEN (a) IN = 41-31-56 (b) IN = -81-21+6	= (0-6)7+(0-0)7+(-30+34)F
PROPORTIONAL (THUS, THEIR LINES OF ACTION ARE PARALLEL). 3.20 GIVEN: FORCE E = 21-71-36 ACTING AT POINT A FIND: MOMENT OF E ABOUT ORIGIN O WHEN (a) TA = 41-31-56 (b) TA = -81-21+6	EXPECTED SINCE IN AND F ARE
SNEN: FORCE $F = 2j - 7j - 3k$ ACTING AT POINT A FIND: MOMENT OF F ABOUT ORIGIN O WHEN (a) $f_A = 4j - 3j - 5k$ (b) $f_A = -8j - 2j + k$	PROPORTIONAL (THUS, THEIR LINES OF ACTION ARE PARALLEL).
EIND: MOMENT OF E ABOUT ORIGIN (a) [= 4] - 3] - 5] (b) [= -8] - 2] +]	PUNEN: LOUCE F = SI-11-35
(b) [x = -8j = 2j + k	FIND: MOMENT OF F ABOUT ORIGIN
	(b) cx = -Bi = 2j + k

O WHEN	DEICIN
(a) [= 4i - 3j - 5k	
(b) [x = -8j - 2j + k	
(c) [x = 1-3.5]-1.5k	
BY DEFINITION MO = TA X F	
(a) HAVE Mo . 4 .3 -5	
= (9-35) <u>i</u> +(-10+12)j+¢28	<i>+د)لا</i>
- 5:1 . 5:	

(b) HAVE...
$$M_0 = \begin{vmatrix} 1 & 1 & 1 & 1 \\ -8 & -2 & 1 \\ 2 & -7 & -3 \end{vmatrix}$$

$$= (6+7)\underline{1} + (2-24)\underline{1} + (56+4)\underline{1}$$

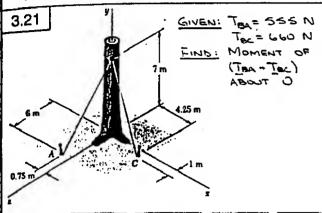
$$= 13\underline{1} - 22\underline{1} + 10\underline{1}$$
(c) HAVE... $M_0 = \begin{vmatrix} 1 & 2 & 1 \\ 1 & 2 & 1 \\ 1 & 2 & 1 \end{vmatrix}$

(C) HAVE -. Mo = 1 -3.5 -1.5 | = (10.5-10.5).+ (-3+3)..+ (-7+7) & = 0 (CONTINUED)

A=26.9.



NOTE: THE ANSWER TO PART C IS AS
EXPECTED SINCE IN AND E ARE
PROPORTIONAL (THUS, THEIR LINES OF
ACTION ARE PARALLEL).



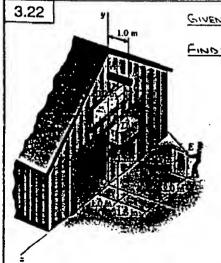
FIRST NOTE --
$$d_{BA} = \sqrt{(-0.75)^2 + (-7)^2 + (6)^2}$$

 $= 9.25' \text{m}$
 $d_{BC} = \sqrt{(4.25)^2 + (-7)^2 + (1)^2}$
 $= 8.25 \text{ m}$
Now. $\underline{T}_{BA} = \frac{T_{BA}}{d_{BA}} \underline{BA} = \frac{545 \text{ N}}{9.25} (-0.75i - 7j + 6k)$
 $= -(45 \text{ N})i - (420 \text{ N})j + (340 \text{ N})k$

AND
$$Toc = \frac{Toc}{doc} \frac{1}{BC} = \frac{GLON}{B.25} (4.25i-7j+1)$$

= (340 N)i - (560 N)j + (80 N)1

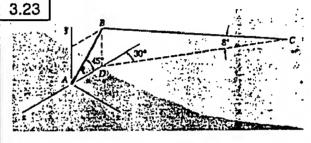
= (3080 N·m)i - (2065 N·m)k Mo = (3080 N·m)i-(2010 N·m)k



GIVEN: MASS IN OF
BALE = 26 kg
FIND: MOMENT ABOUT
A OF RESULTANT
FORCE EXERTED
ON THE
PULLEY BY
THE ROPE

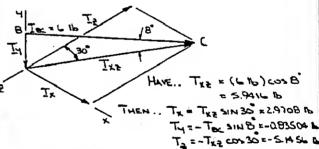
(CONTINUED)

3.22 CONTINUED



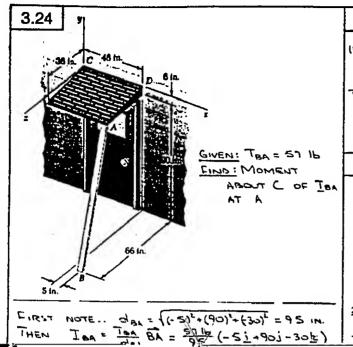
OR MA = 123.5 N·m) + (78.5 N·m) = -(473 N·m) =

GIVEN: dag = L ft, Toc = L 16
FIND: MOMENT ABOUT A OF Toc AT B



NOW. Mx = [8/x * Tec WHERE [8/x = (L + 1145)] - (L cos 45) } = \frac{12}{12} (\frac{1}{2} - \frac{12}{12})

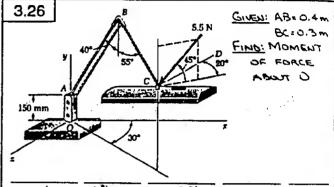
호(80162-) 를 - i(8016.2) 를 - 보(81662-) 를 - 전 (82162-) 표 50 보 선(81616-) - (12164-) - 1(121

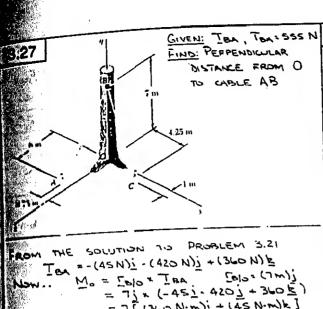


3.25 CONTINUED

16) NOW - MA = COLA = T CO WHERE COLA = (2.7 m) = +(2.3 m) = 1 2 E THEN .. MA = 54 2.7 2.3 0 -2 11 -10

= 54[-23<u>i</u> +27<u>i</u> +(29.7+4.6)} OR MA =- (1242 N.m)<u>i</u>+(1458 N.m)<u>i</u>+(1852.N.m)<u>k</u> =





ROM THE SOLUTION TO PROBLEM 3.21

Tex = -(45N): -(420N): +(360N) k

NOW.. Mo = Telo * Tex Telo: (7m);

= 7 [(360N·m): +(45N·m)k]

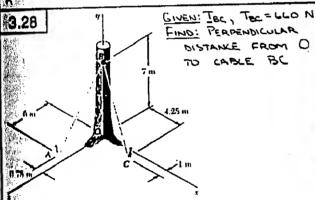
THEN.. Mo = 7 V(360)² + (45)²

= 2539.6 N·m

ALSO.. Mo = dTex

OR 2539.6 N·m: d·555 N

DR d-4.50 m



FROM THE SOLUTION TO PROBLEM 3.21

The = (340 N)i - (560 N)j + (80 N)k

Now .. Mo = [810 x] & [810 = (7 m)j

= 7j x (340i - 560j + 80k)

= 7[(80 N·m)i - (340 N·m)k]

THEN .. Mo = 7 ((80)² + (-340)²

= 2445.0 N·m

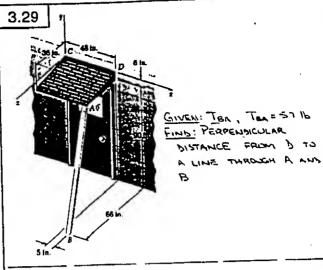
ALSO .. Mo = d The

OR 2445.0 N·m · d·660 N

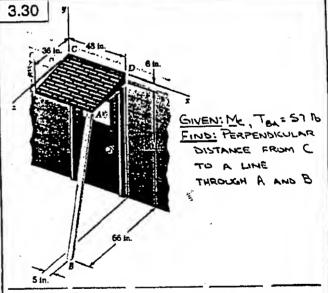
OR d = 3.70 m

ALSO.

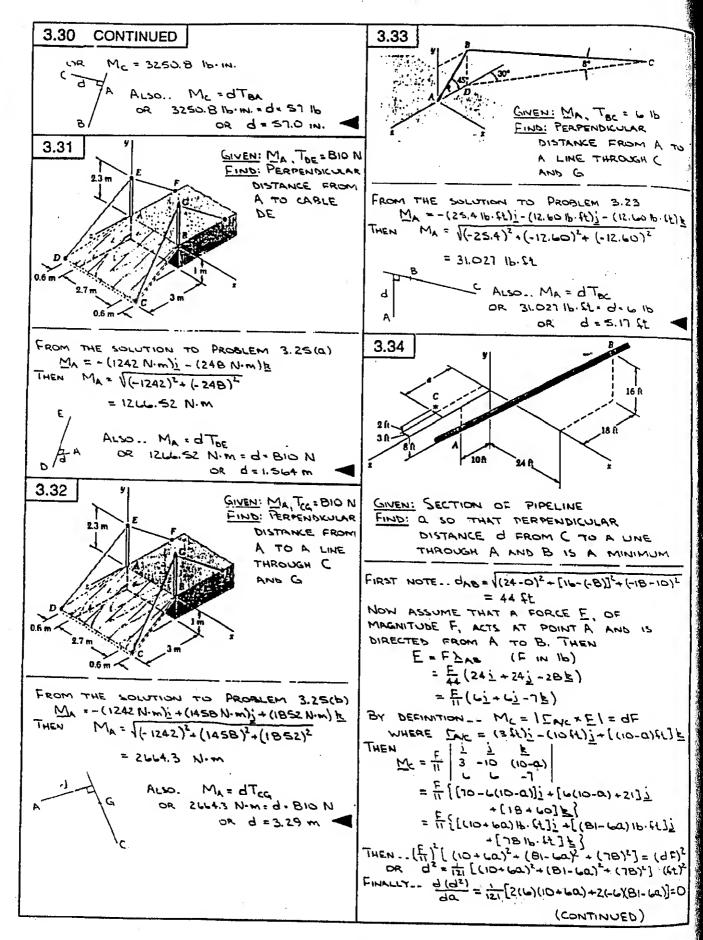
MA = dTca



FROM THE SOLUTION TO PROBLEM 3.24 Ten = 3[-(1 16) + (18 16) - (6 16) }] NOW .. MO = TAID * IBA WHERE [AID = - (6 IN)] + (36 IN) & = 6[- (1 112)] + (6 112)] THEN. $M_b = (3)(4)$ [# - Pa - 186 (10 - 108)] - 181 = = 18[(-102 lb.in.)i-(6 lb.m.)j -(1 1P·1M·) F] Mp = 18 /(-102)2+(-6)2+(-1)2 DUA = 1839.26 16.1N. ALSO .. MD = dTox OR 1839.26 16.1N = d. 57 16 d=32.3 m. 02



FROM THE SOLUTION TO PROBLEM 3.24 $M_{c} = -(1836 + (156 + (156 + (2574 + (2574 + (156 + (2574))^{2} + (2574)^{2})^{2} + (2574)^{2})$ THEN $M_{c} = \sqrt{(-1836)^{2} + (756)^{2} + (2574)^{2}}$ (CONTINUES)



CONTINUED 3.34

(10+60) - (81-60) =0 OR SO THAT FOR MIN

a=5.92 st

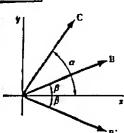
GIVEN: P = 41 + 31 - 2k 3.35

$$P-\underline{S} = (4\underline{1} + 3\underline{j} - 2\underline{k}) \cdot (\underline{i} + 4\underline{j} + 3\underline{k})$$

= $(4)(1) + (3)(4) + (-2)(3)$
OR $P \cdot \underline{S} = 10$

THUS Q AND S ARE PERPENDICULAR

3.36



GIVEN: B, B, AND C PROVE: COSK COSA = { cos(x+ B) + 2 cos(x-B)

FIRST NOTE.. $B = B(\cos \beta i + \sin \beta i)$ B' = B(cospi - sinbi) C = C (cosa i + sina i)

BY DEFINITION. B.C = BC cos
$$(\alpha - \beta)$$
 (1)
B'.C = BC cos $(\alpha + \beta)$ (2)

Now B.C = B(cos Bi+ smbj)

· C(coski + sinaj) = BC (cosp cosx + SNB SMX) (3)

B.C = B(corpi- 2ngi)

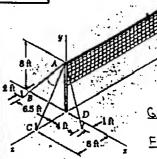
· C (coski + smkj)

= BC (cos B cosx - SWB sina) = (4) EQUATING THE RIGHT-HAND SIDES OF EQS. (1) AND (2) TO THE RIGHT-HAND SIDES OF EQS. (3) AND (4), RESPECTIVELY, YIELDS $BC \cos(\alpha - \beta) = BC (\cos \beta \cos \alpha + \sin \beta \sin \alpha)$ (5) BC cos (x+B) = BC (cosp cosx - snp snx) (6

(5)+(6)=> (05(x-1)+cos(x+B)=2cosBcosa

OR COSK COSB = { COS(K+B)+ { COS(K-B) €

3.37



GIVEN: GUY WIRES AB AND AC

FIND: ANGLE & FORMED BY AB AND AC

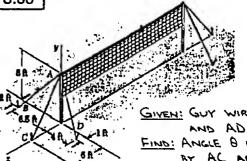
"IPST NOTE .. AB = 1(-6.5)2 - (-B)2 - (2)2 = 10.5 St AC = 1(3)2+(-8)2+(6)2

= 10 ft AND AB = - (6.512) - (B SL) - (2 ft) E YC = - (8 24)? - (6 64) F

BY DEFINITION .. AB. AC = (AB)(AC) cos B OR (-6.51-81+24).(-81+6/)=(10.5)(10)cos0 (-6.5)(0)+(-B)(-B), (E)(6) = 105 cos g

> OR COSD = 0.723 B1 OR 0 = 43.6°

3.38



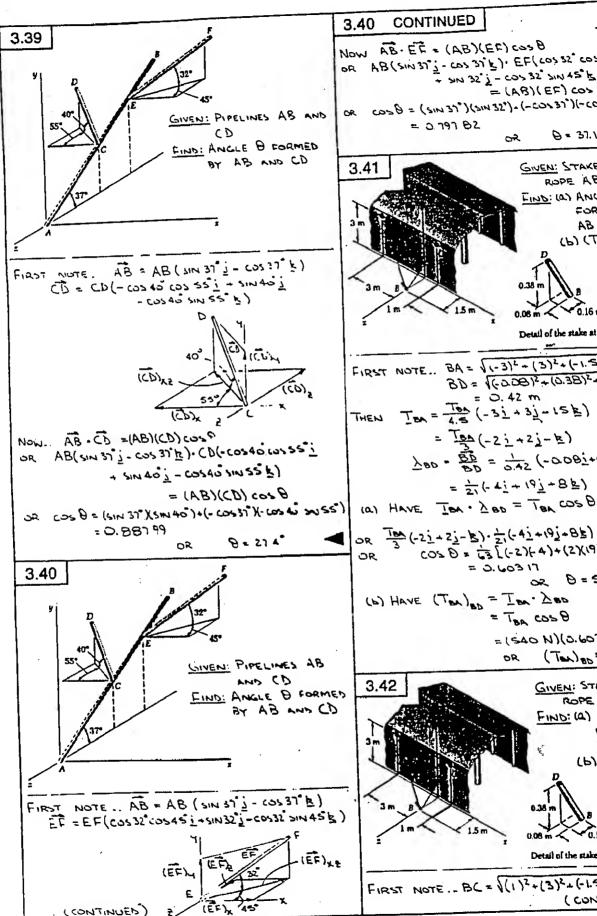
GIVEN: GUY WIRES AC

FIND: ANGLE B FORMED BY AC AND AD

FIRST NOTE __ AC = 1(0)2+(-8)2+(C)2 = 10 It $AD = \sqrt{(4)^2 + (-8)^2 + (1)^2}$ = 9 ft

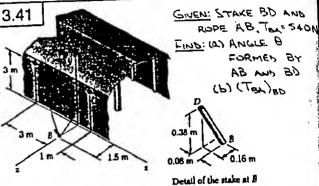
AND AC = - (B St)] + (L St)] $A\bar{D} = (4 \text{ ft})\underline{i} - (8 \text{ ft})\underline{i} + (1 \text{ ft})\underline{k}$

BY DEFINITION -- AC. AD = (AC)(AD) cos B OR (-Bj+6E). (4j-Bj+E) = (10)(9) cosB $(0)(4) + (-8)(-8) + (6)(1) = 90 cor \theta$ פר ררה.ס = 6 אס OR P. 38.9



CONTINUED 3.40

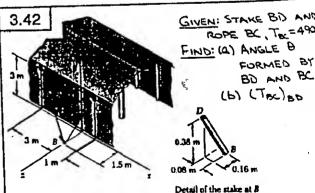
Now AB. ET = (AB)(EE) cos B OR AB(SIN3) 1- COS 3) 1). EF(COS 52° COS 45') + >1 32 1 - CO> 32 214 45 6) = (AB)(EF) co> 0 OR COSO = (SIN 37°)(SIN 32°)- (-COS 37°)(-COS 32° SIN 450) 29 rer c = B = 37.1°



FIRST NOTE.. BA = V(-3)2+(-1.5)2 = 4.5 m BD = 1(-00012+(0.38)2+(0.16)2 TEX = TOX (-31+31-15E) THEN = Ton (-2 1 +2j- E) 180 - BD = 0.42 (-0.08:+0.38)+0.16 = 1/2 (- 41/2 + 191/2 + 8 E)

OR TEA (-21+21-18) - 1 (-41+191+81) = TEA COSB COS 0 = 63[(-2)(4)+(2)(19)+(-1)(8)] = 3.60317 02 B=52.9°

(b) HAVE (TON) = Im. ZOD = TBA COSB = (SAO N)(0.603 17) (Tex) 80 = 326 N

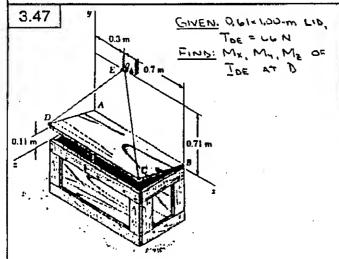


FIRST NOTE .- BC = \((1)^2 + (3)^2 + (-1.5)^2 = 35 m (CONTINUED)

GIVEN: P = 31 - 1+ 1 3.46 Q . 41 - Q41 - 2E 5 = 21 - 25 + 2k FIND: DY SO THAT P. Q. AND S ARE COPLINAR

IF P. Q. AND & ARE COPLANAR, THEN P. MUST BE PERPENDICULAR TO (Q+). ∴ 5. (♂ = ≥) = 0 COR THE VOLUME OF THE PARALLELOGRAM DEFINER BY P. W. AND & IS LERO). THEN 4 0- -2 ÷ 0 -2 2 604 + 4 - B - 204 + B - 12 =0

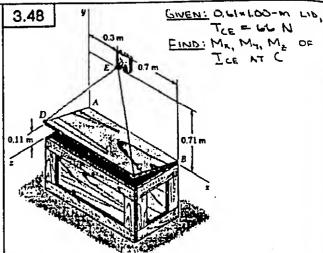
Dy = 2



FIRST NOTE .. 2 = ((0,41)2-(0.11)2 = 0.60 m

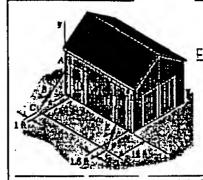
doE = 1(0.3)2 - (06)2+(-0.6)2 = 0.9 m THEN AND THE = (0.31 + 0.61 - 0.6) = 22 [(1 N) + (2 N) - (2 N) k]

Now - Mr = Tol + Toe [NY = (0.11 W)] + (0.00 W) F THEN .. MR = 22 = 28[(-0.88-180)j+0.60j-0.11 <u>k</u>] =-(31.24 N·m) + (13.20 N·m) - (2.42 N-m) k : Mx =-31.2 N·m, My=13.20 N·m, Mz=-2.42 N·m THEN .. TAB = TAB (-1-12)+12 k) (16)



FIRST NOTE .. 2 = 1(0.61)2 - (0.11)2 = 0.60 m dce = 1(-0.7)2+(0.6)2+(-0,6)2 = 1.1 m THEN Ice = 46N (-0.71+0.61-0.68) and = C[-(7N) + (6N) - (6N) k] NOW -- MA = TELL + TLE WHERE TEIN : (0.3 m) 1+(0.71 m) THEN .. Mx = 6 0.3 0.71 0 = 6[-4.261 +1.81+(1.8+4.97)] =- (25.56 N·m) - (1080 N·m); + (40.62 N·m) k

: Mx = -25,6 N·m, My=10.80 N·m, Mz=40.6 N·m 3.49 and 3.50



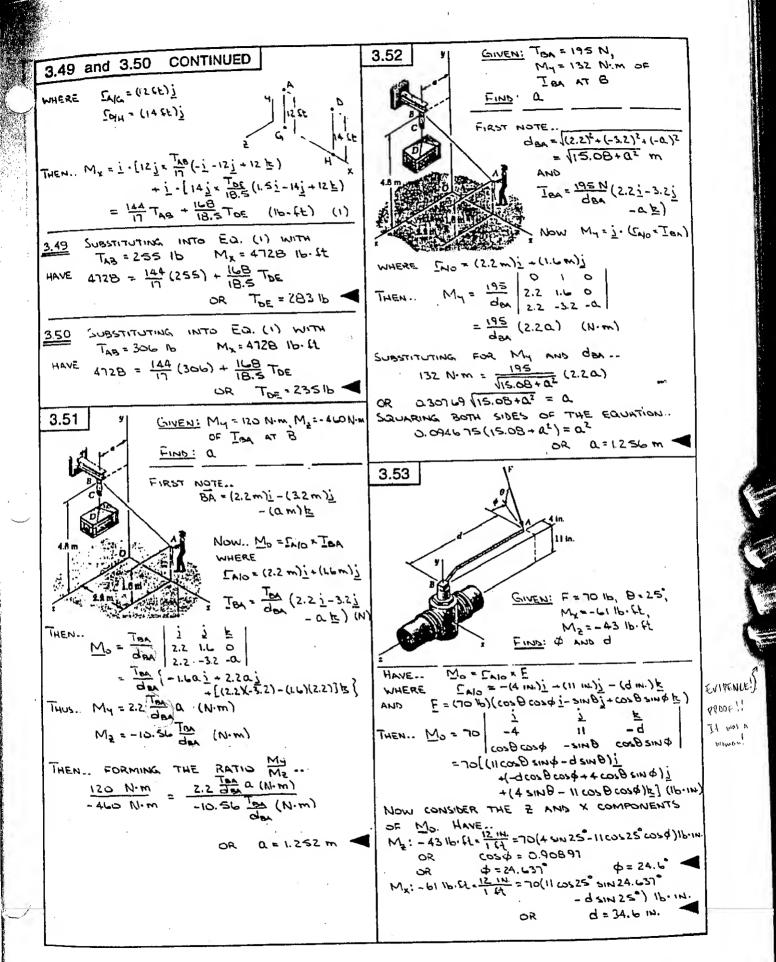
GIVEN: TAB, Mx OF OHA (A TA) BAT IDE (AT D) = 4728 Ib.ft FIND: TDE

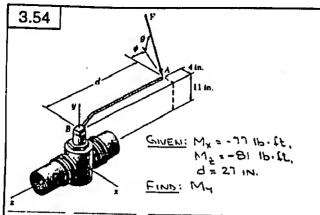
FIRST NOTE .. dAC = \((-1)^2 + (-12)^2 + (12)^2 = 17 Lt dof = V(1.5)2+(-14)2+(12)2 =18.5 \$1

HEN -
$$\frac{1}{2}PE = \frac{18}{12}(-5 - 157 + 15F)$$
 (1P)

Now. Mx = (Tric + Tro) + 1 - (Tolu + Tre)

(CONTINUED)





Mo = CAID = E WHERE [Alo = - (4 IN.) + (11 IN) - (27 IN.)] AND E = F(cosB cospi-sinDj+cosB sind k) THEN .. M₃ = F COSB COSO - SINB COSB SIND = F[(11 cos 8 sin 4 - 27 sin 8) i + (-27 cos8 cos+ +4 cos8 sin4)j + (4 SINB - 11 COSB COSA)] (IFIN) TAMT OC $M_x = F(11\cos\theta\sin\phi - 27\sin\theta)$ $M_Y = F(-27\cos\theta\cos\phi + 4\cos\theta\sin\phi)$ (2) $M_2 = F(4 \sin \theta - 11 \cos \theta \cos \phi)$ WHERE Mx, My, AND MZ ARE IN 16.14. Now. ED (1) => COSB 2ND = 11 (Wx + 51 2NB)

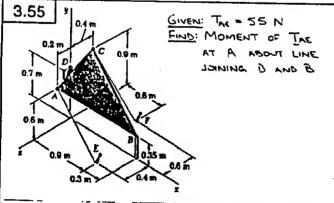
Eq. (3) => $\cos \theta \cos \theta = \frac{1}{11} \left(4 \sin \theta - \frac{M_2}{F} \right)$ (5) Substituting Eqs. (4) and (5) into Eq. (2) YIELDS

 $M_{Y} = F_{1}^{f} - 27 \left[\frac{1}{11} (4 \sin \theta - \frac{M_{2}}{F}) \right] + 4 \left[\frac{1}{11} (\frac{M_{x}}{F} + 27 \sin \theta) \right]$ $= \frac{1}{11} (27 M_{2} + 4 M_{x})$

Noting that the ratios II AND II ARE THE RATIOS OF LENGTHS, HAVE ..

 $W^{d} = \frac{11}{5J} (-81 \text{ IP} \cdot tf) + \frac{11}{4} (-JJ \text{ IP} \cdot tf)$

OR My = - 227 16. St



FIRST NOTE.. $d_{NE} = \sqrt{(0.9)^2 + (-0.6)^2 + (0.2)^2 = 1.1} m$ THEN.. $T_{NE} = \frac{55}{1.1} N (0.9i - 0.6i + 0.2k)$ = 5[(9 N)i - (6 N)i + (2 N)k](CONTINUES)

3.55 CONTINUED

ALSO..
$$DB = \sqrt{(1.2)^2 + (-0.35)^2 + (0)^2} = 1.25 \text{ m}$$

THEN $\Delta DB = \frac{DB}{DB} = \frac{1}{1.25}(1.2i - 0.35i)$
 $= \frac{1}{25}(24i - 7i)$

Now. Mos =
$$\frac{1}{208} \cdot (\frac{1}{140} \times \frac{1}{140})$$

WHERE $\frac{1}{120} = -(0.1 \text{ m}) \cdot \frac{1}{2} + (0.2 \text{ m}) \cdot \frac{1}{12}$
THEN. $\frac{1}{20} = \frac{1}{20} \cdot (5) \cdot \frac{1}{20} = -0.1 \cdot 0.2$
 $\frac{1}{20} = \frac{1}{20} \cdot (-4.8 - 12.6 + 28.8)$
OR $\frac{1}{20} = 2.28 \cdot 1.20$

3.56

0.2 m

COLUMN: Top = 33 N

FIND: MOMENT OF TOP

AT (ABOUT LINE

DOINING D AND B

0.5 m

0.5 m

0.5 m

0.5 m

FIRST NOTE..
$$d_{CE} = \sqrt{(0.6)^2 + (-0.9)^2 + (-0.2)^2} = 1.1 \text{ m}$$

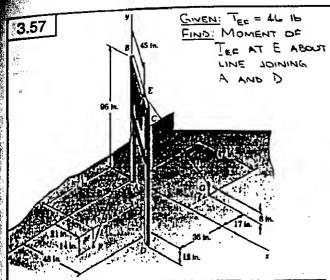
THEN. $T_{CE} = \frac{33 \text{ N}}{1.1} (0.6 \frac{1}{2} - 0.9 \frac{1}{2} - 0.2 \frac{1}{2})$
 $= 3[(L N)\frac{1}{2} - (9 N)\frac{1}{2} - (2 N)\frac{1}{2}]$

ALSO.. $DB = \sqrt{(12)^2 + (-0.35)^2 + (0.5)^2} = 1.25 \text{ m}$

THEN $\frac{1}{2} DB = \frac{DB}{DB} = \frac{1}{1.25} (12\frac{1}{2} - 0.35\frac{1}{2})$
 $= \frac{1}{25} (24\frac{1}{2} - 7\frac{1}{2})$

WHERE
$$\frac{1}{100} = \frac{1}{100} = \frac{1}{100}$$

OR MOB = -950 N.m



FIRST NOTE THAT $BC = (4B)^2 \cdot (3C)^2 = LO$ IN.

AND THAT $BC = \frac{45}{LO} = \frac{2}{4}$ THE COORDINATES

OF POINT E ARE THEN (3-40,96, 3-36) OR (36 IN, 96 IN, 27 IN.). THEN ..

der = ((-15)2+ (-110)2+(30)2 = 115 in.

THEN. TEE = 46 b (-151-1101 + 30 k)

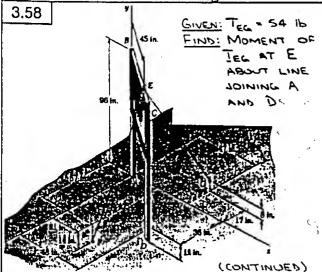
= 2 [-(3 16)] - (22 16)] + (6 16)] ALSO - AD = (48)2+(-12)2+(36)2 = 12 126 1N. THEN DAD = AD = 1212 (4B2-12] + 36E)

 $=\frac{1}{12}(4i-i-3k)$

NOW -. MAD = \(\(\tilde{L}\) AD . (\(\tilde{L}\) Ex \(\tilde{L}\) Ex \(\tilde{L}\) WHERE .. [EIN = (36m)] + (96 m) = (27 m) }

THEN .. MAD = 1/(2) 36 96 27 = (2304+81-2576+84+216+2576)

OR MAN : 1359 16-14.



3.58 CONTINUED

FIRST NOTE THAT BC = $\sqrt{(4B)^2+(3L)^2}$ = 60 in. AND THAT BC = 45: 3. THE COORDINATES OF

POINT E ARE THEN (3.48, 96, 3:36) OR

THEN .. TEG = 99 (11: - 88: - 44 k)

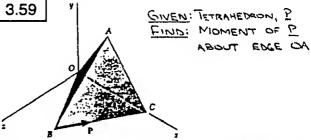
ALSO. AD = V(4B)2-(-12)2-(36)2 = 12(26 10. THEN 1 An = AD = 12(26 (481-121+36E)

= = (41-1+34)

NOW -. MAD = LAB - (TEM = TEG) WHERE TEN = (36 in.) + (96 in.) + (27 in.) E

96 27 THEN MAN = (25 (6) 36 = 126 (-1536-27-864-288-144-864)

OR MAD = - 23 SO 16.1N.



FIRST CONSIDER TRIANGLE OBC. WITH THE LENCTH OF THE SIDES OF THE TRIANGLE EQUAL TO Q, HAVE. BC = a cos 601 - a sin 60 k $\overline{Y} = \frac{5}{5}(\overline{1} - \sqrt{3} \overline{K})$ P = P>= = = (i - 13 k)

TO DETERMINE DON, FIRST OBSERVE THAT KAOC = 60. THE PROJECTION OF OA ON THE X AXIS IS THEN

(DA) = a cos 60 = 2 ALSO, THE PROJECTION OF OA ONTO THE X2 PLANE BISECTS & BOX, WHERE & BOX

= 60. THEN, EROM THE EXETCH .. $(OA)_{s} = (OA)_{s} + (AG)_{s} = \frac{Q}{2\sqrt{3}}$ x(AO) NOW. : (OA)2 + (OA)2 - (OA)2 (AO) a2 = (2)2 + (OA)2 + (2(3)2

THEN .. OA = 2 + 0 = 00 (OA) = 0 = 0 THAT DOR = 21 + 121 + 20 E

(CONTINUED)

3.59 CONTINUED

FINALLY.. $M_{OA} = \lambda_{OA} \cdot (\frac{r}{c_{O}} \cdot \frac{P}{2})$ WHERE $\frac{r}{c_{OO}} = \frac{\alpha_1}{2}$ THEN.. $M_{OA} = \frac{\alpha(\frac{P}{2})}{2}$ $\frac{1}{2} \cdot \frac{\sqrt{3}}{3} \cdot \frac{2(3)}{2(3)}$ $\frac{1}{2} \cdot \frac{\sqrt{3}}{3} \cdot \frac{2(3)}{3}$ $\frac{1}{2} \cdot \frac{\sqrt{3}}{3} \cdot \frac{\sqrt{3}}{3}$ $\frac{\alpha^2}{\sqrt{2}}$ $\frac{1}{2} \cdot \frac{\sqrt{3}}{\sqrt{2}} \cdot \frac{\alpha^2}{\sqrt{2}}$

GIVEN. TETRAHEDRON, P.

MOA OF P.

(A) SHOW: OA AND BC ARE

PERPENDICULAR

(b) FIND: PERPENDICULAR

DISTANCE BETWEEN

C. OA AND BC

A) 0 C FIRST CONSIDER TRIANGLE

| 1600 \times DBC. WITH THE LENGTH OF

THE SIDES OF THE

TRIANGLE EDWAL TO Q, HAVE.

BC = Q (03 60 1-0 50 6)

= $\frac{Q}{2}(\frac{1}{2} - \sqrt{3} \frac{1}{2})$

To determine \overrightarrow{OA} , first observe that \overrightarrow{AAC} = 60. The projection of \overrightarrow{OA} on the X axis is then $(\overrightarrow{OA})_X = 0$ as $0 = \frac{0}{2}$

ALSO, THE PROJECTION OF DA ONTO THE X2 PLANE BISECTS & BOX, WHERE & BOX = 60. THEN, FROM THE SKETCH.

THUS, BC.OA = & (i-13k)-[&i-(OA)1-26k] 3.62

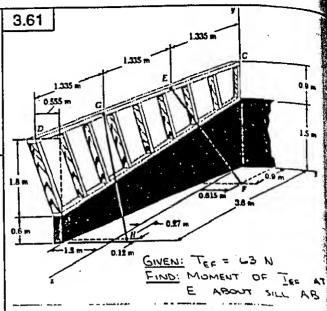
.: BC·OA+O ⇒ BC AND OC ARE PERPENDICULAR ■

(b) Since OA is perpendicular to BC,
AND THUS TO P, IT FOLLOWS THAT

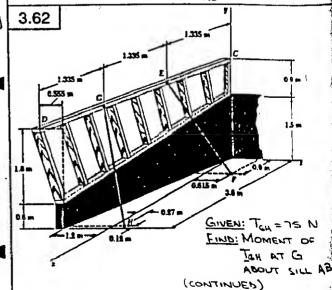
MOA = dP

WHERE d is the Perpendicular distance between DA and BC and from the solution to Problem 3.59 $M_{OA} = \frac{1}{12} QP$

THEN.. $\frac{1}{\sqrt{2}} QP = dP$ OR $d = \frac{Q}{\sqrt{2}}$



FIRST NOTE THAT $(E = \frac{1}{3}(D))^2 + (-2.4)^2$ $dE = \frac{1}{3}(0.555+1.2)+0.615]^2 + (-2.4)^2$ $+ [0.9 - (\frac{1}{3}x.3.6)]^2]^{\frac{1}{2}}$ $= \sqrt{(x.2)^2 + (-2.4)^2 + (-0.3)^2} = 2.7 \text{ m}$ AND $T_{EC} = \frac{63}{2.7}(1.2\frac{1}{2} - 2.4\frac{1}{2} - 0.3\frac{1}{2})$ $= 7[(4N)\frac{1}{2} - (8N)\frac{1}{2} - (1N)\frac{1}{2}]$ ALSO... $AB = \sqrt{(1.2)^2 + (0.9)^2 + (-3.6)^2} = 3.9 \text{ m}$ THEN $\Delta AB = \frac{1}{3.9}(1.2\frac{1}{2} + 0.9\frac{1}{2} - 3.6\frac{1}{2})$ $= \frac{1}{13}(4\frac{1}{2} + 3\frac{1}{2} - 12\frac{1}{2})$



3.62 CONTINUED

FIRST NOTE THAT (G = 3 CD don = [[2 (0.555+1.2)+0.27]2+ (-2.4)2 + [(3,6-0.12)-(3 +3.4)]2"/2 = \(\((1.44)^2 + (-2.4)^2 - (1.08)^2 - 3 m) AND ICH = 75N (1.441-2.41+1.08 12) 1 3[(12 N) : - (20 N) ; + (9 N) E] ALSO. AB = V(1.2)2+(0.9)2+(-3.6)2 = 3.9 M THEN .. \$ 48 = 3.9 (1.21 + 0.91 - 36 12) = 13 (41 + 35=12/E) MAB = ZAB · ([THIN TCH)

WHERE [HA = (1.47 m) - (0.6m) - (0.12 m) k MAB = 13 (3) 1.47 -0.6 -0.12 THEN --12 -20 = 3 (-216-4.32+352.8-86.4-39.69-9.6) MAB = 44.1 N.m

3.63 GIVEN: FORCES F, AND F2, F, = F2 = F SHOW: My, OF F2 = My, OF E,

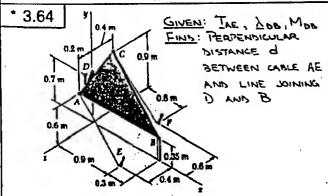
ĮŽ,

Now, by DEFINITION... $M_{\underline{\lambda}_1} = \underline{\lambda}_1 \cdot (\underline{c} \times \underline{F}_2)$ $= \underline{\lambda}_1 \cdot (\underline{c} \times \underline{\lambda}_2)F$

AND $M_{\overline{\lambda}^2} = \overline{\lambda}^2 \cdot (-\overline{c} * \overline{k}') + \overline{\lambda}^2 \cdot (-\overline{c} * \overline{k}')$

Using Ea. (3.39) No. (- [x /21) = /1. (- x /21) M2 = 7. (2 = 72) F TAHT CE

.. My. - Myz



FROM THE SOLUTION TO PRUBLEM 3.55 .. TAE = 55 N, TAE = 5[(9 N): - (L N) + (2 N) +] $M^{DS_{z}} = 5.58 \text{ M·m}$ $\overline{7}^{DB} = \frac{5.2}{2} (547 - 37)$ BASES ON THE DISCUSSION OF SEC. 3.11, IT (CONTINUES)

CONTINUED 3.64

FOLLOWS THAT ONLY THE PERPENDICULAR COMPONENT OF THE WILL CONTRIBUTE TO THE MOMENT OF THE ABOUT LINE DB. NOW (TAE) PARALLEL = TAE . 100 = 5(91-61+2k). 25 (241-71)

= = [(9)(24) + (-6)(-7)]

ALSO. THE = (THE) PARALLEL + (THE) PERP. SO THAT (THE) PERP. = V(55)2-(SIL)2 = 19.0379 N

SINCE LOB AND (TAE) PERP. ARE PERPENDICULAR. IT FOLLOWS THAT

MDB = d(TAE) PERP. 02 2.28 N·m = d · 19.0379 N

OR d=0.1198 m

ALTERNATIVE SOLUTION

LET THE PERPENDICULAR LINE, DRAWN FROM LINE \overline{DB} to the line of action of \overline{L}_{AE} . BE REPRESENTED BY

X,4,2 111 m d = xi + 4j + 2k Now .. d I The = d. The = D OR (xi- 7j+2k). 5(9j- 6j+2k)=0

OR 9X-64+23+0 可丁ダPB → 可·ブPB * Ó

OR (xi=4j=2k). 28 (24j-7j)=0 OR 24x-74=0 => 4= 34x (5)

9x-6(34x)+22=0 +> 2= 81x (3)

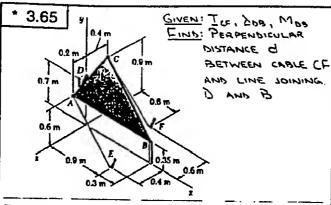
NOW .. Mos = 100 · (dx TAE) 0 = = = (484-632+14x+1442) = = (ABY + 14x + BI 2)

SUBSTITUTING FOR MOB AND USING EQS (2)

AND (3) YIELDS .. 2.28 = \$[48(24x)+14x+81(14x)] OR X= 0.017 614 M (2) => 4=0.060391 m AND THEN

FINALLY, d= 1x2+42+22 =[(0,017614)2+(0,060391)2+(0,101909)2]2 OR" d=01198 m

(3) => 2.0.101909 W



FROM THE SOLUTION TO PROBLEM 356. Ter = 33 N Ter = 3[(LN): - (9N); - (2N)]. IMOBI= 9.50 N·m 208 = = 25 (241-71)

BASED ON THE DISCUSSION OF SEC. 3.11, IT FULLOWS THAT DALY THE PERPENDICULAR COMPONENT OF ICE WILL CONTRIBUTE TO THE MOMENT OF ICE ABOUT LINE DB. NOW. (ICE) PARALLEL = ICE · Y DB

= 3 (6 1 -9 1 - 2 k) - 25 (24 1 - 7)) = == [(-7)(-7)] = 24.84 N

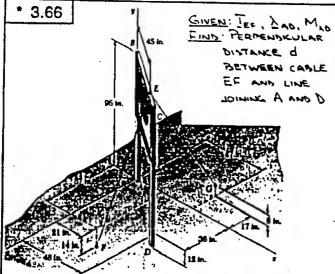
ALSO. ICF = (ICF) PARALLEL - (ICF) DERP. SO THAT (TLE) PERP = 1(33)2-(24.84)2

= 21.725 N

SINCE LOB AND (TCF) PERP. ARE PERPENDICULAR. IT FULLOWS THAT

IMDBI = d(TCF) PERP 9.50 N·m = d + 21.725 N

OR d = 0437 m FOR A SECOND METHOD OF SOLUTION, SEE THE SOLUTION TO PROPLEM 3.64.



FROM THE SOLUTION TO PROSLEM 3.57 .. TEE = 46 16 TEE = 2[-(316)i - (2216)j + (616)&] (CONTINUES)

3.66 CONTINUED

MAD = 1359 16.14. ZAD = (2-(4)-1-3+3k)

BASED ON THE BISCUSSION OF SEC. 3.11, IT FOLLOWS THAT ONLY THE PERPENDICULAR COMPONENT OF TEE WILL CONTRIBUTE TO THE MOMENT OF IEE ABOUT LINE AB. NOW (LEE) BURNTIET = IEC. JUD

= 2(-31-221-62). 126(41-143) = (26/(-3)(4)+(-22)(-1)-(6)(3)]

= 10.9825 1b

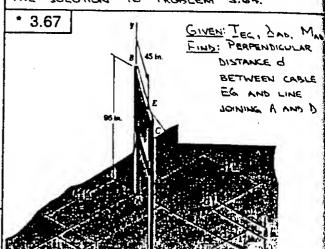
ALSO. TEC = (TEF) PARALLEL + (TEC) PERP. 50 THAT (TEF) PERR = V(46)2-(10.9825)2

= 44, 470 16

SINCE LAD AND (TEF) PERP. ARE PERPENDICUL IT FOLLOWS THAT

MAN = d(TEF) PERP. 1359 16.1N. = d. 44.670 16

OR "0 = 304 IN FOR A SECOND METHOD OF SOLUTION, SEE THE SOLUTION TO PROBLEM 3.64.

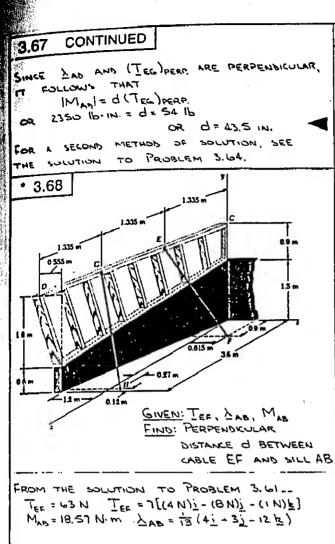


FROM THE SOLUTION TO PROBLEM 3.58' .. TEG = 54 16 TEG = 6[(1 16)2-(8 16);-(4 16)] IMAN = 2350 16. IN. \(\frac{1}{126}(4i-j-3k)\)

BASED ON THE BISCUSSION, OF SEC. 3.11, IT follows that only the perpendicular COMPONENT OF TEG WILL CONTRIBUTE TO THE MOMENT OF TEC ABOUT LINE AD. NOW (TEG) PARALLEL = TEG . LAD

= 6(1-81-4 k). (21(41-1-3k) = (2[(1)(4)+(-8)(-1)+(-4)(3)]

THUS, (TELL) PERP. = TELL = 54 16 (CONTINUED)



BASED ON THE DISCUSSION OF SEC. 3.11, IT FOLLOWS THAT ONLY THE PERPENDICULAR COMPONENT OF TER WILL CONTRIBUTE TO THE MOMENT OF $T_{\sf EF}$ ABOUT SILL ${\sf AB}.$ Now.. (TEF) PARALLEL = JEF · ZAB

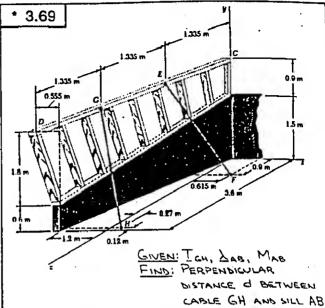
=7(41-B1-E)-13(41+31-12E) $= \frac{1}{3} (4)(4) + (-8)(3) + (-1)(-12)$ = 2.1538 N

ALSO. TEE = (TEE) PARALLEL + (TEE) PERR SO THAT (TEF) PERO = (63)2-(2.1538)2

= 62,963 N SINCE JAB AND (TEF) PERP ARE DERIENDICULAR, IT FOLLOWS THAT

MAD = d(TEF) PERP. OR 18.57 N.m. d. 62.963 N

OR d=0.295 m FOR A SECOND METHOD OF SOLUTION, SEE THE SULUTION TO PRUBLEM 3.64.



FROM THE SOLUTION TO PROBLEM 3.62 .. TGH = 75 N TGH = 3[(12 N) 1- (20 N) 1+ (9 N)]

BASED ON THE DISCUSSION OF SEC. 3.11, IT FOLLOWS THAT ONLY THE PERPENDICULAR COMPONENT OF IGH WILL CONTRIBUTE TO THE MOMENT OF IGH ABOUT SILL AB. NOW .. (TGH) PARALLEL = IGH . LAB

= 3(121-201491)-13(41+31-121) = = = (12/4)+(-20/3)+(P)(-12)] = - 27. L92 N

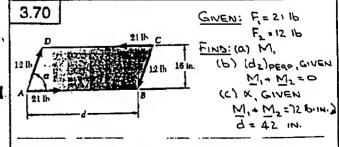
ALSO. TGH = (TGH) PARALLEL + (TGH) PERP. SO THAT .. (TGH) DERP. = V(75)2- (-27.692)2

= 49.700 N SINCE LAB AND (TGH) PERP. ARE PERPENDICULAR, IT FOLLOWS THAT

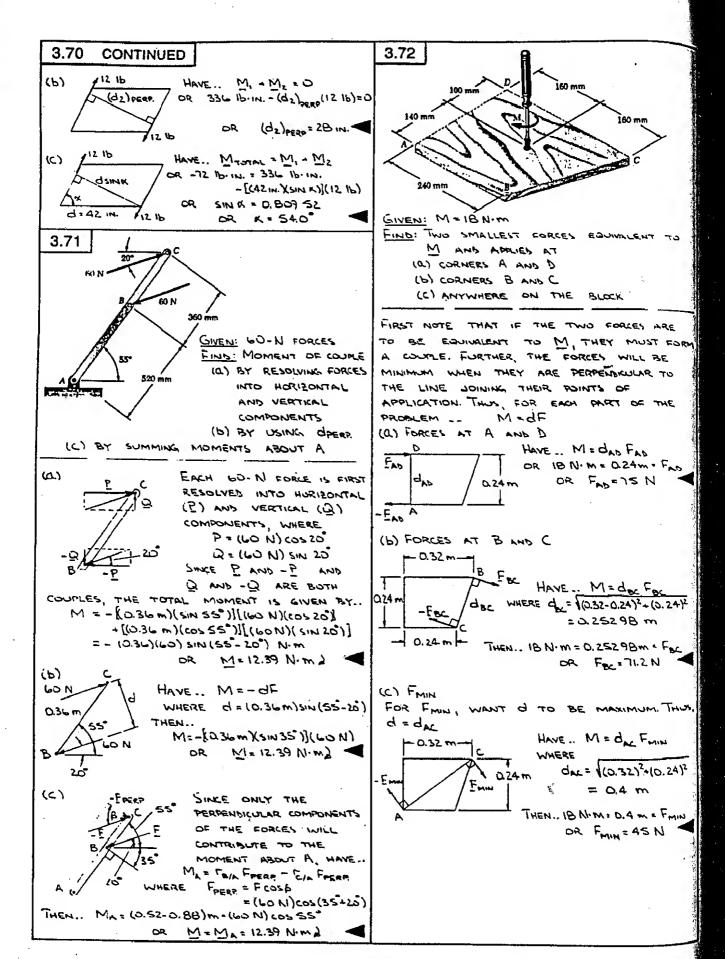
MAB = d(TGH) DERD. 44.1 N·m - d. 69.700 N

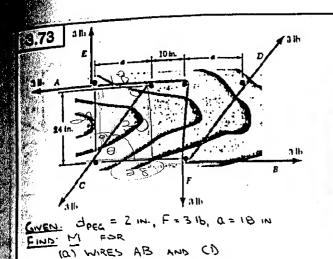
OR d=0,633 m

FOR A SECOND METHOS OF SOLUTION, SEE THE SOLUTION TO PROBLEM 3.64.



M = d, F, (a) HAVE WHERE d, = 16 IN. = (16 m.XZ1 16) M, = 336 16.14.) (CONTINUED)





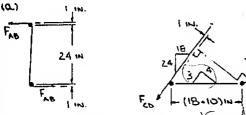
(b) WIRE'S AB, (1), AND EF

JN GENERAL, M = ZdF , WHERE d IS

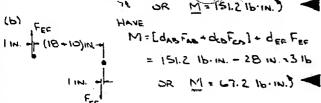
THE PERPENDICULAR DISTANCE BETWEEN THE

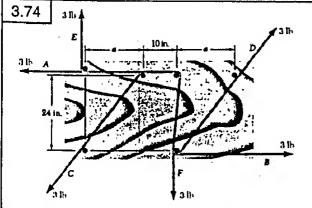
LINE'S OF ACTION OF THE TWO FORCE'S

ACTING ON A GIVEN WIRE.



HAVE.. M = das Fac + dco Fco (2+19/228))nv. = 316 = (2+24)nv. = 316 + (2+19/228))nv. = 316 > OR M=151.216.1N.)





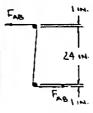
GIVEN: OPEC = 2 m., FAB = FOD = 3 lb.
M = 159.6 lb.m.

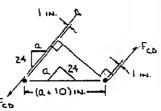
FIND: amin

HAVE.. M = dABFAB + dcoFco (CONTINUED)

3.74 CONTINUED

WHERE das and do are the perfudicular bistance's between the line's of action of the forces action on wires AB and CD, respectively.



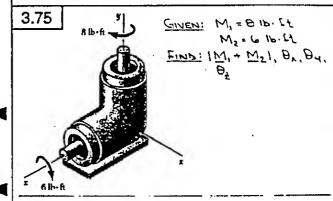


THEN. 159.6 (b. IN. = (2+24) IN. = 3 16 + $\left[2 + \frac{24}{124^2 + \Omega^2} (0 + 10)\right] IN. = 3 16$

OR (25.2)2(576+02) = (576)(0+10)2 OR 59.0402-11 5200+308183=0

OR a = 11 520 = V(-11 520)2-4(59.04)(308 183)

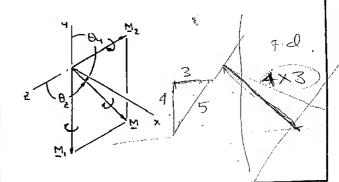
SOLVING YIELDS. Q=32.0 IN. Q=163.1 IN. TAKING THE SMALLER ROST. Q=32.0 IN.

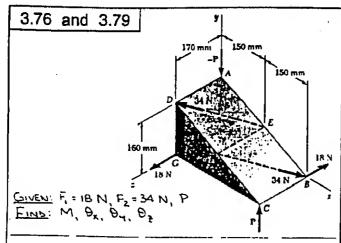


HAVE - M = M1 = M2 = - (B 16. ft) = (6 16. ft) k

THEN .. M = \((0)^2 + (-8)^2 + (-6)^2\)
OR M = 10 16 ft

AND $\cos \theta_{x} = 0$ $\cos \theta_{y} = -\frac{\theta}{10}$ $\cos \theta_{z} = -\frac{b}{10}$ or $\theta_{x} = 90$ $\theta_{y} = 1431$ $\theta_{z} = 126.9$





HAVE. $M = M_1 - M_2 - M_3$ WHERE $M_1 = \Gamma_{C/G} \times F_1 = (0.3 \, \text{m})_2 \times F(18 \, \text{N}) \times F(18$

 $\frac{3.76}{9.7} P=0 : M = M_1 + M_2$ $0R M = (5.4j) + \sqrt{2}(1.36j + 2.55j)$ = (1.92333 N - m)j + (9.0062 N - m)j 0R M = 9.2093 N - m 0R M = 9.21 N - m 0R M = 9.21 N - m $M = \frac{M}{2} = 0.208 BSj + 0.9799Sj$

THEN.. (050, 0.208 B5 (050, = 09)795 (060, 0) = 0 THAT Bx - 77.9 By = 12.05 B2 = 90

3.19 P=20N : M=M,+M2+M3

OR M=(1.92333;+9.0062j)+20(-0.17:+0.3 E)

=-(1.47667 N·m);+(9.0062 N·m);+(6.4m)E

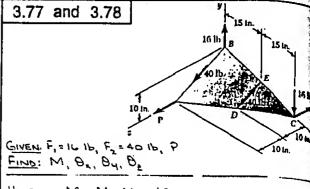
THEN .. M= (-1.47667)2+(9.0062)2+(6)2 = 10.9221 N·m

OR M=10.92 N·m

AND MANS = M = -0.1352001+0.82459j+0.54934E

THEN...

COS $\theta_{x} = -0.135200$ COS $\theta_{y} = 0.82459$ COS $\theta_{z} = 0.135200$ COS $\theta_{y} = 0.82459$ COS $\theta_{z} = 0.135200$ COS $\theta_{y} = 0.8459$ COS $\theta_{z} = 0.135200$ COS $\theta_{y} = 0.8459$ COS $\theta_{z} = 0.135200$ C



HAVE .. $M = M_1 + M_2 - M_3$ WHERE $M_1 = \Gamma_C \times \Gamma_1 = (30 \text{ m.}) \cdot \times [-(16 \text{ lb}) \cdot j]$ $= -(480 \text{ lb·m.}) \cdot \Sigma$ $M_2 = \Gamma_{ElB} \times \Gamma_2$ WHERE $\Gamma_{ElB} = (15 \text{ m.}) \cdot (-(5 \text{ m.}) \cdot j)$ AND $C_{DE} = \sqrt{(5)^2 + (5)^2 + (-10)^2} = 5(5 \text{ m.})$ THEN .. $\Gamma_2 = \frac{40 \text{ lb}}{5(5)} (5 \cdot j - 10 \cdot \Sigma)$ $= 8(5 \cdot [(1 \text{ lb}) \cdot j - m(2 \text{ lb}) \cdot \Sigma)$ SO THAT $M_2 = 8(5 \cdot [3 - 5 \cdot 0] \cdot j - 3$

$$= (30b)^{\frac{7}{2}} \qquad (1p \cdot m)$$

$$= (30b)^{\frac{7}{2}} \qquad (1p \cdot m)^{\frac{7}{2}} \times (-b)^{\frac{7}{2}}$$

= 845 [(10 lb.m) + (30 lb.m) + (15 lb.

3.77 P=0 : M= M, 1 M, OR M=-(480) =+ B(\$(101+301-15 =) = (178.885 16.11.) + (536.66 16.11) -- (211.67 16.11.) \]

THEN. M = V(178.BBS)2+(536.66)2+(-211.67)2
= 603.99 16.10.

AND DANG = M = 0.296 171 + 0.888 521 - 0.350 45 5
THEN.

COS Bx = 0.296 17 COSBy = 0.888 52 COSB2 = 0.3504

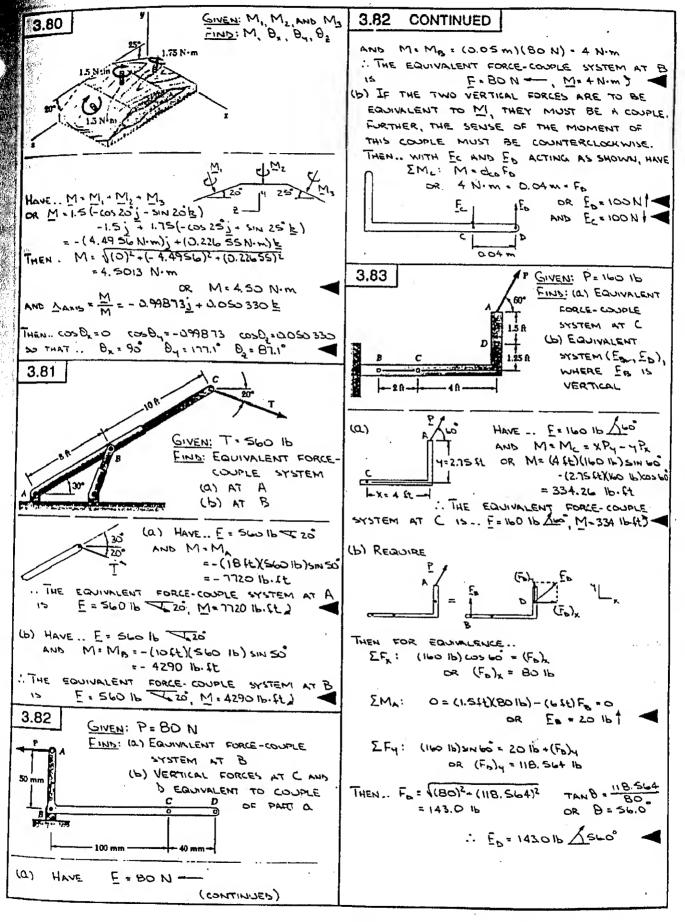
3.78 P=20 Ib :: M = M,+ M2 + M3

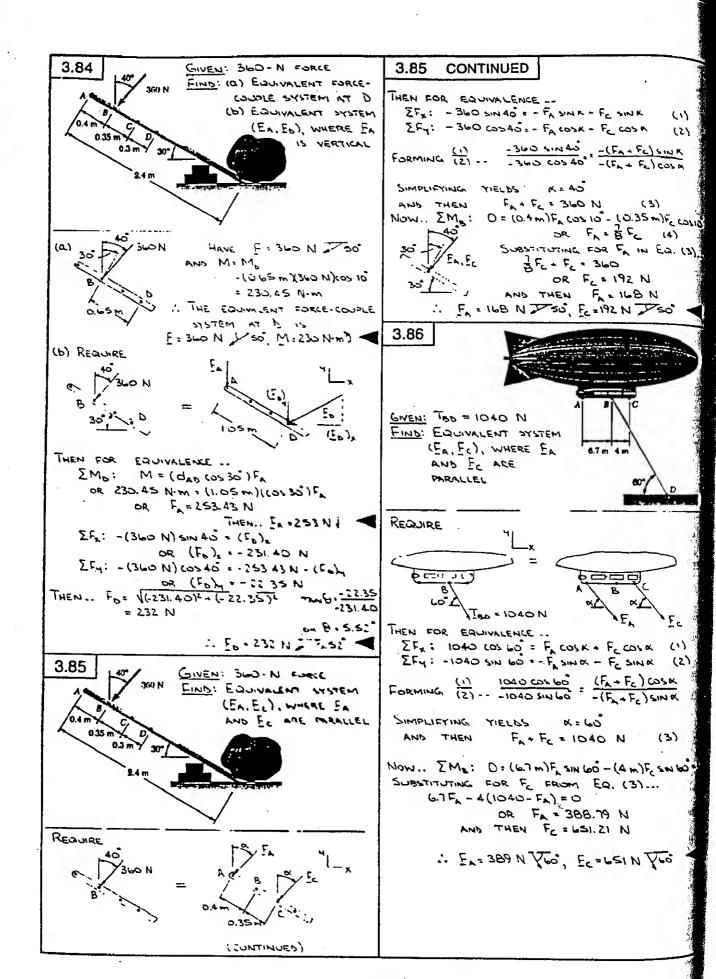
OR M = - (480) \(\frac{1}{2} + 8 \) \(\frac{10}{2} + \) \(\frac{1}{2} + \) \(\frac{1}{2}

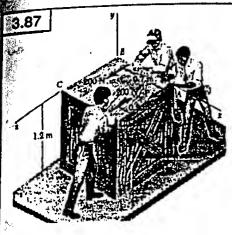
THEN .. M = \(\((178.885)^2 + (1136.66)^2 + (-211.67)^2\)
= 1169.96 16.10.

OR M = 1170 lb.m.
AND \(\frac{\text{Anis}}{M} = 0.152 \text{ 898} \frac{1}{2} + 0.971 \text{ 54} \frac{1}{2} - 0.180 921 \frac{1}{2} \]

THEN ... COSBX = 0.152 BAB COSBY = 0.971 SA COSB2 = -0.18012







GIVEN: 1-1-1.2-M CRATE

FIND: (a) Equivalent force couple system

AT A IF P= 240 N

(b) SINGLE EQUIVALENT FORCE AND

POINT OF APPLICATION ON SIDE AB

(c) P IF THREE FORCES ARE

EQUIVALENT TO A SINGLE FORCE AT B

(a) Since the two 200-N forces form a couple. The three forces are equivalent to a force E and a couple vector M, where E = (240 N) E

AND $M = (0.7-0.2)m \times 200 N = 100 N·m$ THE EQUIVALENT FORCE-COUPLE SYSTEM AT

A 'S--E = (240 N)E, M = (00 N·m)

(b) THE SINGLE EQUIVALENT FORCE F' IS EQUAL TO (240 N) & AND IS APPLIED ALLOW AB

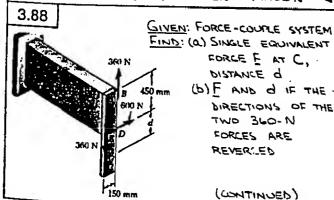
SO THAT ITS MOMENT ABOUT A IS

EQUAL TO MI. THUS:

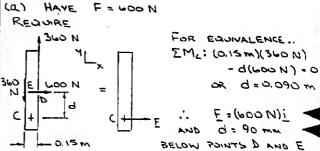
B = GF' C = GF'

(C) FOR THIS CASE, d: 1 m. THEN.

OR 100 N·m = (1 m)P OR P=100 N







(b) THE DALY EFFECT OF REVERSING THE DIRECTIONS OF THE TWO 360-N FORCES WILL BE TO CHANGE THE SENSE OF THE MOMENT OF THE COUPLE. THUS

F=(600 N);

AND EMC: - (0.15m)(360 N) - d(600 N) = 0

OR d=-0.090 m

... d=90 mm ABOVE POINTS D AND E

3.89

GIVEN: FORCE-COUPLE

SYSTEM

FIND: (a) EQUIVALENT

FORCE-COUPLE

SYSTEM AT B

SO SINIII

(b) SINGLE

EQUIVALENT

FORCE, POINT

OF APPLICATION

(a) FIRST NOTE THAT THE TWO 20-16 FORCES

FORM A COUPLE. THEN $F = 48 \text{ lb } \Delta \theta$ WHERE $\theta = 180 - (60 + 55)$

AND M = IMB = (30 m. X48 lb) cos 55 - (70 m.)(20 lb) cos 20 = - 489. LZ lb. m.

THE EQUIVALENT FORCE-COUPLE SYSTEM AT B

(b) THE SINGLE EQUIVALENT FORCE E IS EQUAL TO E. FURTHER, SINCE THE SENSE OF M IS CLOCKWINE, E MUST BE APPLIED BETWEEN A AND B. FOR EQUIVALENCE...

EMB! M = - OF cos ss'

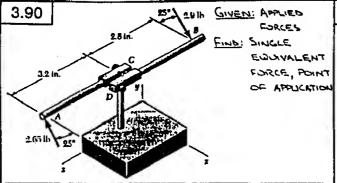
WHERE Q IS THE DISTANCE FROM B TO THE

POINT OF APPLICATION OF E'. THEN...

- 489.62 16.10 = - Q (48 16) COS SS"

OR Q = 17.78 16.

AND IS APPLIED TO THE LEVER 17.78 IN. TO THE LEFT OF PIN B



FIRST TRANSFER THE 2.65-16 FORCE AT A TO B. THE RESULTING FORCE-COUNTE SYSTEM (F,M) AT B 15 THEN --

F = (2.9-2.65)1b = 0.251b

AND M=MB=(6m.X2.6516)x0525

THE SINGLE EQUIVALENT FORCE F' IS EQUAL TO F. FURTHER, FUR EQUIVALENCE

 ΣM_B : $M = QF' \cos 25^\circ$ WHERE Q is the distance from B to the POINT OF APPLICATION OF F'. SINCE M ACTS IN THE -1 DIRECTION, E' WOULD HAVE TO BE APPLIED TO THE RIGHT OF B. THEN..

- 14.4103 lb·10. =- α (0.25 lb) cos 25° or α = 636 in.

.. $E' = (0.25 \text{ lb})(\cos 25) + \sin 25 \text{ b})$ AND IS APPLIED ON AN EXTENSION OF HANDLE BD AT A DISTANCE OF 63.6 IN. TO THE RIGHT OF B.

3.91

GIVEN: FORCE- COUPLE

SYSTEM

AN FIND: (a) Magnitude of

SINGLE FIDUVALENT

FORCE F' AND ITS LINE

OF ACTION FOR A: 40

(b) & IF LINE OF

ACTION OF F'

INTERSECTS CD

300 mm TO THE

RIGHT OF D

(a) The given force. Counce system (E,M) at B is E = 48 N and $M = \Sigma M_B$ $= (0.4 \text{ m})(15 \text{ N})\cos + (0.24 \text{ m})(15 \text{ N})\sin 40$ or $M = 6.9103 \text{ N} \cdot \text{m}$

THE SINCLE EQUIVALENT FORCE E' IS EQUAL TO E. FURTHER FOR EQUIVAL FACE...

3.91 CONTINUED

Single

(b) Following the solution to PART Q By EQUIVALENT

INITH $d = 0.1 \, \text{m}$ AND α UNKNOWN, HAVE FORCE, POINT $\sum M_B : (0.4 \, \text{m})(15 \, \text{N}) \cos \alpha + (0.24 \, \text{m})(15 \, \text{N}) \sin \alpha$ of APPLICATION $= (0.1 \, \text{m})(48 \, \text{N})$

OR $5 \cos x + 3 \sin x = 4$ REARRANGING AND SOLDARING... $25 \cos^2 x = (4 - 3 \sin x)^2$ Using $\cos^2 x = 1 - \sin^2 x$ AND Expanding... $25 (1 - \sin^2 x) = 16 - 24 \sin x + 9 \sin^2 x$ OR $34 \sin^2 x - 24 \sin x - 9 = 0$

THEN SINK = 24 = V(-24)2-4(34)(-9)

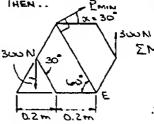
OR SINK = 0.976 86 SINK = - 0.270 98
OR R = 77.7° Q = -15.72°

3.92

CINEN: FORCE-COUPLE
SYSTEM (P.M)

DEQUIVALENT TO
A SINGLE FORCE
AT E

FROM THE STATEMENT OF THE PROBLEM, IT FOLLOWS THAT $\sum_{E=0}^{\infty} \sum_{E=0}^{\infty} \sum_$



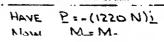
WN EME: (0.2 sin30+0.2)m·300 +(0.2 m)sin 30 · 300 -(0.4 m)Pmin = 0 OR Pmin = 300 N △20 ∴ Pmin = 300 N △20

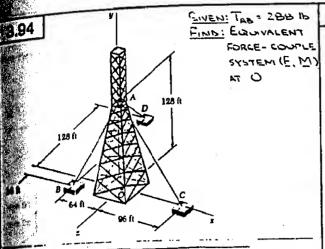
GIVEN: P= 1220 N

FIND: EQUIVALENT FOR

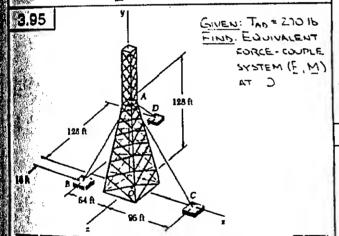
COUPLE SYSTEM

(E,M) AT G





HAVE.. $CAB = \sqrt{(-64)^2 + (-128)^2 + (16)^2} = 144 \text{ ft}$ THEN $T_{AB} = \frac{288 \text{ lb}}{144} (-64\underline{i} - 128\underline{j} + 16\underline{k})$ $= (32 \text{ lb})(-4\underline{i} - 8\underline{j} + \underline{k})$ $= (400 \text{ lb} \cdot 12\underline{j} + (16,384 \text{ lb} \cdot 12\underline{k})$ THE EDAVALENT FORCE-COUPLE SYNTEM AT $= -(128 \text{ lb})\underline{i} - (256 \text{ lb})\underline{j} + (32 \text{ lb})\underline{k}$ $= (4.10 \text{ kgp} \cdot 12\underline{j} + (16,38 \text{ kp} \cdot 12\underline{k})$



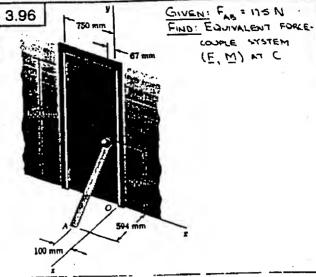
MAVE .. day = 1(-64)2+(-128)2+(-128)2 = 192 Et

THEN.. IAD = 192 (- LA ! - 129] - 128 E)

=-(23,040 10.ft)i+(11,520 16.ft)E = 12Bj + 90(-i-2j-2k) = 12Bj + 90(-i-2j-2k)

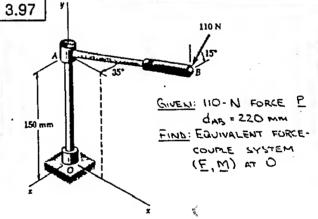
THE EDUIVALENT FORCE-COUPLE SYSTEM AT

O 15 .. $E = -(90 \text{ lb})\underline{i} - (180 \text{ lb})\underline{j} - (180 \text{ lb})\underline{k}$ $M = -(230 \text{ kp}, (4)\underline{i} + (11.52 \text{ kp}, 4)\underline{k})$



= 5/[(-0860X-18)]i + [-(0.683X-18)]i . [(0.683)(30)-(-0.860)(1)] !:] = (774 N·m)i+(6647 N·m)i+(10675 N·m)!: :. THE EQUIVALENT FORCE-COUPLE SYSTEM AT (

THE EQUIVALENT FORE-COUPLE SYSTEM AT C 15. F. (SN) - (150 N) - (90 N) E M = (77.4 N-m) + (61.5 N-m) + (106.8 N-m) E



HAVE .. P = (110 N)(- SW 152+ COS 15 k)

NOW .. M = Mo = TBO = P

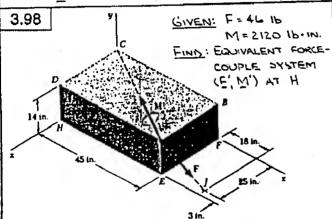
WHERE TBO = (0.22 m)CDS 352 + (0.15 m)

- (0.22 m) SIN 35 k

THEN .. M = 110 0.22 COS 35 0.15 - 0.22 SIN 35

3.97 CONTINUED

M = 110{[0.15](0515")-(-0.22 m 25")(-11015")} +[-(022 cos35°)(cos 15°)]} +[(0.22 cos 35)(-sin 15) 12] = (12.345 Nom) = (19.148 Nom) = (5.131 Nom) 1 THE EDUNALENT FORCE-COUPLE SYSTEM AT E = (110 N) (- SIN 15, 7 + cos 12, B) = - (28.5 N) 1- (106.3 N) E M= (12.35 N·m)i - (19.15 N·m)j-(5.13 N·m)E



HAVE -- da= (18)2+(-14)2+(-3)2= 23 in.

THEN. F = \frac{46 1b}{23} \left(18\frac{1}{2} - 14\frac{1}{2} - 3\frac{1}{2} \right) \frac{1}{2} - (6 1b) \frac{1}{2} - (6 1b) \frac{1}{2}

ALSO. dec = V(-45)2+(0)2+(-28)2 =53 IN.

M = 2120 16.14 (-45: -28 E)

=-(1800 lb.in.) - (1120 lb.in.) k

NOW. M' = M + TAIN * F WHERE TAIN = (45 IN.) 1 + (14 IN) 1

THEN. M'=(-1800)-1120 b) + 45 14 0

= (-1800)-1120 1)+1[(14)(-6)]= + [-(45)(-6)]j

+[(45)(-2B)-(14)(36)]E

= (-1800 - 84)i + (270)j

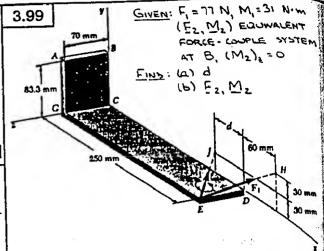
+ (-1120-1764) E =-(1884 16.14) + (270 16-14) 1

-(2884 Ib·IN) <u>k</u>

=-(157 16.52)=+(22.5 16.52)j

- (240 16.4t)E

.. THE EQUIVALENT FURCE- COUNTE SYSTEM AT F' = (36 16) 1 - (28 16) 1 - (6 16) 1 M=-(157 16. ft) i+(22.5 Tb.ft) j-(240 16.6t) !



HAYE .. den = V(60)2+(60)2+(-70)2 = 110 mm

F. = \frac{110}{110} (60\frac{1}{2} + 60\frac{1}{2} - 70\frac{1}{2})
= (42 N)\frac{1}{2} - (42 N)\frac{1}{2} - (49 N)\frac{1}{2}

ALSO. des = \((-d)2+(30)2+(-70)2 mm

M' = GE7 [-(9)] + (30 mm)]-(10 mm)]

(a) HAVE. $M_2 = M_1 + C_{WB} \times F_1$ (1) WHERE $C_{WB} = (0.31 \text{ m})1 - (0.0233 \text{ m})2$

0.31 -0.0233 THEN . . CHB + F. = - 49

= [(-0.0233)(-49)] i +[-(031)(-49)]j +[(0.31)(42)-(-0.0233)(42)] =

= (1.1417 N·m) + (15.19 N·m) j +(13.99B6 Now) 12

EQ. (1) CAN THEN BE EXPRESSED AS (M₂)_x i + (M₂)_y i = 31 N·m [-(d)i + (30 mm) i (M₂)_x i + (M₂)_y i = 31 N·m [-(d)i + (30 mm) i -(10 mm/) []

> + (1.1417 N.m) + (15.19 N.m) + (13.9986 N.m) k]

EQUATING THE E COEFFICIENTS...

0 = 31 N·m (-70 mm) + 13.99BL N·m

THEN. des = (3) = (3) = (0) = (0) = (0) = (0) d=135.0 mm OR 0 = 135.018 mm

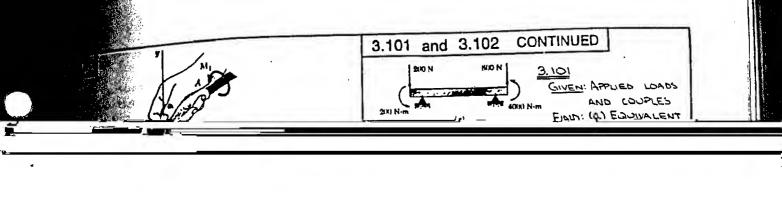
(b) First NOTE $d_{E,1} = \sqrt{(-135.018)^2 + (30)^2 + (-70)^8}$ 155,016 mm

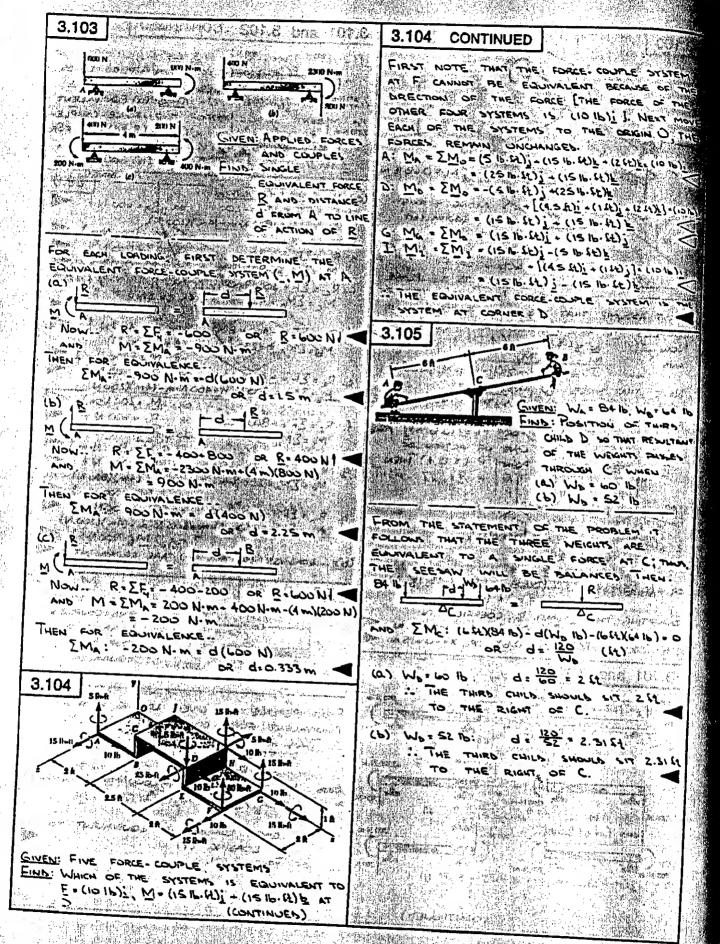
Using Eq. (2), M_2 is THEM... $M_2 = \left(-\frac{31 \times 135.018}{155.016} + 1.1417\right)_1$

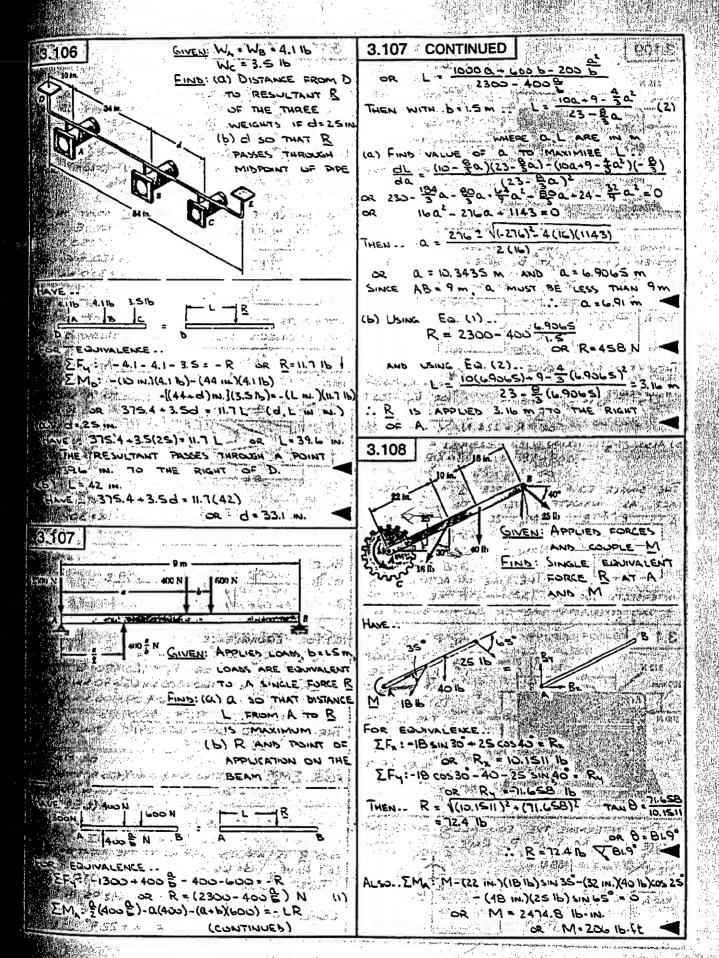
+ (31x 30 + 15A)j

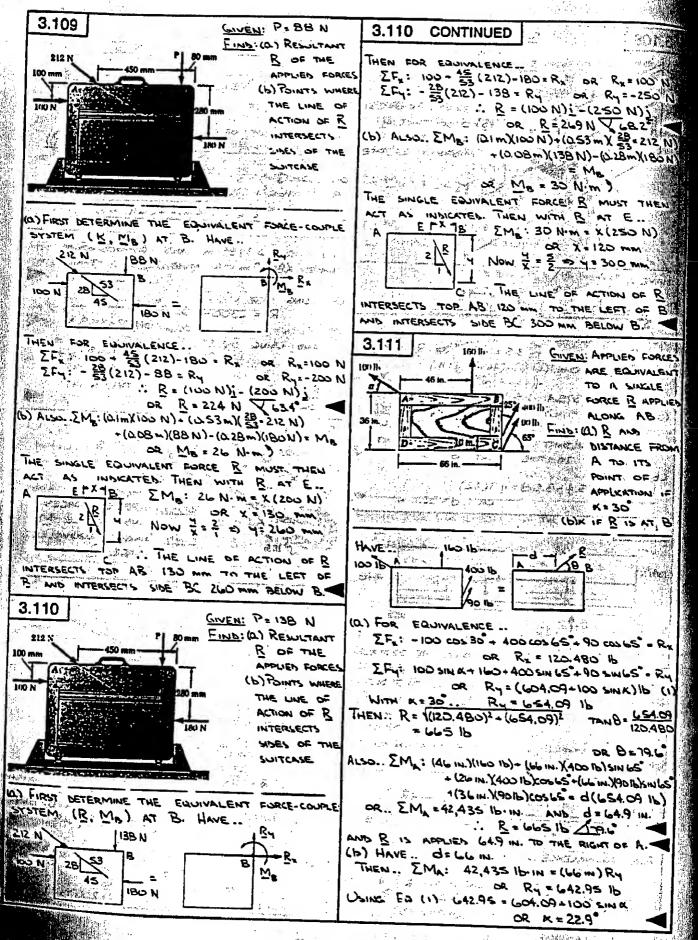
= -(25.859 N·W) + (21.189 N·m);

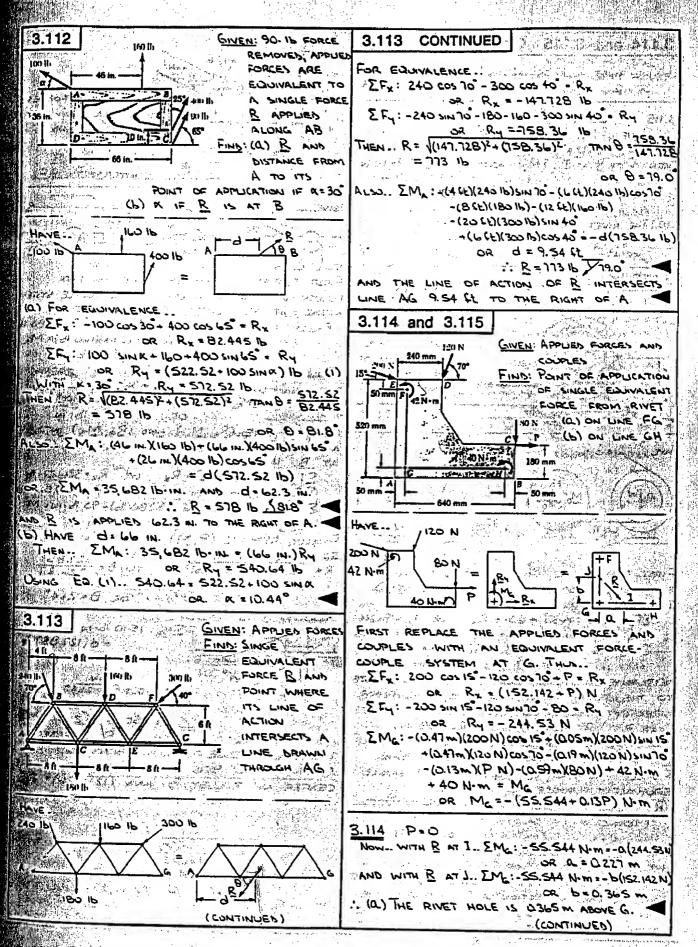
E, = (42 N) = + (42 N) = - (49 N) = M =- (25.9 N·m) =+ (21.2 N·m)

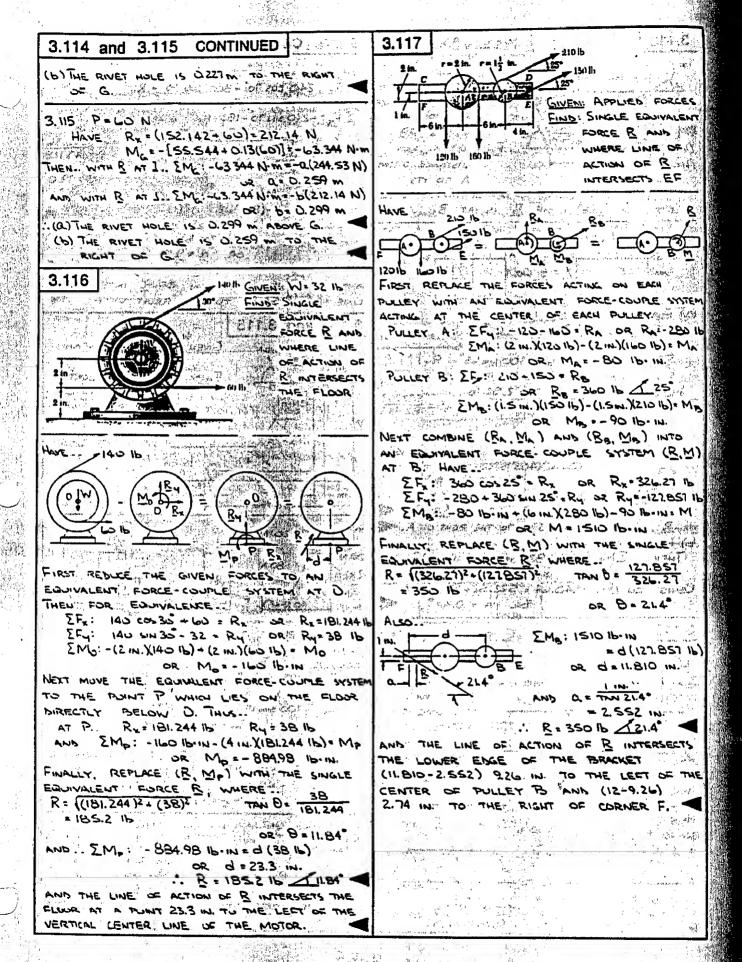


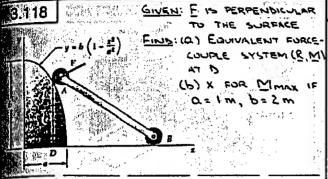












THE SLOPE AT ANY POINT ON THE SIRFACE OF MEMBER C 15 ..

SINCE E IS PERPENDICULAR TO THE CAPACE, IT FOLLOWS THAT

WHERE IN THE ANGLE THAT F FORMS MITH THE HORIZONTAL. THEN FOR EUNVALENCE

EE E R EMB COSK & M NCE A 15 A POINT ON THE GENE HAVE TO AT A



<u> 26x</u> (02)2+(2PX)2

 $M = [b(1 - \frac{x^2}{\Omega^2})] \cdot F \cdot -$



THE EQUIVALENT FORCE-COURLE SYSTEM R = F TAN' (CEX)

 $M = \frac{2EB^2(x - \frac{x^3}{4}z^2)}{\sqrt{0^4 + 4B^2x^2}}$

DESTITUTING Q=1 M, D= 2 M M THE EXPRESSION FOR MY YIELDS ..

(1+ 10 x2)

Se (1-3x2)(1+16x2) - 16x(x-x3) = 0

En. X2 = -3 = 1(3)2-4(32)(-1)

WHE POSITIVE ROUT SINCE X2 >0 ELDS X2 = 0.136011 M2

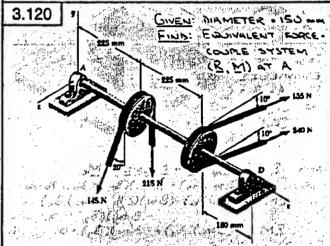
THEN FOR MMAX

x = 0.369 m

GIVEN: DIAMETER - 60 MM 3.119 APPLIED FORCES 20 mm S. J. 1996 S. FIND: EQUIVALENT FORCE-12 N COUPLE SYSTEM (R M) AT C FOR EQUIVALENCE EF: ER + FR + FR + Ec + Eb - - - 17 - 18 7 54 1960 1 - 16 E - 211 == (21 N);-(29 N); EM: M = CAK = EA

LOIC & FO DR M= (0.11m) - (0.03m) &] = [- (17 N)] + [(0.02m)i+(0.11m)j-(0.03m)]z]-[-(12N)j) + [(003m)i+(003m)j-(0.03m)k] = [-(21N)] i =- (0.51 N. m) + [- (0.24 N.m) 12 - (0.36 N.m) i] 1 +[(0.63 N-m)k+(0.63 N-m)]]

. THE ECHNICENT FORCE-COUPLE SYSTEM AT C 15 .. R = -(21N) - (29N) ; - (16N) = M +-(0.87 N-m) +(0.63 N-m) = (0.39 N-m)



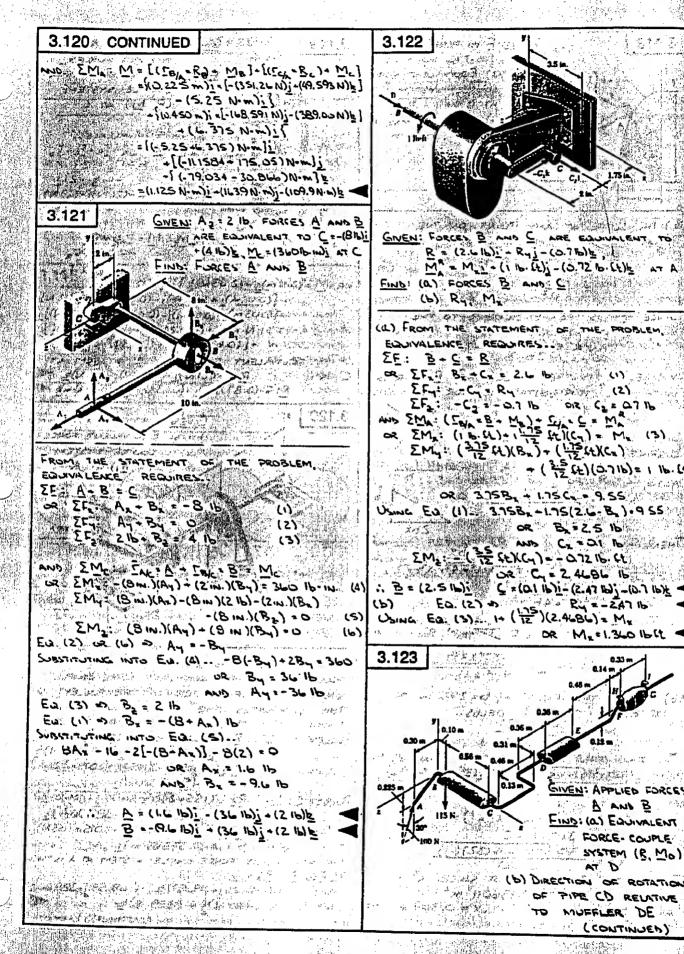
FIRST REPLICE THE BELT FORCES ON EACH PULLEY WITH AN EQUIVALENT FORCE COURLE SYSTEM AT THE CENTER OF THE PULLEY! THIS ELIMINATES THE NEED TO DETERMINE WHERE THE BELTS CONTACT THE PULLEYS PULLEY B: EE: RB = -2151+145(-cos20j-sin20) = -(351.26 N)j-(49.593 N)E EM : MB = [(0.075 m X 145 N) - (0.075 m)(215 N)] 14.2 H ADM = -(525 N·m); 1986 140 140

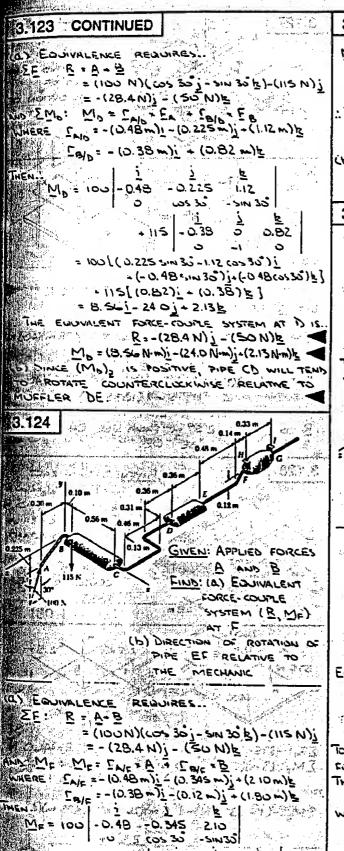
PULLEY C: EF: Rc = (155+240X-sin 10 j-cos 10 k) y(N 00.089) : (N 18284) = = -(L8.59) N) ~ [(O.075mX240N)-(0.075mX155N)]

= (6.375 N·m)i

THE EQUIVALENT FORCE-COURLE SYSTEM AT A 13 THEN EF: R = RB - Rc = (-35126j-49.593k)+(-68.591j-389.00k = - (420 N); - (339 N)E

(CONTINUED)





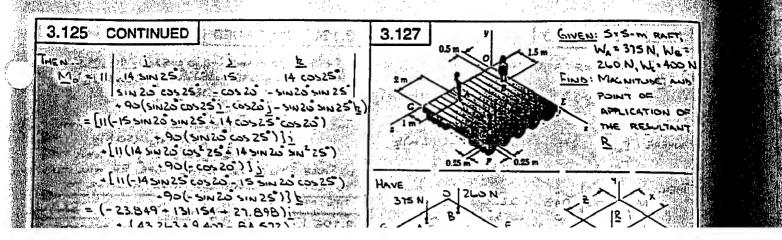
+ 115 -0.38 -0.12 1.80

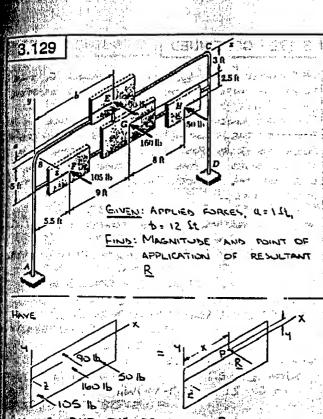
(CONTINUED)

3.124 CONTINUED M= = 100[(0.345 sin 36 - 2.10 cos 36) 1 1 (-0.48 cos 30) + (-0.48 cos 30) } +115[(1.80)i+(0.38) k] () = 42.41 - 24.01 - 2.13 \ To my in the state of its THE EDNUMLENT FURE-COUPLE SYSTEM AT F IS. R = - (28.4N) - (50N) E M== (42.4 N-m)-(24.0 N-m) + (2.13 N-W) (b) Since (ME) IS POSITIVE, DIPE EF WILL TEND TO ROTATE COUNTERCUCKWISE RELATIVE TO 在, 在, 是一种一种一种一种 THE MECHANIC. 3.125 GIVEN: APPLIED FORCE AND COUPLE FIND: ELANVALENT - WING FORCE- COUPLE " SYSTEM (R, M.) The Committee of the second of the second MYSTAN WALLERS . Miller E. Charles of the - 2006 Contract of X Complete Contract of the Contrac THE PROPERTY OF THE PARTY OF TH EQUIVALENCE REQUIRES... ZE: R.E. = (11 16)(sin 20 cos 25 i - cos 20 j = (341 16) = (10.34 16); - (1.590 16) E TO SIMPLIFY THE COMPUTATION OF MO SLIDE THEN.: M. = TB/O x Fc + Mc 179 H-140 77 [(III 5) + (15 III) = 12 4 (14 IN.) COS 25 L Me = (90 16.14.) (51420 cos 251 = cos20)

- SINZO SINZS" 12)

(CONTINUED)





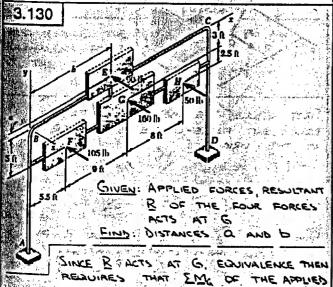
SOUME THAT THE RESULTANT R IS APPLIED AT SINT P. WHOSE COORDURTES ARE (1, 7,0). EDUIVALENCE THEN RESURES ... EF-105-90-160-50= R OR ER=405 Ib [41 001)(42 E)+(41 00)(421)-(41 201X)1 = (14)

(5.5 ft)(50 lb) = -4(40 s lb)

photocomes in in consist annihilation of the constant of = = 2.94 ft infiliation EMy: (5.5 ft)(105 115)+(12 St)(90 116)+(14.5 ft)(160 116)

+ (22.5 ft X50 lb) + x (405 lb) OR X = 12.65 \$t

R ACTS 12.60 St TO THE RIGHT OF MEMBER AB AND 2.94 ft BELOW MEMBER



(CONTINUED)

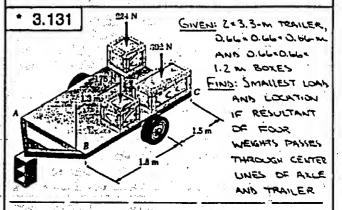
3.130 CONTINUED

是有一点的。2. 可以不够**是这**的证据。 1. 4

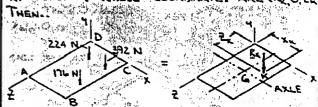
SYSTEM OF FORCES ILLSO BE ZERO. THEN. MT G: EMx : - (0+3) ff - (90 16) + (2 ff) (105 16) # (2.5 ft)(50 lb) • 0

DR Q = 0.722 St 6- 6- 5- 5- 14.5-B)42-(90 1b) (64th) (50 lb) = 0

OR 6=20.6 12 -



FIRST REPLACE THE THREE KNOWN LONDS WITH A SINGLE EQUIVALENT FORCE RK APPLIES AT POINT K WHISE COORDINATES ARE (X) 24) THEN.



EQUIVALENCE REQUIRES ..

ΣΕν:
«- 224-392-176:-Rκ οκ Rκ=792 Ν Ι EMx: (0.33 m)(224 N)+(06 m)(392 N)

or 2 = 2 = 08475 m

~ (0.33 m)(224 N) - (1.67 m)(392 N) - (1.67 m)(176 N) = - xx(792 N)

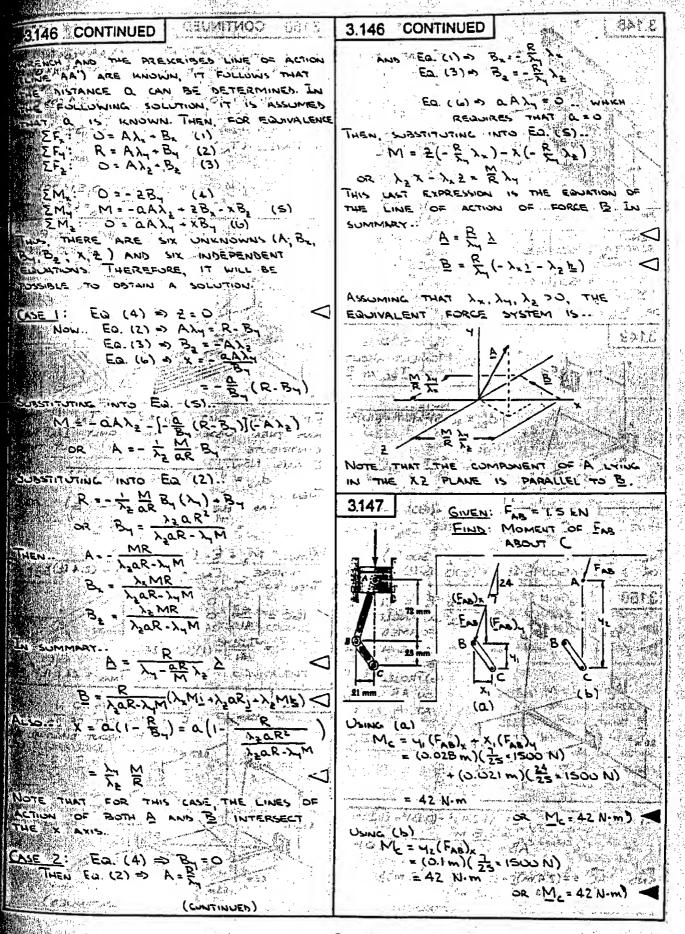
FROM THE STATEMENT OF THE PROBLEM IT IS MOWN THAT THE RECLIANT OF BK AND THE LIGHTEST LOAD WE PHOSES THROUGH G, THE POINT OF INTERSECTION OF THE TWO CENTER LINES. THUS, $\Sigma M_c = 0$ FURTHER, SINCE W_c is to be as small as

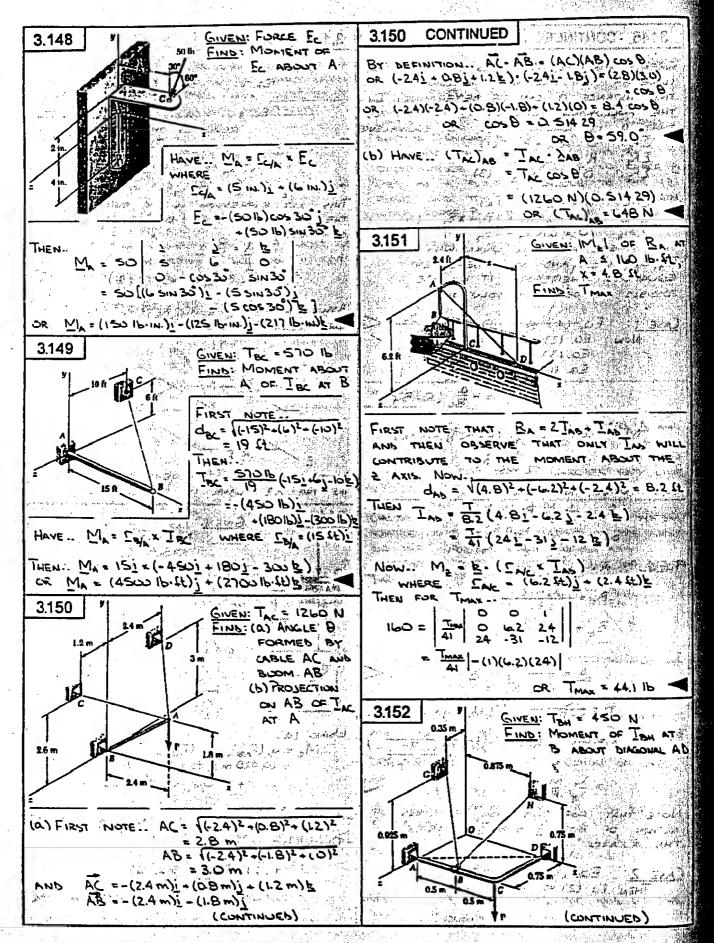
POSSIBLE, THE FOURTH BOX SHOULD BE PLACED AS FAR FROM G AS POSSIBLE. THESE TWO REQUIREMENTS WIMILY ...

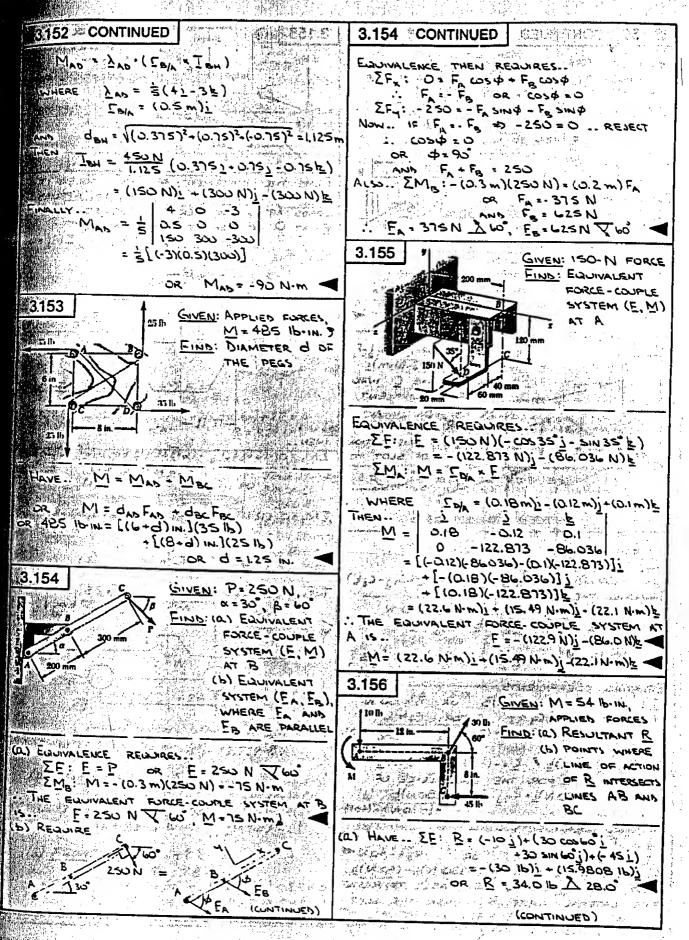
033m & X (& 1.0 m AND 1.5 m & 2 6 2.97 m WHERE "THE LOWER BOUND ON Y AND THE UPPER BUSHT THAT OF BECOMING 35A & NO THAT THE BOX DOES NOT OVERHANG THE TRAILER. SINCE THE BOX 15 TO BE AS FAR FROM G AS FOLLAGE CUNSIDER FIRST IF THESE BOUNDS ARE PHYSICALLY APOSUBLE.

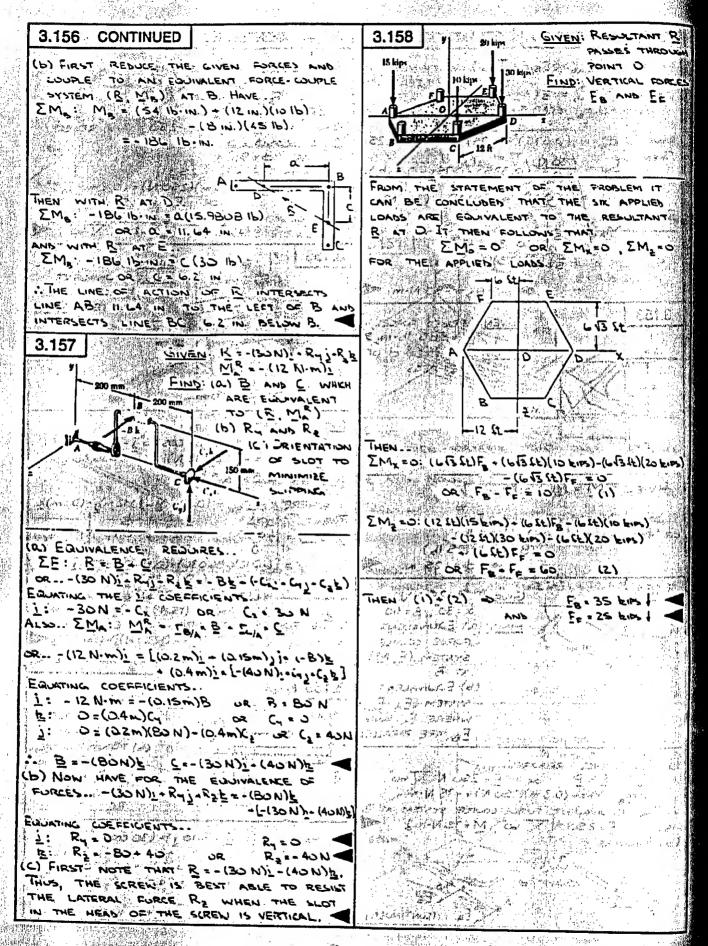
THE RELEASE OF THE PROPERTY OF A PROPERTY OF A

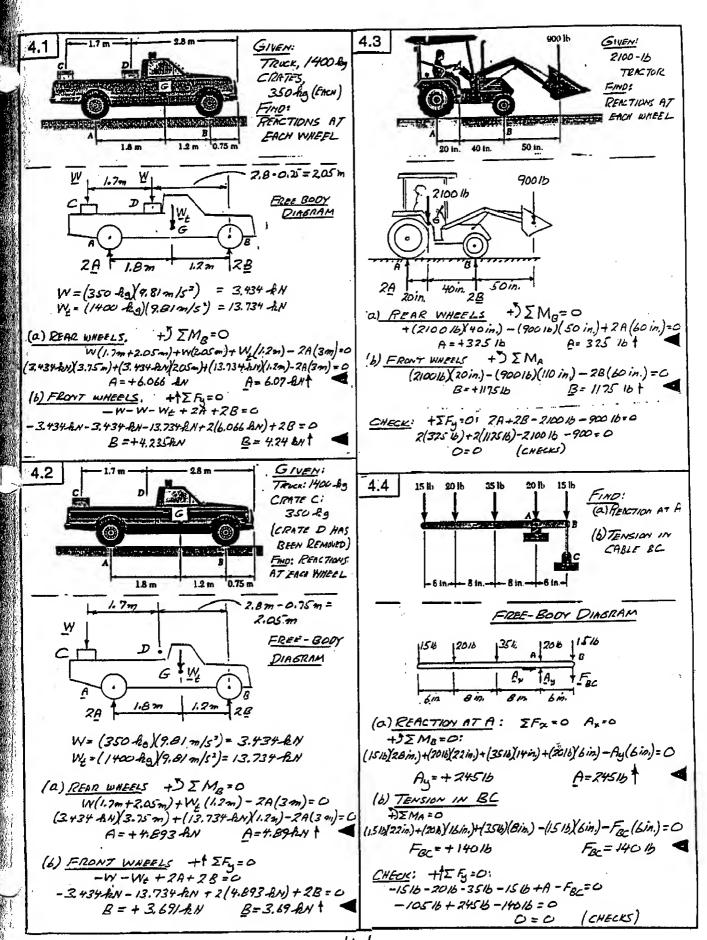
(CONTINUED)

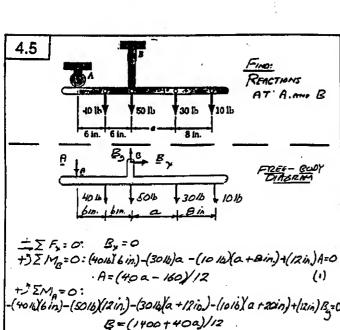












-{4016}6in}-(5016)(12in)-(3016)(a +12io)-(1016)(a +20in)+(12in)18,=0 R=(1400+40a)/12

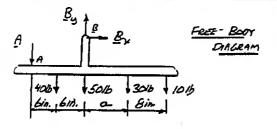
B=(1400+400)/12 SINCE BY=0, (2) (a) For a = 10in.

EQ11): A = (40x10-160)/12 = +2016 A=2010+ < B=15015 Ea.(2): B = (1400+40x10)/12 = +15016 (b) FOR a = 7in.

A= 1016+ Eq.(1): A = (4017-160)/12 = +1016 EQ(1): B = (1400+40×7)/12=+140 16 B=140169

4.6

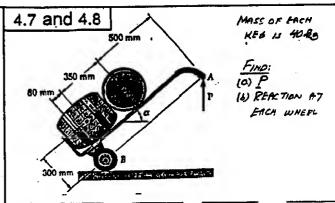
SIMPLIAST DISTANCE OL FOR NO MOTION 30 th ¥101b



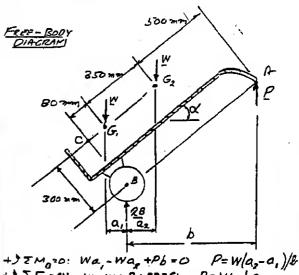
FOR NO MUTION REACTION AT A MIST BE DOWNWARD OR RERO SMALLEST DISTANCE a FOR NO MOTION CORRESPONDS TO ASO

+ DIMB=0 (4016)(6in.) - (3016)a - (1016)(a+&in)+(12in)A=0 A= (40a - 160)/12

A=0: (40a-160)= C a=4in.

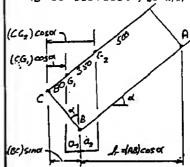


FOR EACH KEG: W-mg= (40 Rg) (9.81 m/s) = 392.4 N



P= W(a,-a,)/& +1 2 Fy=0: -w-w+P+28=0 B=W-1P

FIRM Q, and Q2 IN TERMS OF & GEOMETRY BC = 300 mm, CG, = 60 mm, CG, = 60+350 = 430mm AB = 80+350+500 = 930 mm

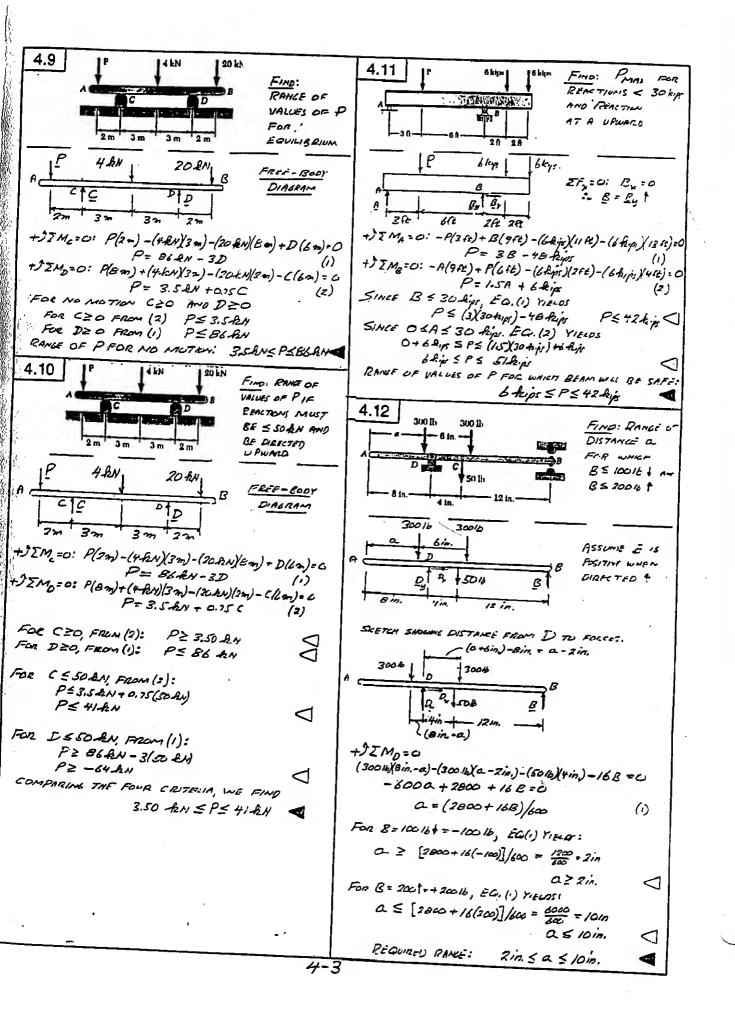


a, = (BC) SMOX - (CG) COOX a = 300 smd - 80 cost az= (C62) wax - (BC) &m = 430 cos x - 300 sind L=(AB)cod = 930 cosa

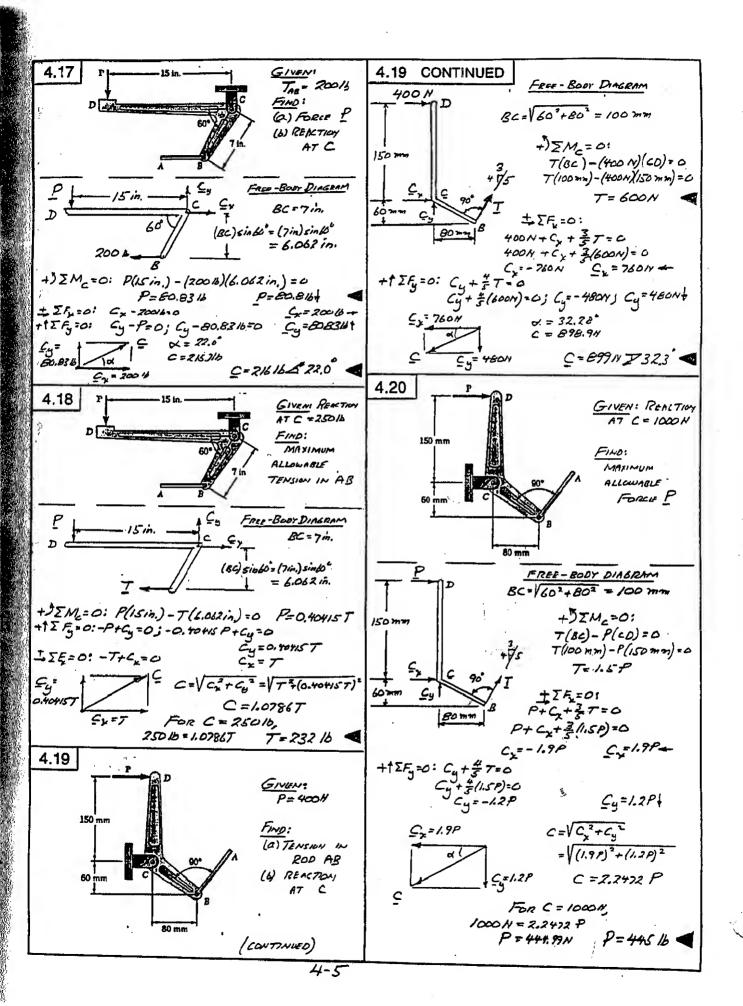
EO(1): P=W(a1-a,)/& P=W[(430 cosd - 300 sind) - (300 sind - 80 cosx) /930 cosx = (392,4 Ag) (510 cost - 600 sind) / 930 cost P=(392.4) 0.5404 - 0.6452 tona)

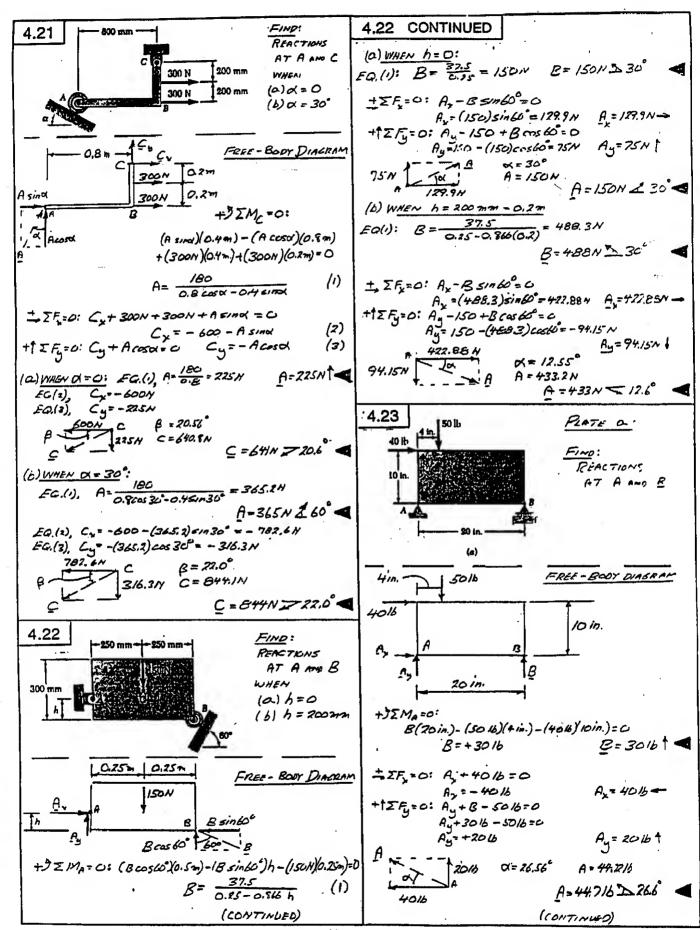
PROB. 4.7 X = 35; P=392,4 (0.5+8+-0.6+52 ton35)=+37.9N P=37.9Nt EG(2) B:W- 1P = 392.4N- 1 (379A) =+374 N B = 374N1 PROS 4.E x = 400;

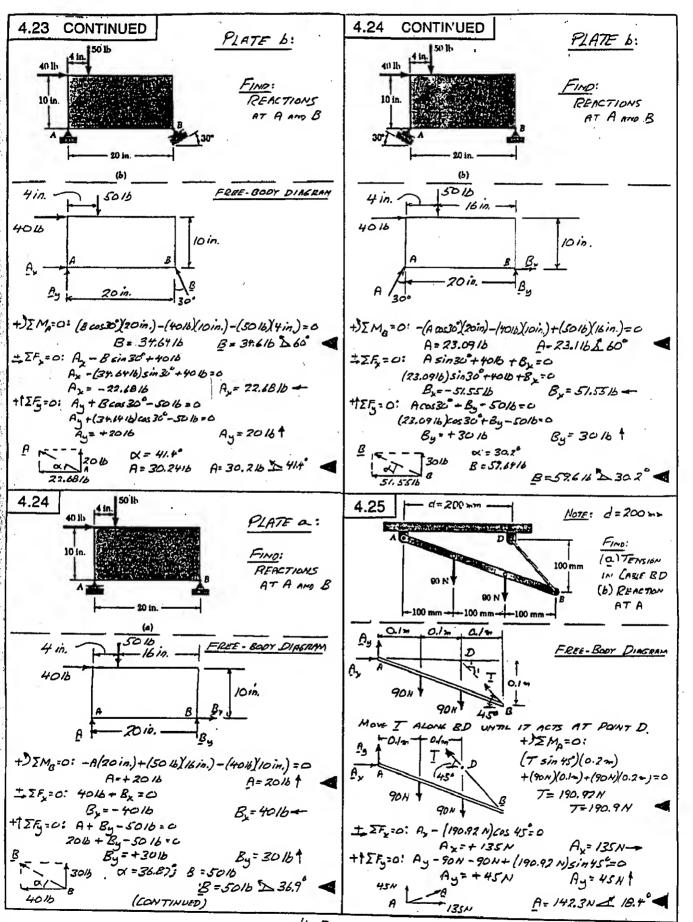
P = 392.4(0.5484-0.6452 tan40) = +2.76N P= 2.7641 EQ(2): B= W-= P= 372H - = 12.XM) =+391 N B= 39/N +

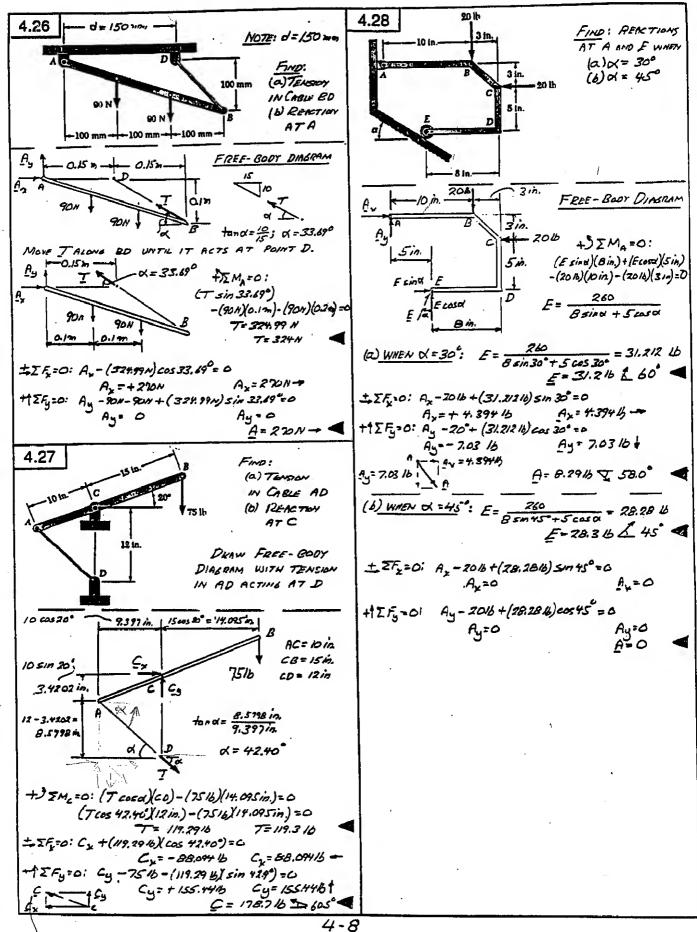


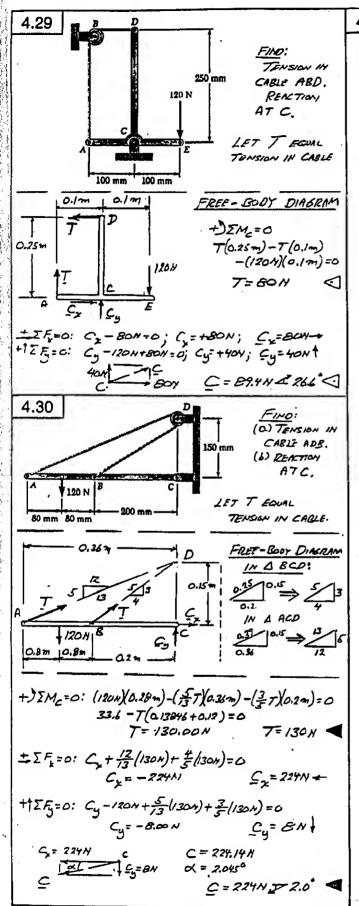


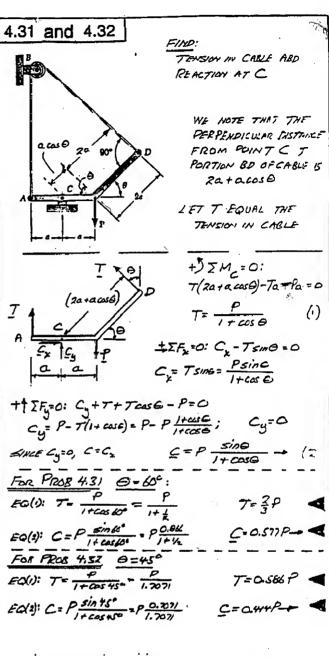




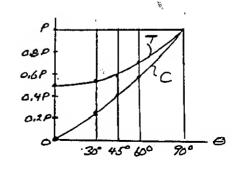


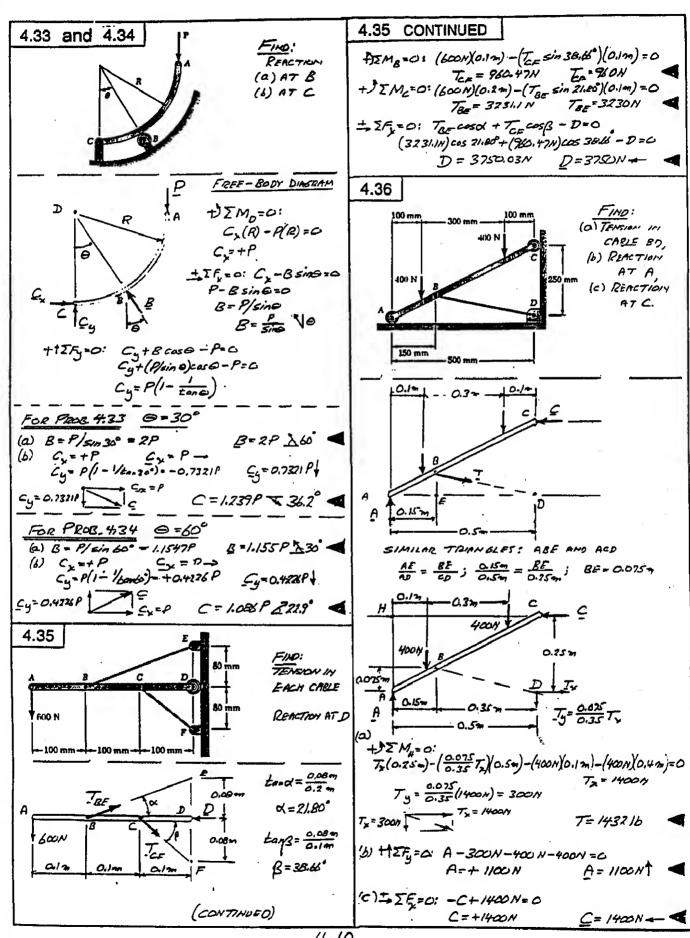


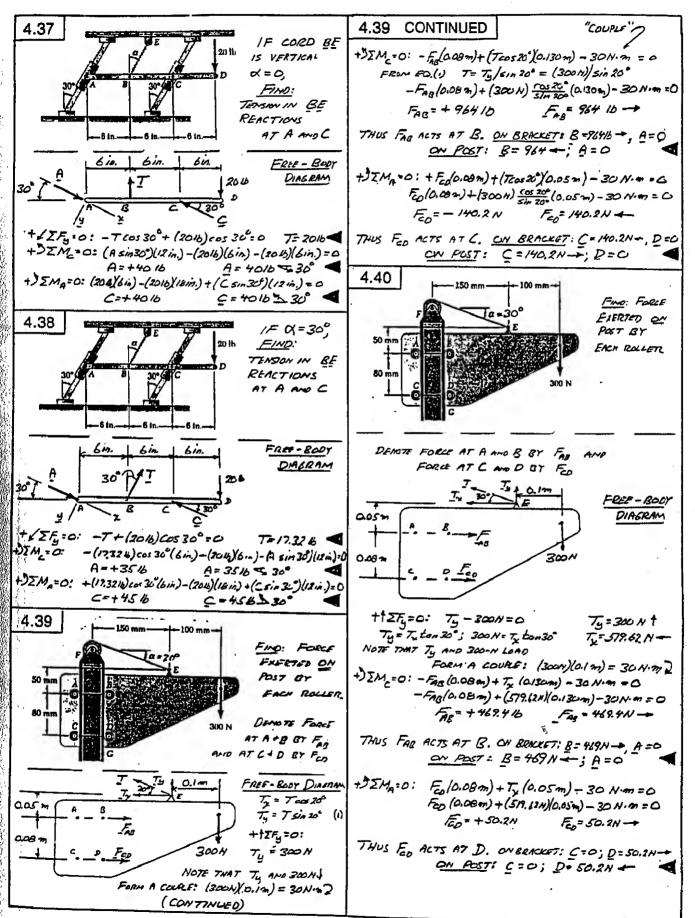


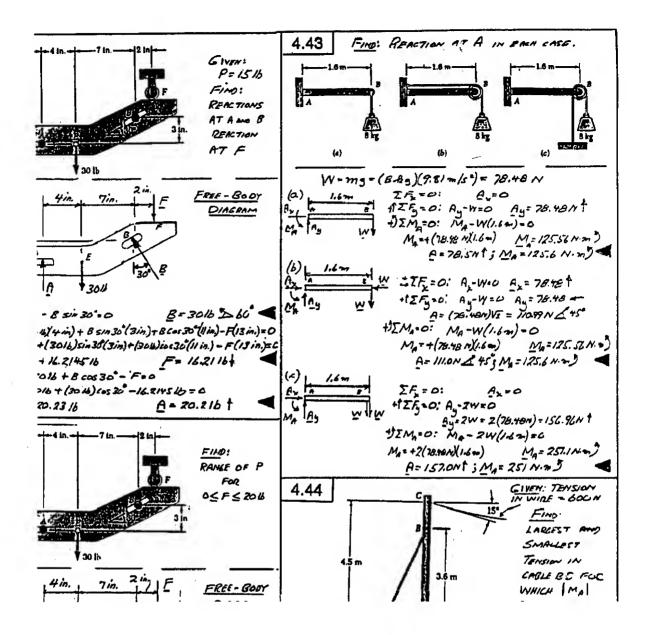


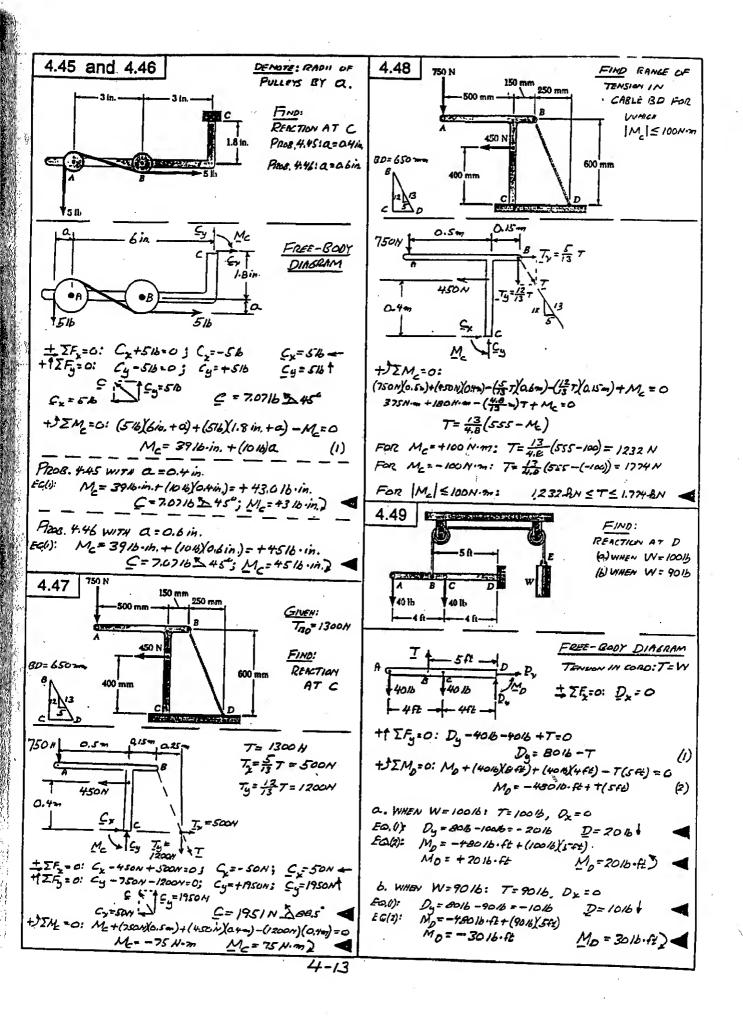
- THE FOLLOWING IS A PLOT OF TAND C FOR O & 6 & 90°

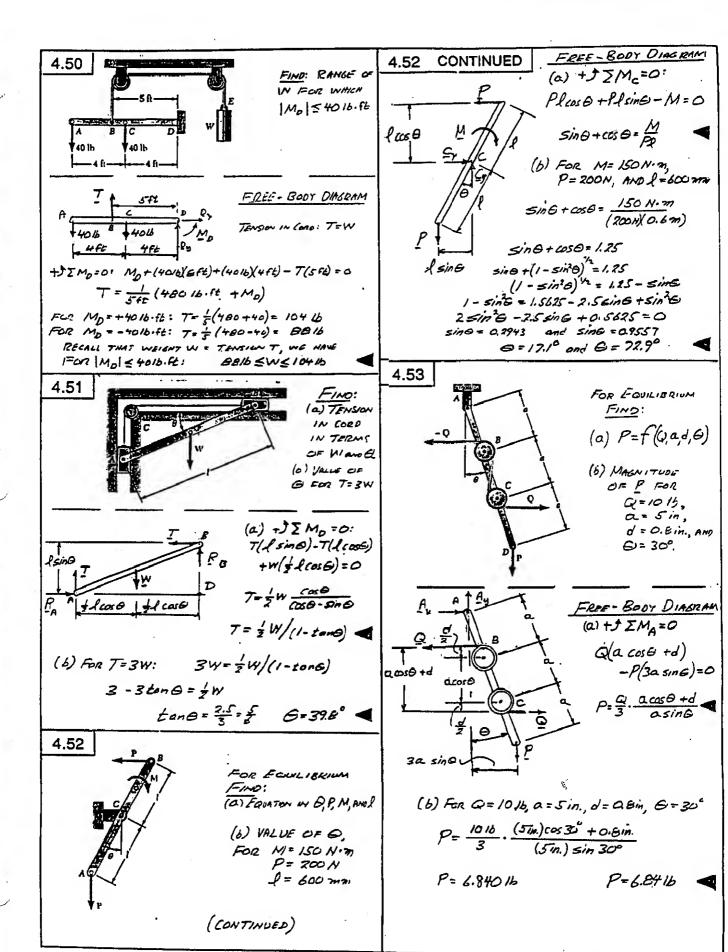


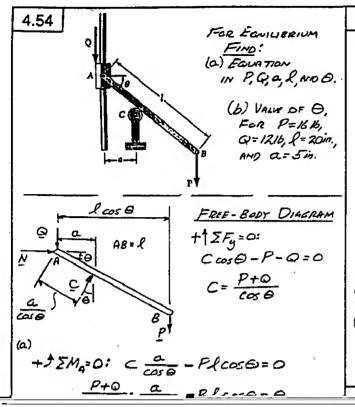


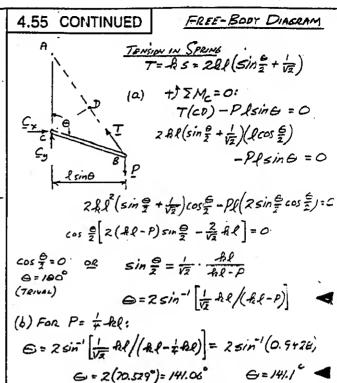


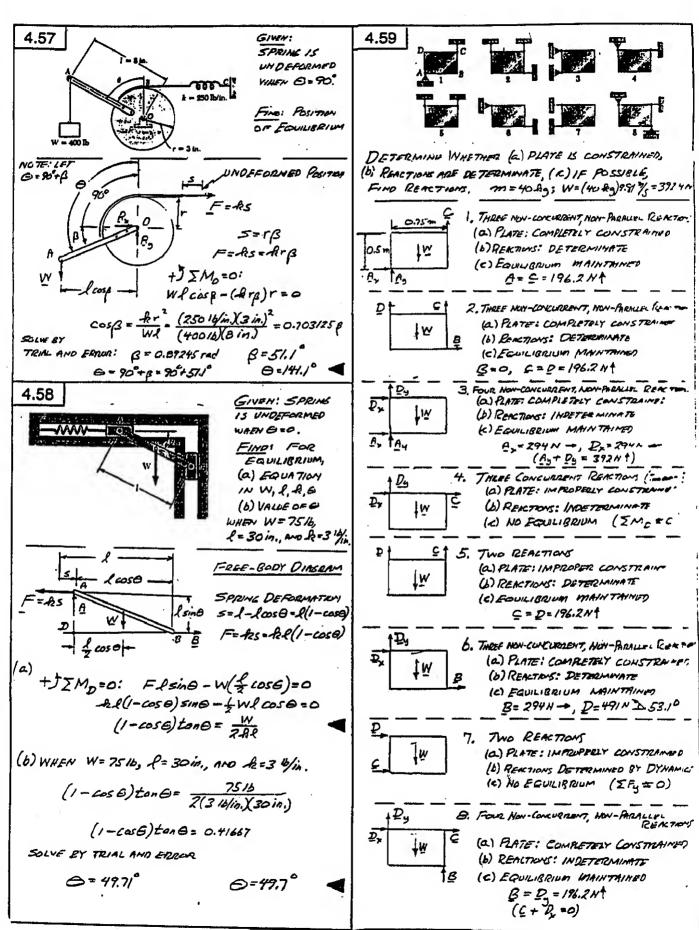


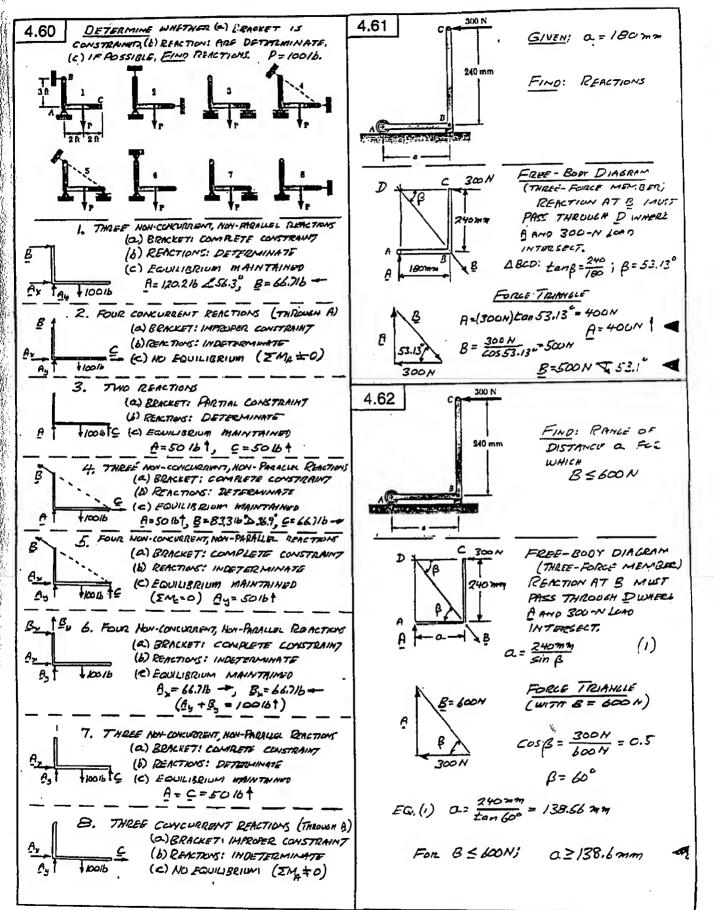


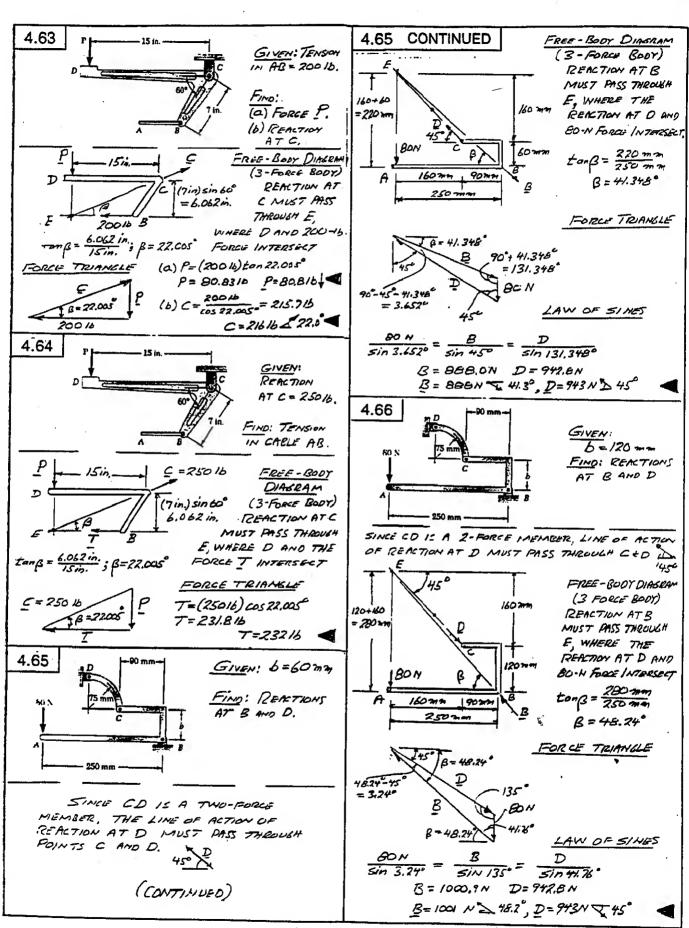


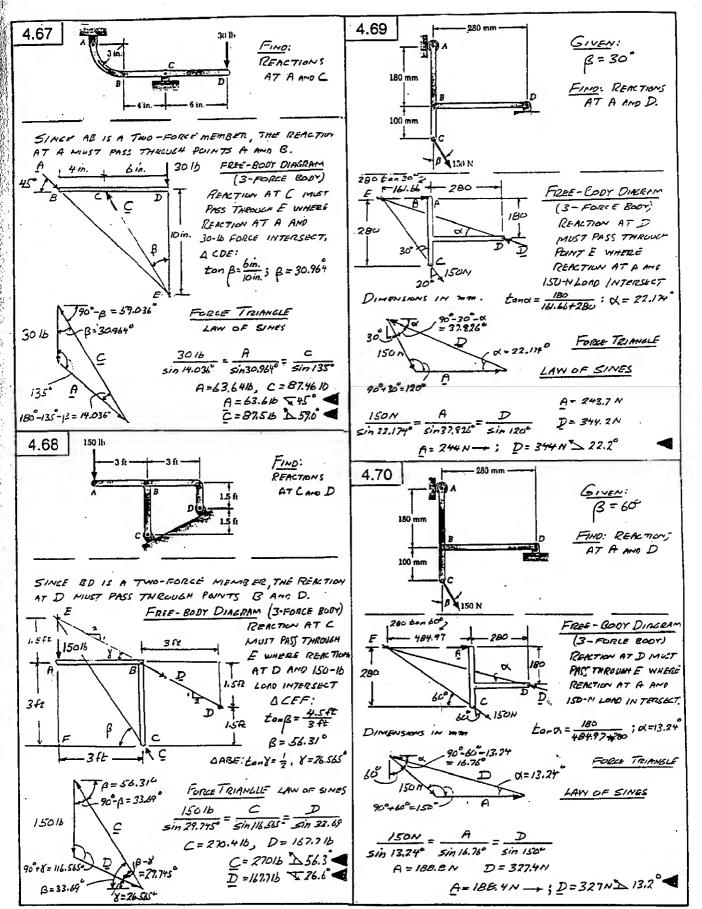


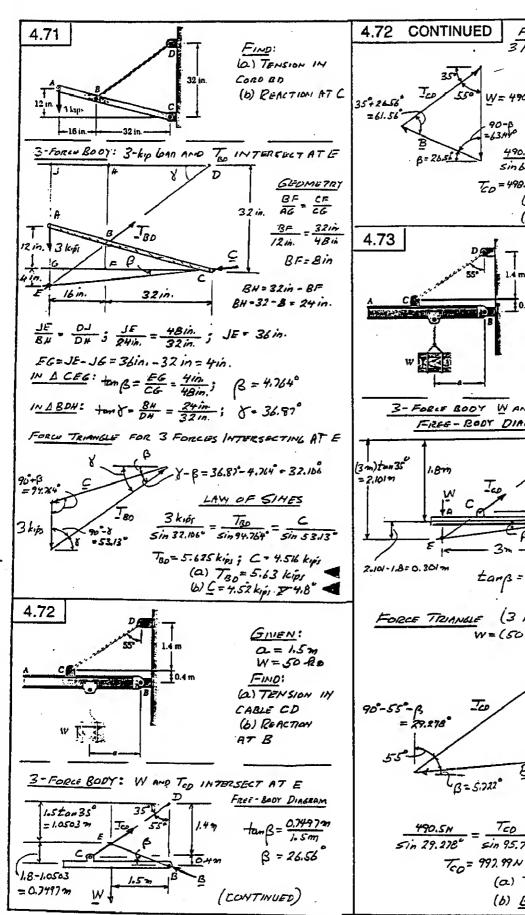


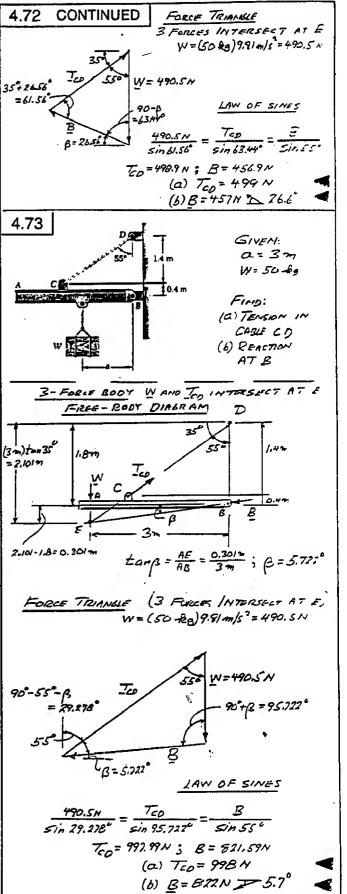


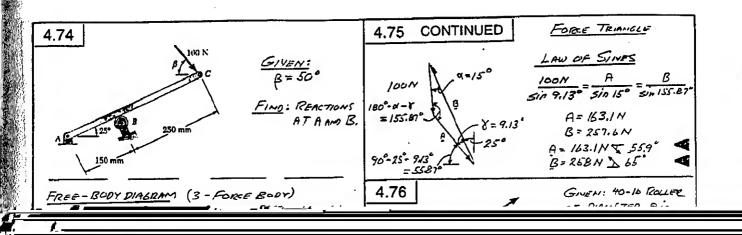


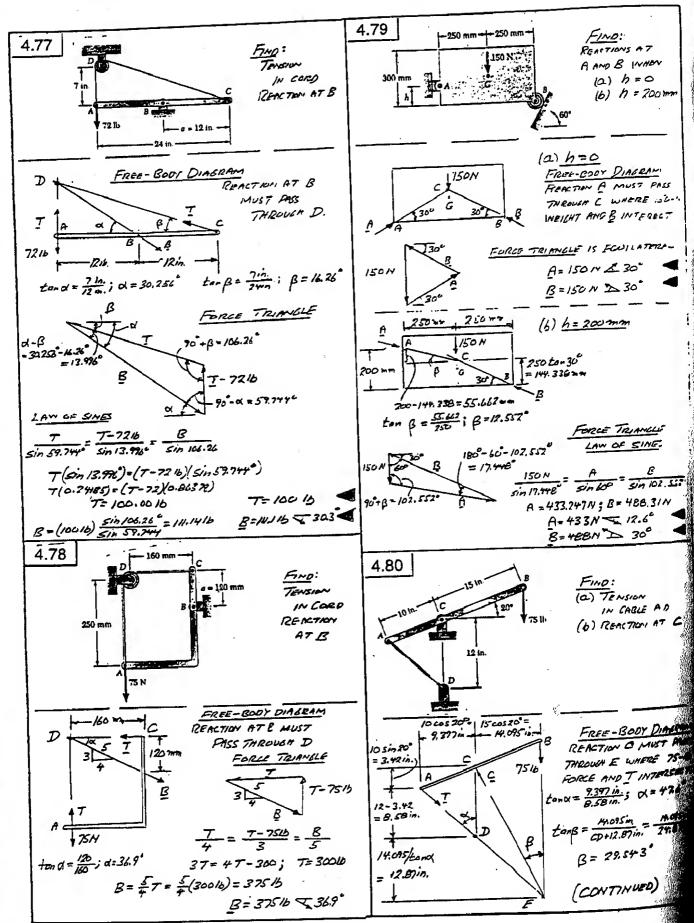


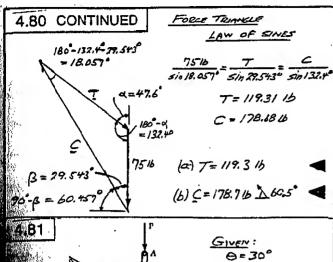


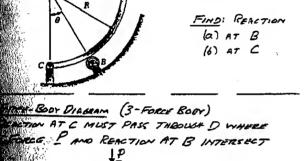


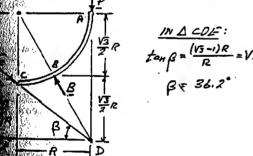




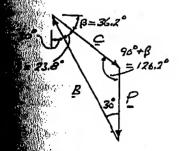




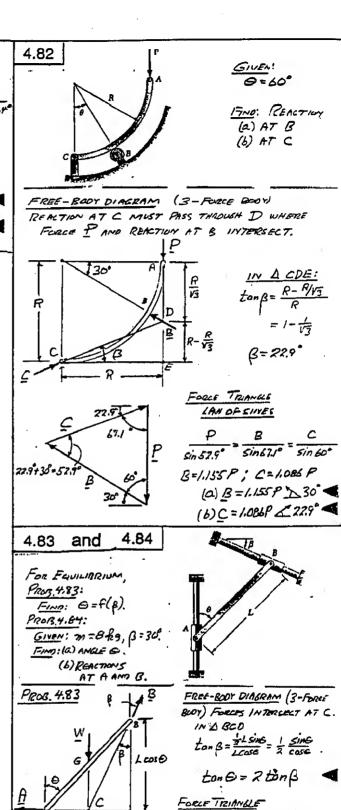


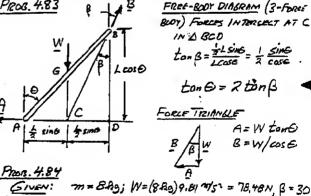


* TRANCLE

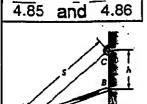


SINES 2.00 P ; C=1.239 P (a) B= ZP 1 60° (b) C=1:239P 7 362





(a) ton0 = 2ton 30 = 1.1547 G= 49.1° A= 45.3N-(b) A=W ton B = (78.48N) tan 30° B=W/CosB = (78.484)/cos36° B= 90.6N & 60°



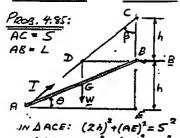
PAOB. 4.85:

FIND: EXPRESSION FOR h

Pros 4.86:

GIVEN, L=20in., S=30in., AND W=1015 FIND: (C) DISTANCE h (b) TENSION IN AC

(4) REACTION AT B



FREE-BODY DIAGRAM
(3-FORCE GOOT)
THE FORCES VI AM B
MUST INTERSECT AT D
ON LINE OF ACTION OF T.

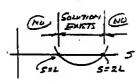
(z) (3) $h = \sqrt{(5^2 - L^2)/3}$

AS LENGTH S INCREASES
RELATIVE TO L, ANGLE @
INCREASE UNTIL ROD
AS IS VERTICAL AND
h ≥ 5-L



(1)

 $\sqrt{(s^{2}L^{2})_{3}^{2}} \geq s-L$ $s^{2}-L^{2} \geq 3(s^{2}-2sL+L^{2})$ $0 \geq 2s^{2}-6sL+4L^{2}$ $0 \geq 2(s-L(s-2L))$

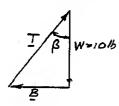


: No SOUTION FOR 5>2L

Pros 4.86 L = 20 in., S = 30 in., W = 10% $h = \sqrt{(S^2 L^2)/3} = \sqrt{(30^2 - 20^2)/3} = \sqrt{500/3}$ (a) h = 12.91 in.

IN \triangle ALE: $\cos \beta = \frac{2h}{5} = \frac{2(12.91in)}{30in} = 0.8607$ $\beta = 30.609^{\circ}$

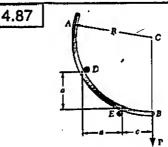
FORCE TRIANGLE



$$T = \frac{W}{\cos \beta} = \frac{10 \text{ lb}}{\cos 30.609^6}$$

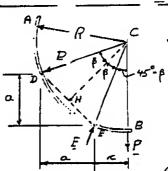
(b) T= 11.621b

B = W tonß = (1016) ton 3010



GIVEN: Q= 20 mm R = 100 mm

FIND: DISTANCE C CORRESPONDING TO EQUILIBRIUM



:. SLUME OF CH 15 \triangle 45° $DE = V\overline{2} \text{ a}$ $DH = HE = \frac{1}{2}DE = \frac{V\overline{2}}{2}\text{ a}$

SLUPE OF DE 15 145

IN Δ DHC AND IN Δ CEH: $\sin \beta = \frac{\sqrt{2} \alpha}{R} = \frac{\alpha}{\sqrt{2} R}$ $C = R \sin(45^6 - \beta)$

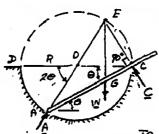
FOR a=20 mm, R=100 mm $\sin \beta = \frac{20 \text{ mm}}{\sqrt{2} (100 \text{ mm})}$; $\beta = 8.13^{\circ}$

K= (100 mm) sin (45-8:13) K= 60.0mm



GIVEN: RADIUS OF BOWL IS R.

FIND: ANGE &



FREE-BOOT DIAGRAM
(3-FORCE BODY)

POINT E IS POINT OF INTERSECTION OF A AND E.

SINCE A PASES
THROUGH O AND SINCE
C IS PERPENDICULAR

TO RUD, TRIANGLE ACE IS A RIGHT TRIANGLE INSCRIBED IN THE CIRCLE. THUS E IS A PONT ON THE CIRCLE.

NOTE THAT LOOK IS THE CENTRAL ANGLE CORRESPONDED TO THE INSCRIBED ANGLE DEA.

THUS LOOK = 20

HORIZONTAL PROJECTIONS OF AE AND AG ARE EQUAL.

(AE) C os 26 = (AG) Cos 6

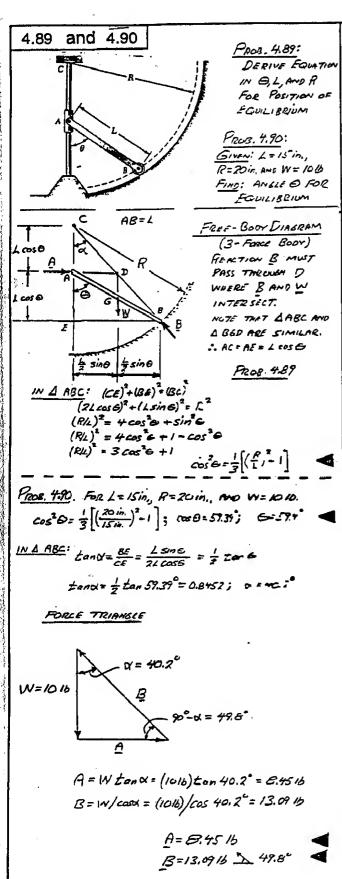
 $(2R)\cos 2\theta = (R)\cos \theta$ SET: $\cos 2\theta = 2\cos^2\theta - 1^2$ $+\cos^2\theta - 2 = \cos \theta$ $+\cos^2\theta - \cos \theta - 2 = 0$

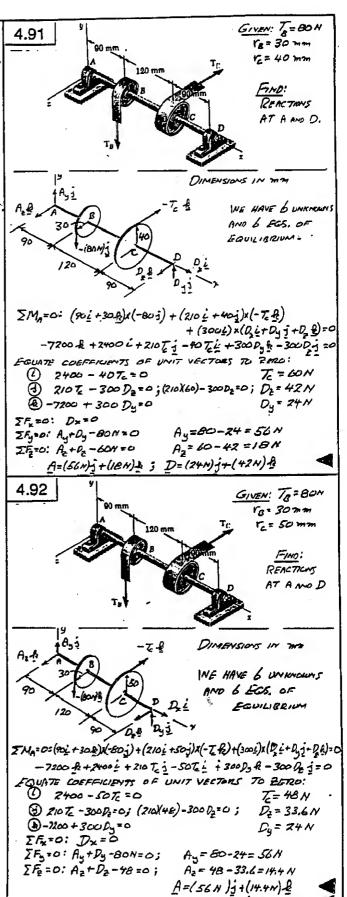
COS 0 = 0.84307

G=32,5°

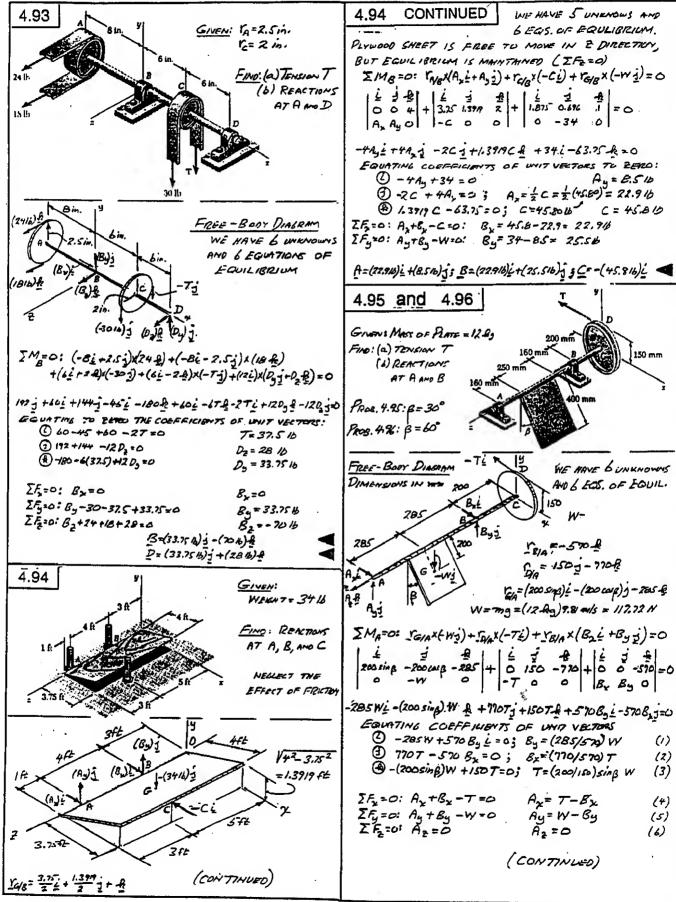
COS 6 = -0.59307

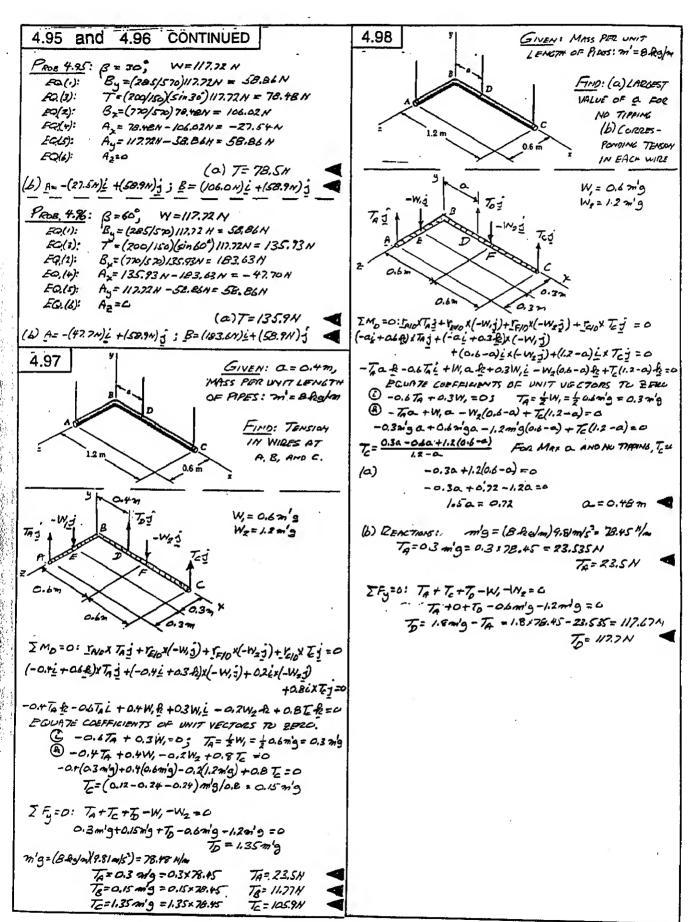
6= 126.4° (DISCARD)

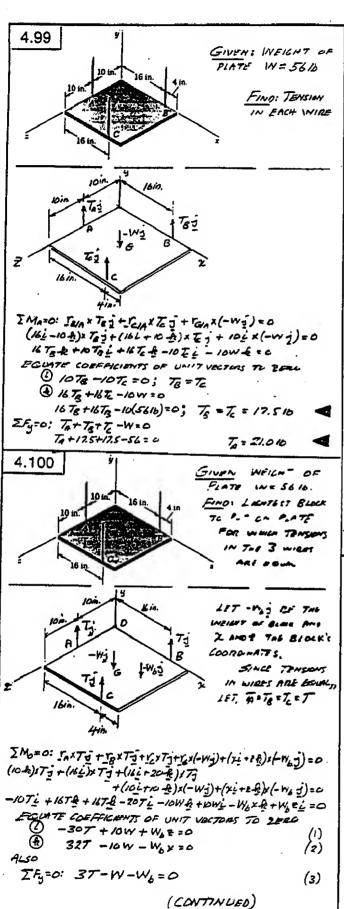


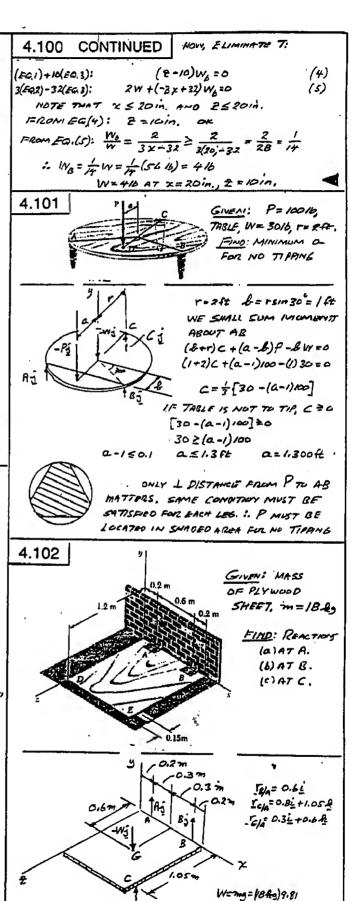


D=(24N) g+(33.6N)&



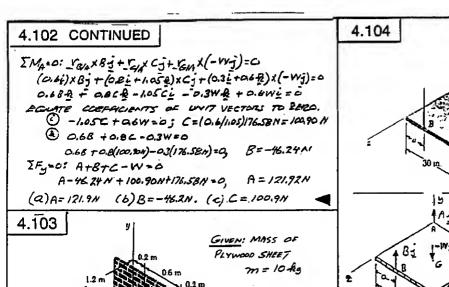






W=176,58 N

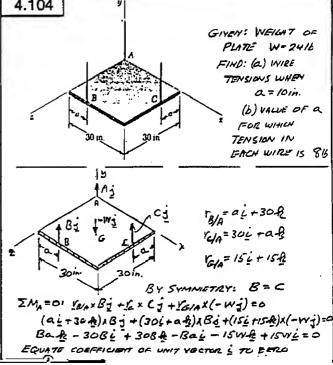
(CONTINUED)

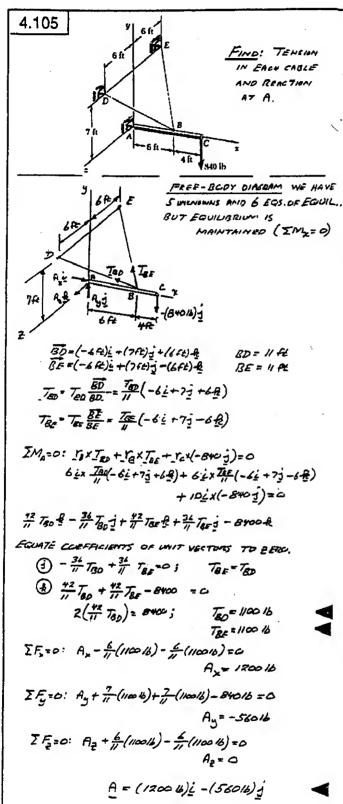


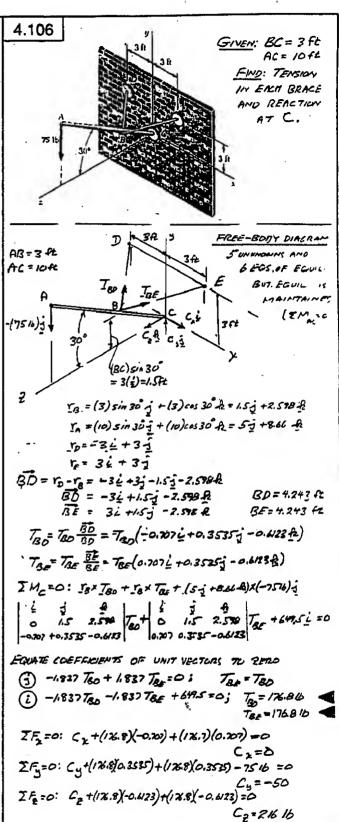
FIND: REACTIONS

(a) AT A.

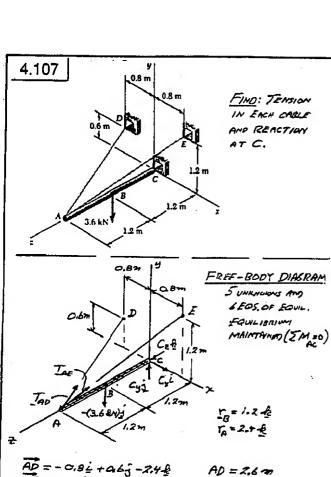
(b) AT B.







C=-(5016)j+(21616)&



$$\frac{AD}{AE} = -0.8 \frac{1}{2} + 0.6 \frac{1}{2} - 2.4 \frac{1}{2}$$

$$AD = 2.6 m$$

$$AE = 0.8 \frac{1}{2} + 1.2 \frac{1}{2} - 2.4 \frac{1}{2}$$

$$AE = 2.6 m$$

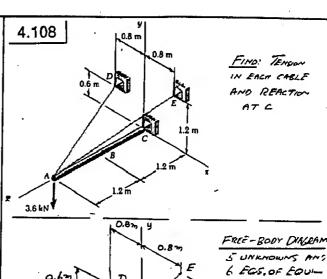
$$T_{AD} = \frac{AD}{AD} = \frac{T_{AD}}{2.6} (-0.6 \frac{1}{2} + 0.6 \frac{1}{2} - 2.4 \frac{1}{2})$$

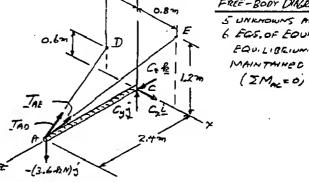
$$\begin{split} & \sum M_{e} = 0: \ \, \underbrace{Y_{A} \times T_{A0} + Y_{A} \times T_{AE}}_{T_{AE}} + \underbrace{I_{B} \times (-3RN)}_{J_{e}} = 0 \\ & | \underbrace{L}_{J_{e}} \underbrace{J}_{J_{e}} \underbrace{T_{A0}}_{J_{e}} + | \underbrace{L}_{J_{e}} \underbrace{J}_{J_{e}} \underbrace{T_{AE}}_{J_{e}} + | \underbrace{J_{A} \underbrace{F_{A} \times (-3RN)}_{J_{e}}}_{J_{e}} = 0 \\ & | - \alpha_{5} \ \alpha_{6} - 2.4 | \underbrace{J_{A0}}_{J_{e}} + | \underbrace{J_{A} \times J_{AE}}_{J_{e}} + | \underbrace{J_{A} \times J_{A} \times J_{A}}_{J_{e}} + | \underbrace{J_{A} \times J_{A} \times J_{A}}_{J_{e}} + | \underbrace{J_{A} \times J_{A}}_$$

$$\sum F_{\chi} = 0$$
: $C_{\chi} = \frac{0.8}{2.6} (2.6 \text{ RN}) + \frac{0.6}{2.6} (2.8 \text{ RN}) = 0$; $C_{\chi} = 0$

$$\sum F_{g} = 0$$
; $C_{g} + \frac{0.6}{2.6} (2.6 \text{ AN}) + \frac{1.2}{2.2} (2.8 \text{ AN}) - (3.6 \text{ AN}) = 0$

$$\Sigma_{\overline{b}} = 0$$
: $C_{\overline{b}} = \frac{7.4}{2.6} (2.6 \text{ km}) - \frac{7.4}{2.8} (2.3 \text{ km}) = 0$
 $C_{\overline{b}} = 1.800 \text{ km}$
 $C_{\overline{b}} = 1.800 \text{ km}$





$$T_{AD} = \frac{\overline{AD}}{AD} = \frac{T_{AD}}{2.6} (-0.8 i + 0.6 j - 2.4 \frac{A}{2})$$

$$ZM_{c}=0$$
: $Y_{A} \times \overline{I}_{A0} + \overline{I}_{A} \times \overline{I}_{AE} + \overline{I}_{A} \times (-3.6 RN) \frac{1}{2}$
FACTOR Y_{A} : $Y_{A} \times (\overline{I}_{A0} + \overline{I}_{AF} - (3.6 RN) \frac{1}{2})$

$$\frac{C_{OERF, OE \dot{L}}: -\frac{7_{AB}}{2.6}(0.8) + \frac{7_{AE}}{2.8}(0.8) = C}{7_{AB}:= \frac{7.6}{2.8}T_{AE}}$$
 (1)

COEFF OF j:
$$\frac{7a0}{2.4}$$
 (0.6) + $\frac{7a6}{2.8}$ (1.2) - 3.6-2N = 0
 $\frac{2.6}{2.8}$ $7aF(\frac{0.6}{2.4}) + \frac{1.2}{2.6}$ $7aF - 3.6$ $42N = 0$
 $7aF(\frac{0.6+1.2}{2.8}) = 3.6$ $42N$

$$T_{AE} = 5.600 \text{RN}$$
 $T_{AE} = 5.600 \text{RN}$ $= 5.600 \text{RN}$ $= 5.200 \text{RN}$

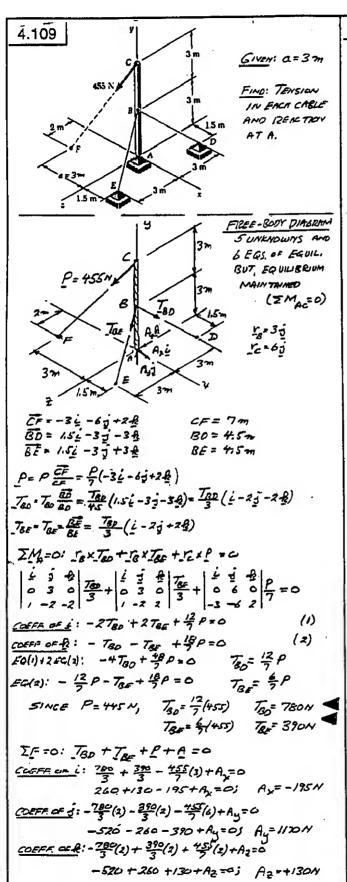
$$\sum_{k=0}^{\infty} (-\frac{1}{2.6}(3.2+hn) + \frac{1}{2.8}(3.6+hn) = 0; C_{\chi} = 0$$

Ify=0:
$$C_y + \frac{c.6}{2.6}(5.2RN) + \frac{1.2}{2.8}(5.6RN) - 3.6RN = 0$$

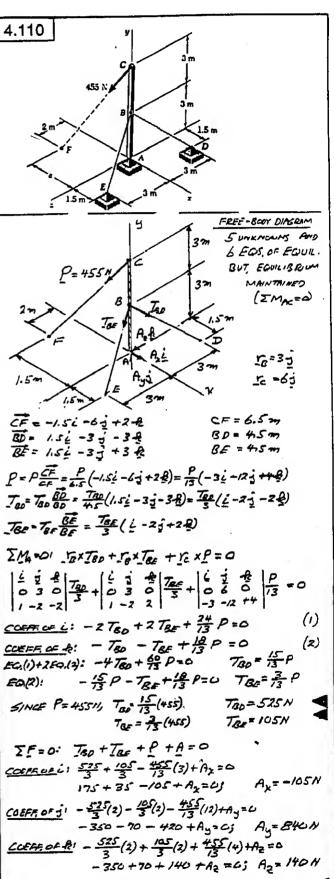
$$\sum_{f_2=c:} C_2 - \frac{2.4}{2.6} (5.2 \text{ AN}) - \frac{2.4}{2.8} (5.6 \text{ AN}) = 0$$

$$C_2 = 9.6 \text{ AN}$$

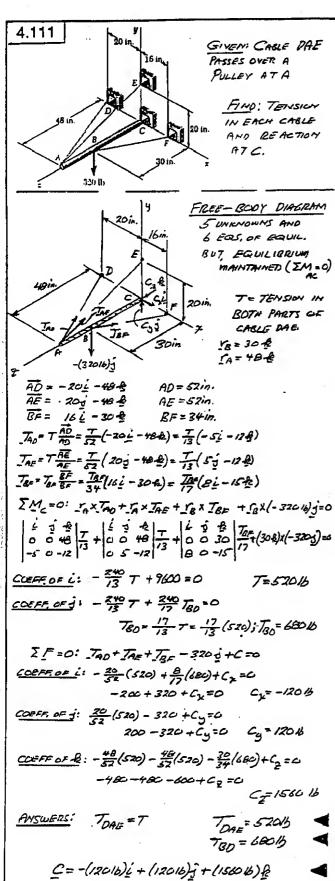
C=(9.6-BN) A NOTE: SINCE FORCES + REACTION ARE CONCURRENT AT A, WE COULD HAVE USED THE METALOS OF CHAPTER ?

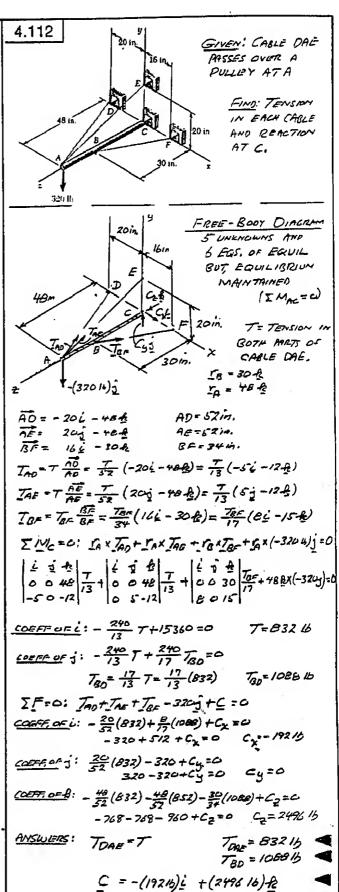


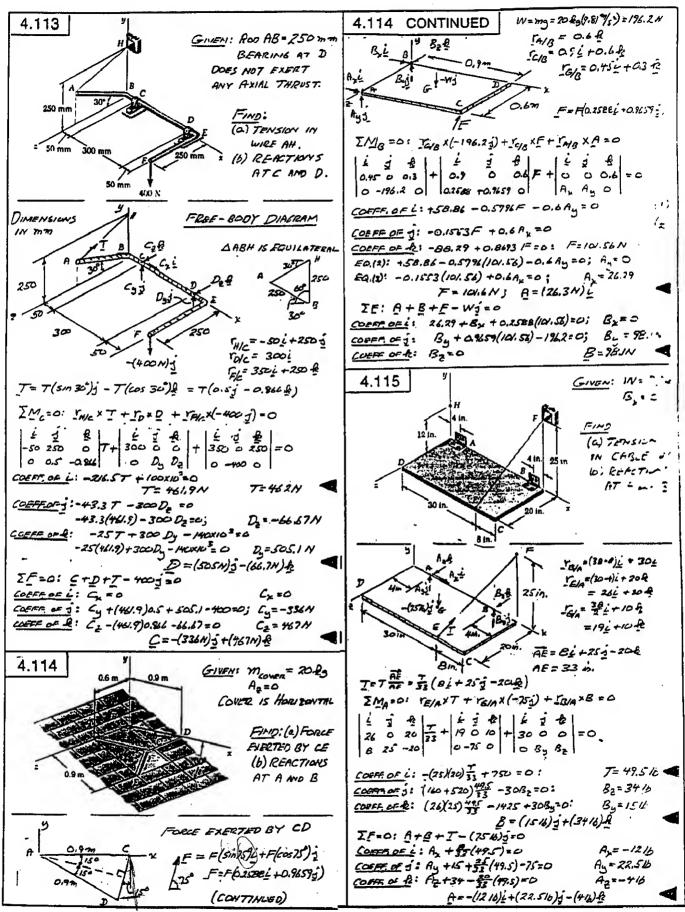
A=-(195N) +(1120N) +(130N)&

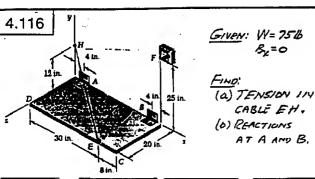


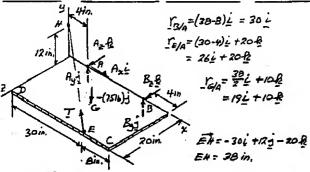
A=-(105N)++(840N) + (140N)&











$$T = T \frac{EH}{EH} = \frac{T}{38} \left(-30 \frac{L}{4} + 29 - 20 \frac{R}{2} \right)$$

$$IM_{A^{2}} O: Y_{E/A} \times T + I_{GA} \times (-750) + I_{RA} \times B = 0$$

$$\stackrel{\stackrel{\stackrel{\cdot}{}}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\uparrow}}{\uparrow} \stackrel{\stackrel{\uparrow}{\uparrow}}{\uparrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\uparrow} \stackrel{\stackrel{\uparrow}{\uparrow}}{\uparrow} \stackrel{\stackrel{\uparrow}{\uparrow}}{\uparrow} \stackrel{\stackrel{\uparrow}{\uparrow}}{\uparrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\uparrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\uparrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\downarrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\downarrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\uparrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\downarrow}{\downarrow}}{\downarrow} \stackrel{\stackrel{\downarrow}{$$

COSEF. OF 6 - (12)(20) ₹+750=0; T=118.25; T=118.816 coeff. OF j: (-600 + 520) 118.75 - 308=0; B=-8.336

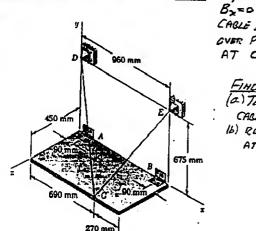
COFFF. OF A: (26)(12) 118.75 -1425+308, =01 By= 15.00 B B= (1516) 2-18,3316) &

IF=0: A+B+T-(756) ==0

COFFF. OF i: fly - 20 (118.75) = C . Ax=93.7516 COFFE OF 5: Ay +15 + 12 (18.75) - 75=0 Auf 22.5 16 CCEFF. OF A: A: -8.33 - 30 (118.71) + 0 A2=70.1315

A = (93.816) + (22.516) + (20.816) &

4.117 and 4.118

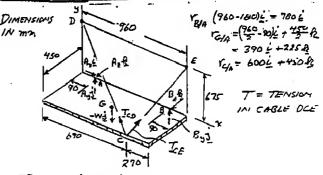


CABLE DOE PASSES OVER PULLEY AT C. FIND:

GIVEN: mplate = 100 ftg

(a) TENSION IN CABLE DEF. 16) REACTIONS AT A AND B.

4.117 and 4.118 CONTINUED



CD = - 690 + 675 j - 450 - R CD = 1065 mm CE = 2701+675j-450-A CE = 855 mm T= T (-6901+6752-450-4) Top= 7 (270: +675j-450-12) W=-mgi--1100 kg/9.81 m/s2) = - (981 N) 5

PROB. 4.117

IMA = 0: ICIAX TED + YOUR TEE + YOUX (-W)+YOUX B = 0 600 0 450 7 + 600 0 450 0 55+ -670 675 -450 7065+ -690 675 -450

+ 300 0 225 + 780 0 0 = 0 0-780 0 0 By B2

CONFF. OF L: - (450)(675) T - (450)(675) T + 220.725 x103 = 0

T= 345N T=344.6 N

COFFF OF J: (-6706450+600x450) 344.6 +(R708450+6008450) 3446 B2= 185.49 N -780/S=0

COUPE OF R: (600)(675) 3446 + (600)(675) 3446

- 382.57410 + 780B4; By=1/3.2N

IF=0: A+B+ To+Zo+W=0 = (113,2N) + (1855N) & COST. OF L: Az - 600 (3444) + 200 (2444) =0; CDEFF. OF J: Ay + 13.2 + 105 (344.4) + 25 (344.4) - 20 | 60; Ay = 377 N

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) - 20; Ay = 377 N

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) = 0; Az = 141,5 N

A= (144.4 N) L + (377 N) Ay + (144.5 N) Az

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) = 0; Az = 141,5 N

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) = 0; Az = 141,5 N

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) = 0; Az = 141,5 N

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) - 20; Az = 141,5 N

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) - 20; Az = 141,5 N

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) - 20; Az = 141,5 N

CDEFF. OF J: Ay + 185.5 - 405 (344.4) - 455 (344.4) - 405

PRUB. 4.118

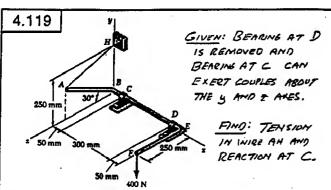
IMA = 0: TOUXE + YOUX (-W3)+YOUXB=0 \(\frac{1}{2} \) \(\frac{1} \) \(\frac{1}{2} \) \(\frac{1}{2} \) \(\frac{1}{2} \) \(\frac{ 0-181 0 0 By 82

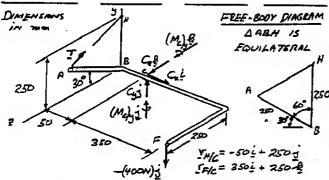
T=621N ECEFFO DE 3= (270×450 +600×450) 621.3 -780B2=0; B2=364.7 N COPPE OF A: (600)(675) 6713 - 382,59163+7808=0; B= 113.2N B=(113.2N) 3+(365H) 1/2

IF=0: A+B+ Tosty =0

COFFE OF L: Az + 270 (6213)=0 Az=-196.2N. COFFF. OF 9: Ay + 1/3.2 + 675 (621.3) -981=0; Ay= 377.3N COFFF. OF A: A2 + 3647 - 450 (621.3)=0

A=-(196.2N)+(377N)-(37.7N)A





T= T(sin 30) j-T(cos 30) k = T(0.5 j - 0.8 k k) IMC=0: TE/EX (-400 j) + YA/EXT + (Me) j+ (Me) & + 0 -20 250 O T+(ME) 3+(ME) == 0 350 0 250 0 0.5 -0.864

COEFF. OF. L: + 100×103-216.5 T=0; T=4619N; T=462N

(Mc)y=20×0 Nom; (Mc)y=20Nom

(Mc)y=20×0 Nom; (Mc)y=20Nom

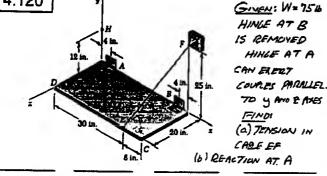
(Mc)y=20×0 Nom; (Mc)y=20Nom

(Ma) = 151.57x103 Nomm; (Ma)=157.5 Him

If = 0: C+T-400 -0 -0

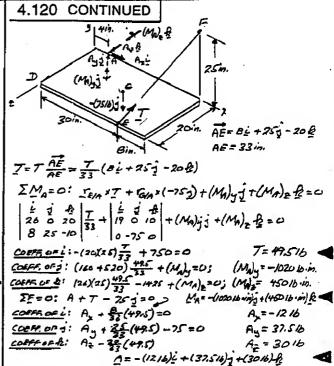
Me= (20Nom) + (151, 5Nom) & COSFF. C. C , EO Cx = 0

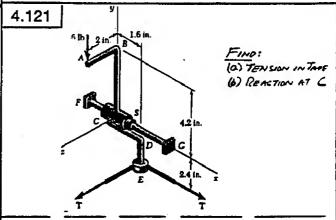
CUEFF. OF 1: Cy + 0,5(461,9) =400=0
CUEFF. OF &: C2 -0.966(461,9)=0 C.F 169.1N =400N C= (169.1N) + (400N) & 4.120 HINGE AT B

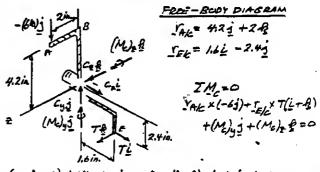


YEM= (30-4) + +204 = 26 + 20 & IGA = (0.5×38) +10 = 19 + +10 A

(CONTINUED)





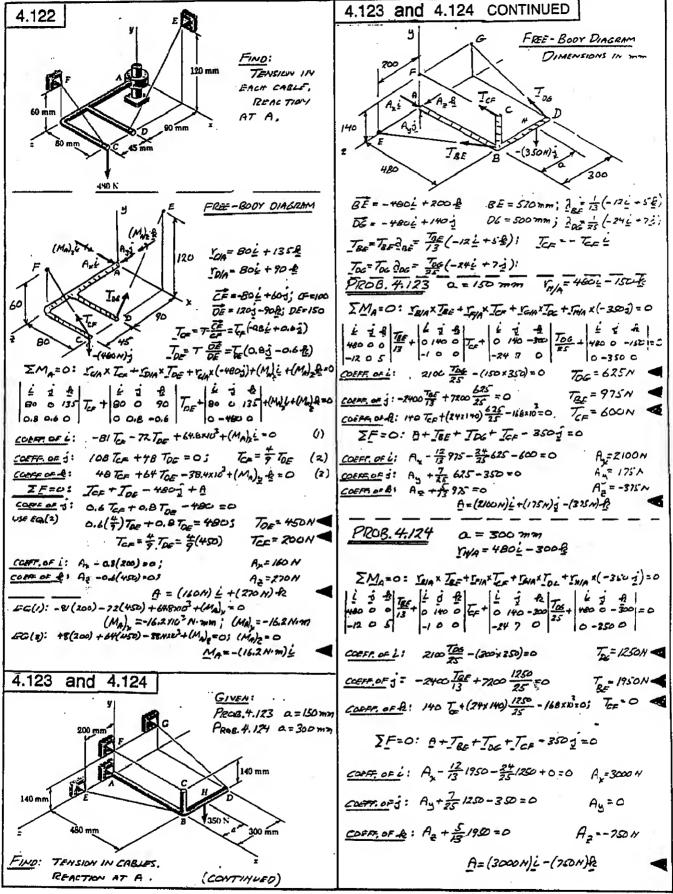


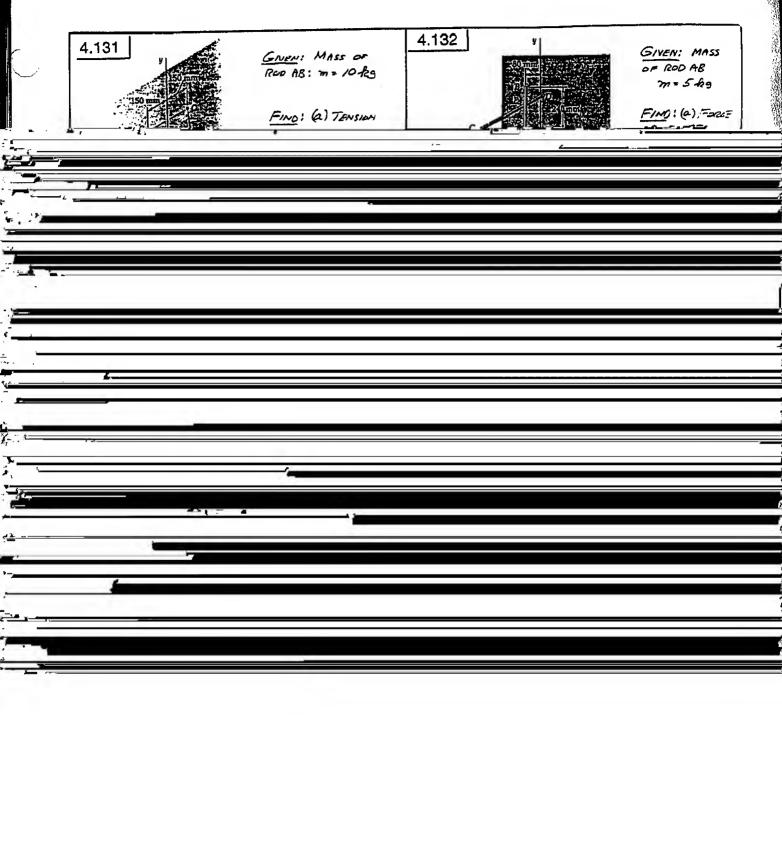
(42 = +2 +2)x(-6) + (16 i -2.4) xT(i++)+(M2) j+(M2) = = 0 CORFF. OF L: 12-2.47=01 T=510 -1.6(54)+(Me)y =0 (M) = 816.in. (Ma) = -1216.in. COPPE OF j: 2.4(54) + (ME)=0 CCEFFOF B:

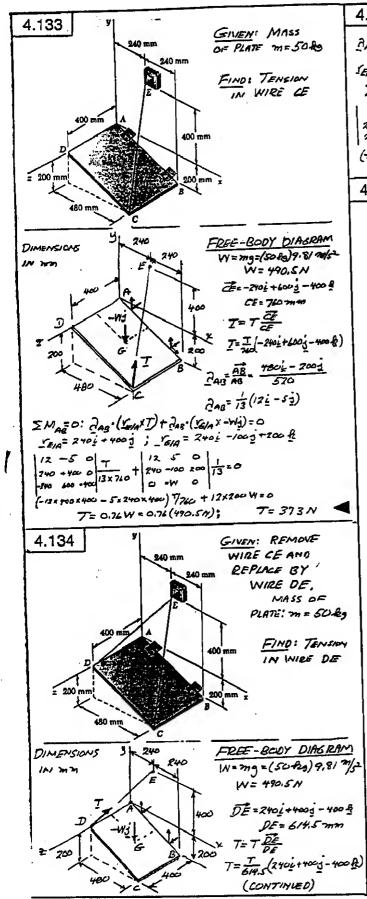
M=(BID-in) =- (12 10 in) }

EF=0: C, i + Cy i + C= & - (614) j + (514) i + (614) } = C

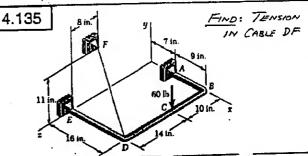
ESUATE COFFFICIENTS OF UNIT VELTORS TO 2016 Cx= -516 Cy = 616 C=-(510)+(616)-j-(516)A

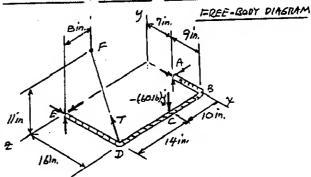






4.134 CONTINUED



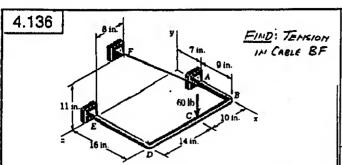


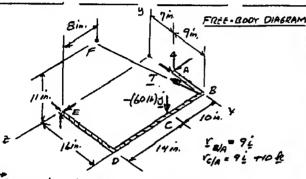
$$\hat{A}_{FR} = \frac{\vec{E}\vec{R}}{\vec{E}\vec{A}} = \frac{7\vec{E} - 24\vec{A}}{25}$$

IMER = 0: BER - (TOLEXT) + BER - (YOLE - (-60)) = 0

$$-\frac{24\times16\times11}{21\times26} + \frac{-7\times14\times60 + 24\times16\times60}{26} = 0$$

T=85,3 1b

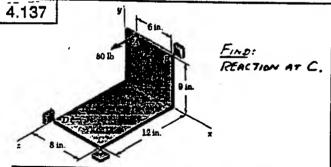


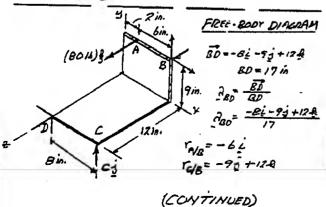


$$\begin{array}{ll}
\overrightarrow{BF} = -16\underline{i} + 11\underline{j} + 16\underline{R} & BF = 25.16 in. \\
T = T \frac{BF}{BF} = \frac{7}{25.16} \left(-16\underline{i} + 11\underline{j} + 16\underline{R} \right) \\
\overrightarrow{ABE} = \frac{\overline{AB}}{\overline{AB}} = \frac{7\underline{i} - 24\underline{R}}{7}
\end{array}$$

- 24×9×11 25×25-16 94.4267-17,160 =0

T= 181.716

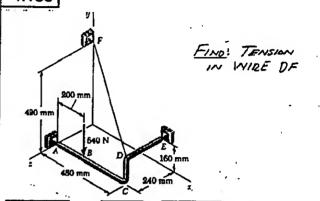


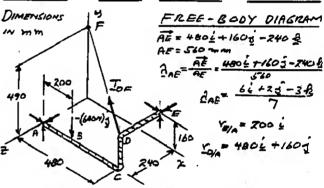


4.137 CONTINUED

 $\sum_{BD} = 0: \underbrace{\lambda_{BD}}_{BD} \left(\underbrace{x_{AB}}_{CAB} - C \right) + \underbrace{\lambda_{BD}}_{CAB} \left(\underbrace{x_{AB}}_{CAB} - (Bolb) + \frac{1}{4} \right) = 0$ $\begin{vmatrix} -8 - 7 & 12 \\ 0 - 9 & 12 \\ \frac{1}{17} + \begin{vmatrix} -8 & -9 & 12 \\ -6 & 0 & 0 \\ 0 & 0 & 60 \end{vmatrix} = 0$ $\underbrace{\lambda_{AB}}_{CAB} = 0: \underbrace{\lambda_{AB}}_{CAB} = 0: \underbrace{\lambda_{AB}}_$

4.138





DF = -480 i + 320 i - 240 k; DF = 680 mm

TOF = TOF OF = TOF -480 + 3303 - 240 k = TOF - 16i + 1/3 - 8 k

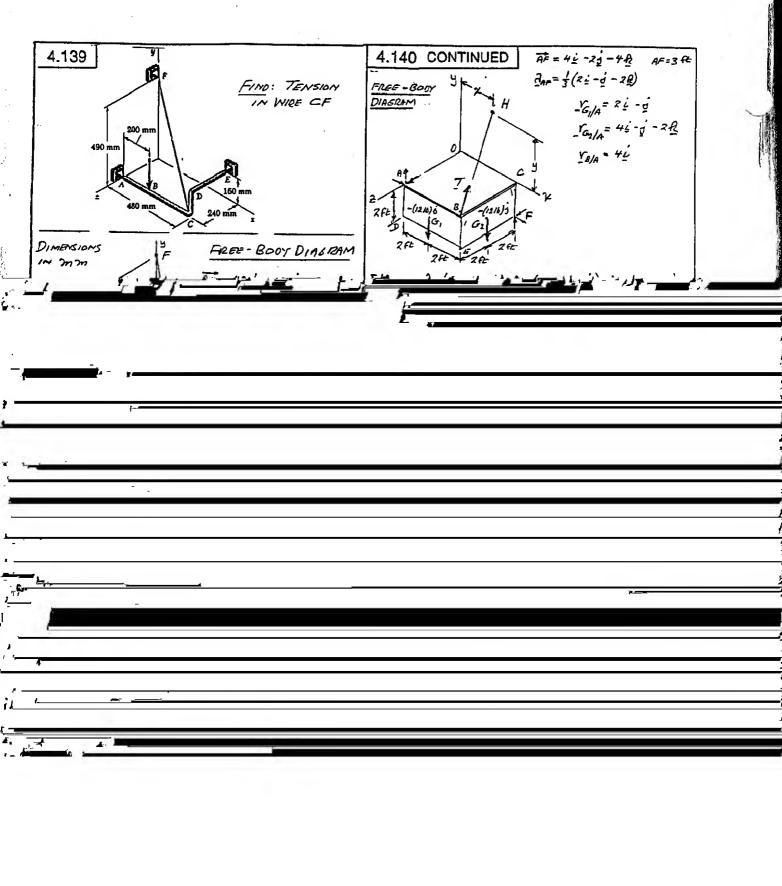
$$\sum_{AE} M_{AE} = \frac{1}{2} M_{E} = \frac{(Y_{Q/A} Y_{DE})}{2} + \frac{1}{2} M_{E} = \frac{1}{2} \frac{1}{2} = 0$$

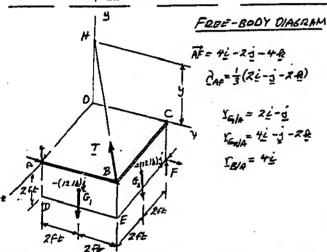
$$\begin{vmatrix} 6 & 2 & -3 \\ 460 & 160 & 0 \\ -16 & 11 & -8 \end{vmatrix} = \frac{1}{2} \frac{1}{1} = 0$$

$$-6x K_{Q/A} + 2x 480 \times 8 = 2x 480 \times 11 = 2x 160 \times 16 = 0$$

$$-1120 T_{DE} + 384 \times 10^{2} = 0$$

Tom = 3+2.9 N . Tos = 3+3N





 $\begin{vmatrix} 2 & -1 & 2 \\ 2 & -1 & 0 \end{vmatrix} \frac{1}{3} + \begin{vmatrix} 2 & -1 & 2 \\ 4 & -1 & -2 \end{vmatrix} \frac{1}{3} + \frac{1}{2} \frac{1}{4} \frac{1}{4} \cdot \left(\frac{1}{2} \frac{1}{4} \times \frac{1}{2} \right) = 0$ 0-120 0-120 (2222) = + dag ((2122) = C ZAF. (YBIAXT)=-32 (1)

BN = -41+45-4-B BH = (32+7) 12 T=T BH = T -46+49-4R (32+42)2

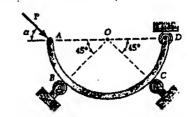
 $\hat{C}_{AF}(r_{BH} \times 7) = \begin{vmatrix} 2 & -1 & -8 & T \\ 4 & 0 & 0 \\ -4 & 4 & -4 \end{vmatrix} = \frac{7}{3(32+3^2)} \hat{r}_2^2 - 32$

 $(-16-8y)T = -3x32(32+y)^{1/2}$ $7 = % \frac{(32+y)^{-1}}{8y+16}$ $\frac{dT}{dy} = 0: 96 \frac{(8y+4)\frac{1}{2}(92+9)^{-1/2}(24) + (32+9)^{3/2}(6)}{(8y+46)^{2}}$

NUMBERATURE = 0: (84+16) y = (32+42) 8 2 842+164 = 32x8+84 y=16ft €

FG.(2): T= 26 (32+162)1/2 = 11.31316 T= 11.3116

4.142 and 4.143



PRUB. 4.141: FOR X = 45, FIND REACTIONS AT B, C, AND D.

PRUB. 4.142: FIND RANGE OF X FOR EQUILIBRIUM.

FREE-BOOY DIAGRAM Psing PCOSON BNE

+3 IM0=0: (Psina)R-D(R)=0

(2: \$IF,=0: PCOSX +B/V2-C/V2=0

+ 12Fg=0: -Psina + B/V2 + C/V2 - Psina = 0 (3. -28sind +B/V2 + 4/V2 = 0

(2)+(3): P(cosx -2 sina) + 2B/VZ = 0

 $B = \frac{\sqrt{2}}{2} (2 \sin \alpha - \cos \alpha) P$ (+

P(cosx + Zsma) - ZC/VZ =0 /2)-(3):

C= = (ZeinX + COEX)P

PROB 4142 FOR X = 45°; SINX = COSK = 12 EQ(4): B= (是一世) P= P; B=P645°

EG(5): C = \frac{\frac{1}{2}}{2}(\frac{1}{12} + \frac{1}{12})P=\frac{3}{2}P; C=\frac{3}{2}P\delta 45^c \

D= 8/3 1 EQ.() D=PNZ

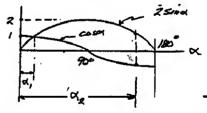
PROB. 4.143 RANGE OF & FOR EQUILIBRIUM

FOR .830:

25ind -cosx >0 FROM EQ.(4):

FOR CZO:

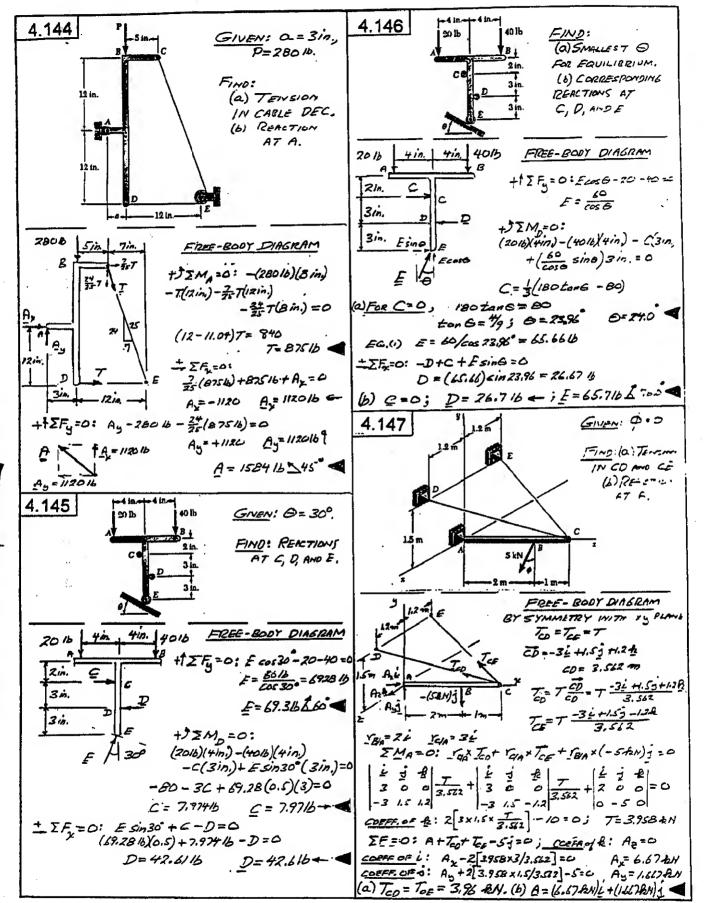
From Fa(s): 2 sina + cosa 20

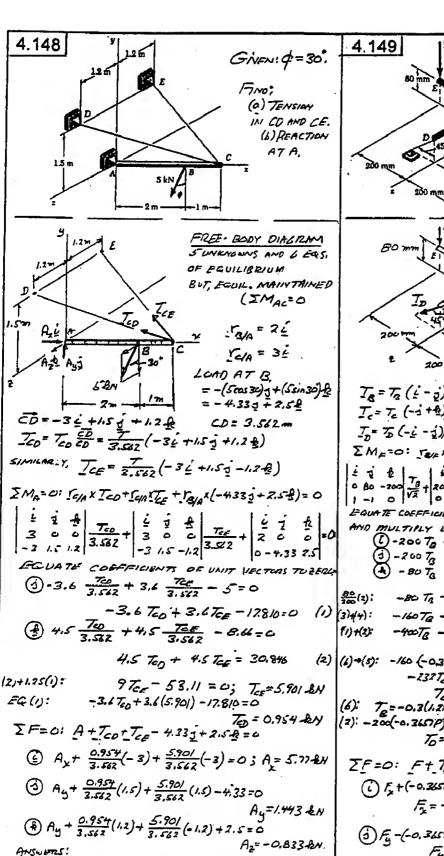


2 SING & COSO, tand, 2 0.5 × ≥ 26.6° 25/40 2 - COSO 2 tand2 - 0.5 d≥ 153.4°

26.6 € × ≤ 153.4

FOR THIS RANGE SINGED, THUS EG(1) YIELDS D>0, OK

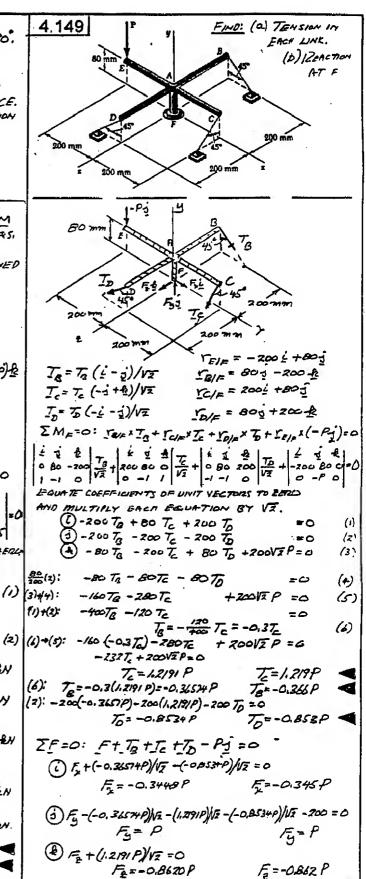




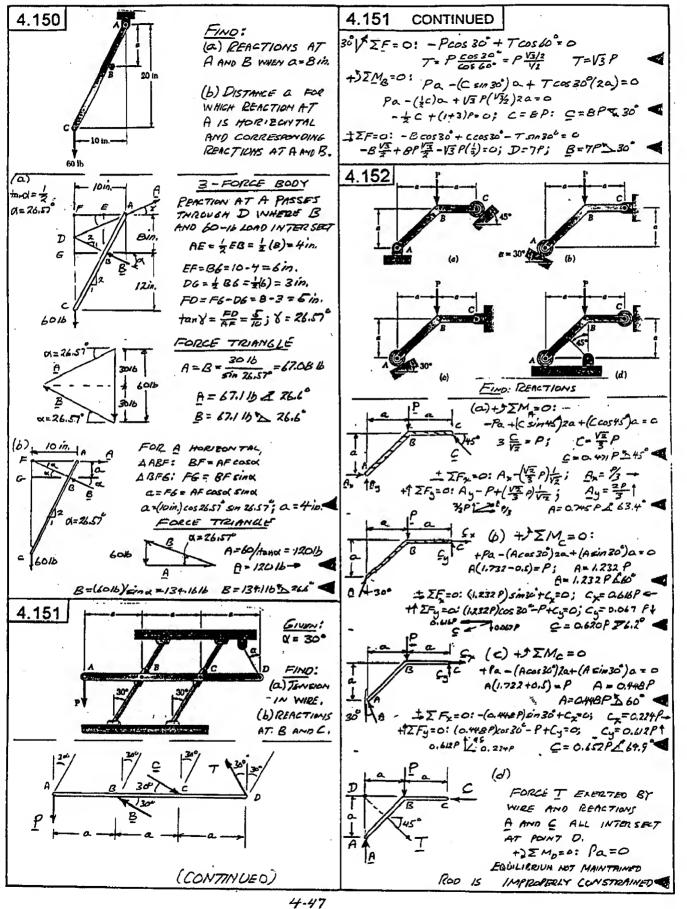
(a)

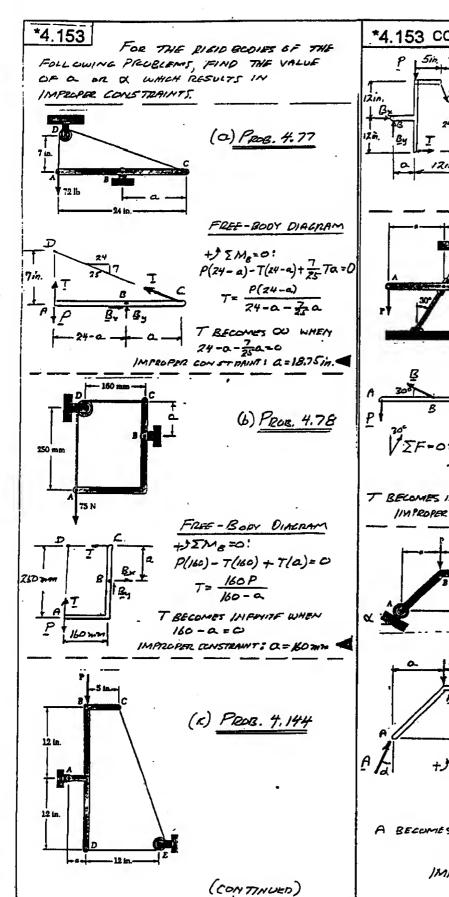
TCD=0.954 AN; TCE=5.90 AN

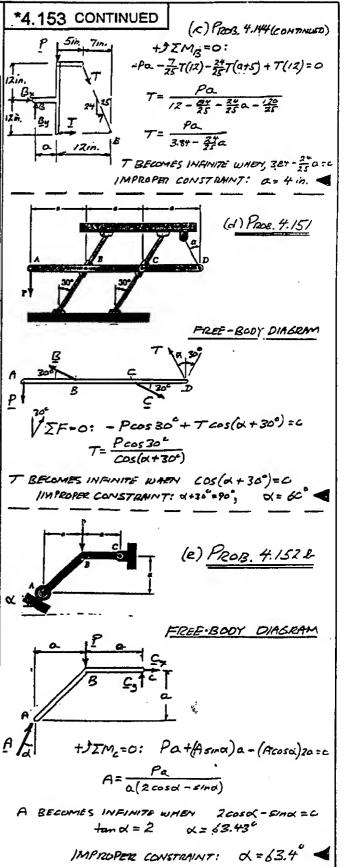
A = (5.77-12N)+(1.443 DN) 5-(0.833 DN) &

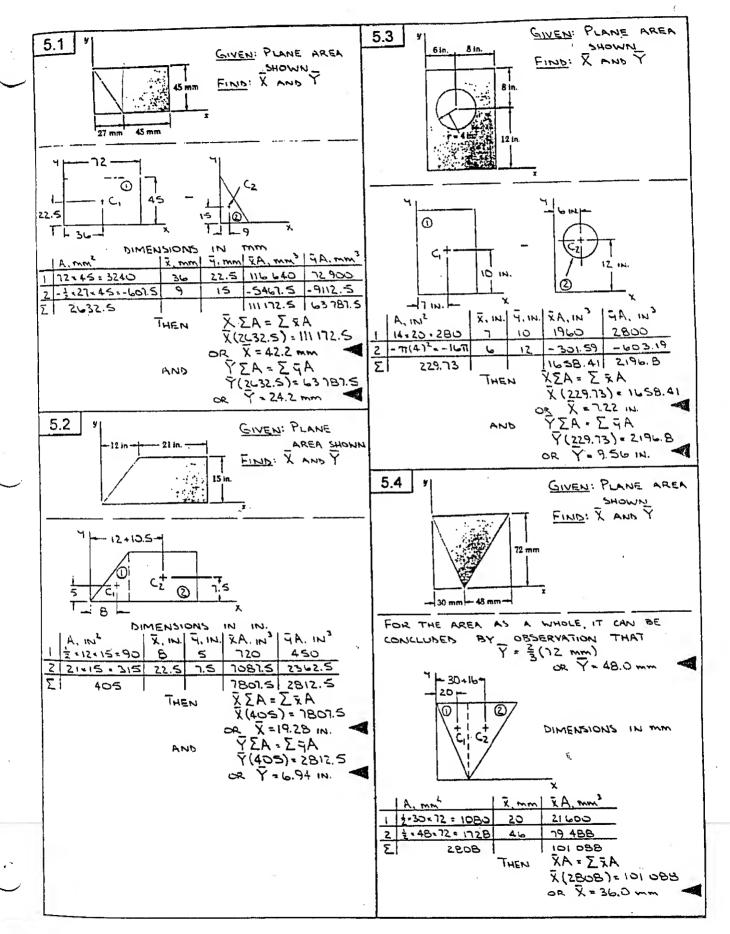


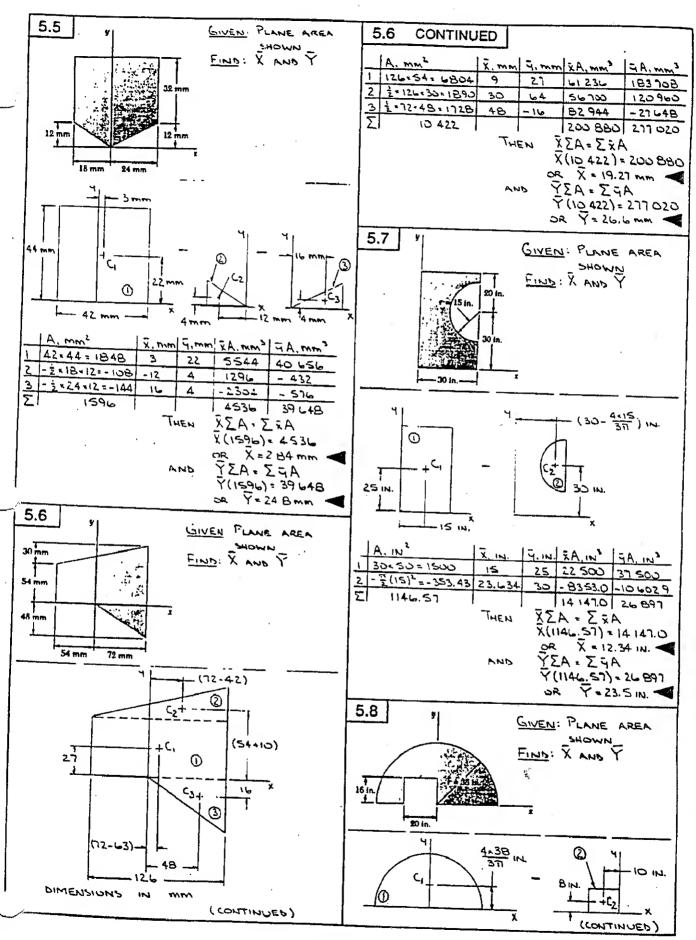
F=-0,345Pi+Pj-0,862P-B

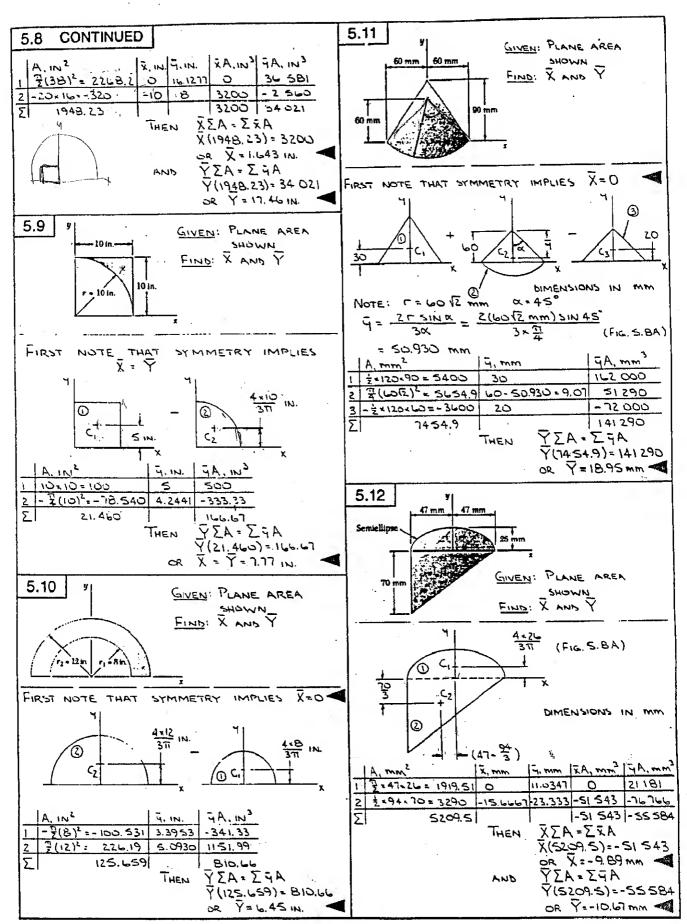












and a desire that the second

CONTINUED 5.16 X,mm F.mm XA,mm3 GA,mm3 \$ - LO = 150 = 2250 48 42.857 108 000 94 429 5.3511 - 3375 - 753,35 2-4-30-18.75-140.425 24 104 625 95 675 2109.4 <u> ΧΣΑ = Σ λΑ</u> THEN X(2109.4) = 104 625 DR X = 49.6 mm 4F3=A39 AND Ÿ(2109.4)= 95675 OR Ÿ= 45.4 mm ■ 5.17 and 5.18 5,17 GIVEN PLANE AREA SHOWN FIND: $A^{3} = (\frac{T}{2} - \alpha) L_{S}^{2}$ = 3/2 (2-a) SIMILARLY ... $\overline{q}_1 = \frac{2}{3} \Gamma_1 \frac{\cos \alpha}{(\Omega - \alpha)}$ $A_1 = (\frac{\Omega}{2} - \kappa) \Gamma_1^2$ IHEN. ZAY = 3 2 (1 - x) (1 - x) LS - 3 4 (1 - x) [1 - x) [2 - x) [2 - x] = 3 (53- 53) cosa $\sum A = (\frac{5}{2} - \alpha) r_2 - (\frac{5}{2} - \alpha) r_2$ $=\left(\frac{\pi}{2}-\alpha\right)\left(r_{3}^{2}-r_{1}^{2}\right)$ $\frac{1}{2}\left[\left(\frac{S}{2}-\kappa\right)\left(\frac{C_{5}}{2}-\frac{C_{5}}{2}\right)\right]=\frac{3}{5}\left(\frac{C_{5}}{2}-\frac{C_{5}}{2}\right)\cos\kappa$ Now A = 3 45-43 cora GIVEN: PLANE AREA SHOWN <u>5.18</u> SHOW: Y APPRIDACHES Y OF AN ARC OF RAMUS Z(TIATZ) AS

1 - 12

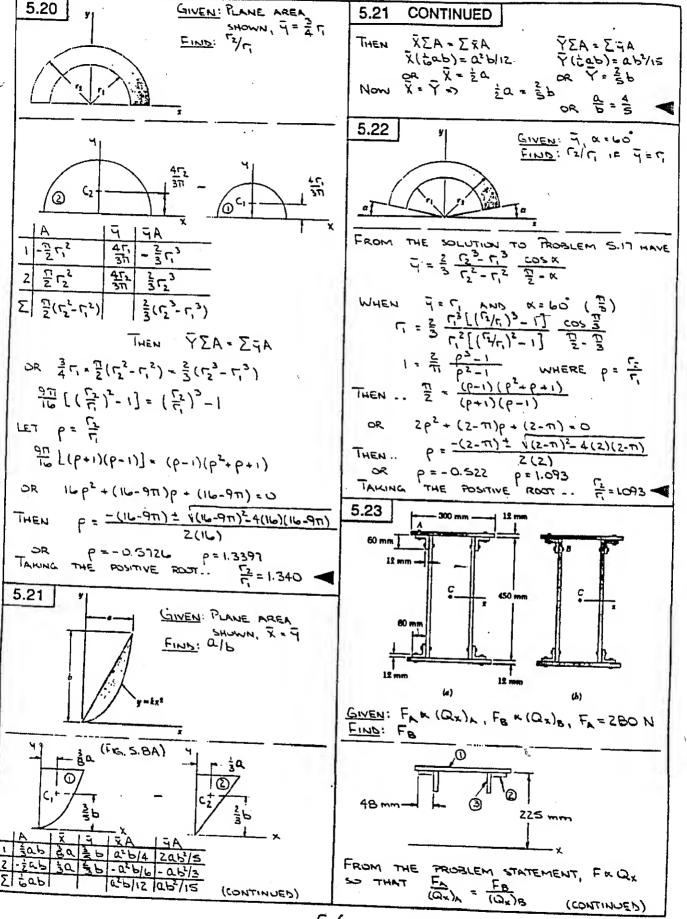
2(1+12) 15- = = (1-12) SIN(2-a)

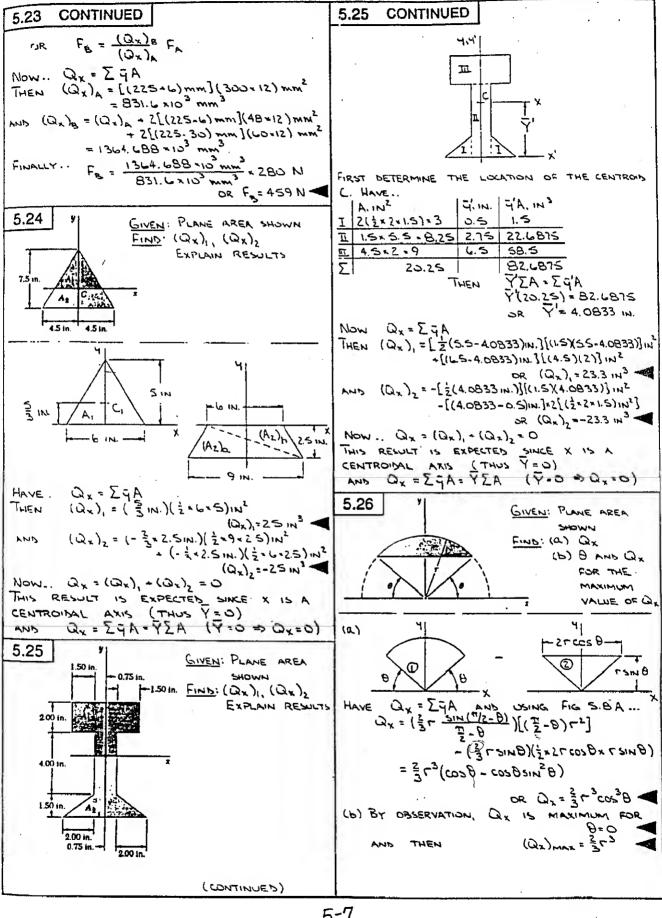
 $=\frac{1}{2}(\Gamma_1 + \Gamma_2)\frac{\cos\alpha}{(\frac{n_2}{2} - \alpha)}$ (CONTINUED)

GIVEN: PLANE AREA

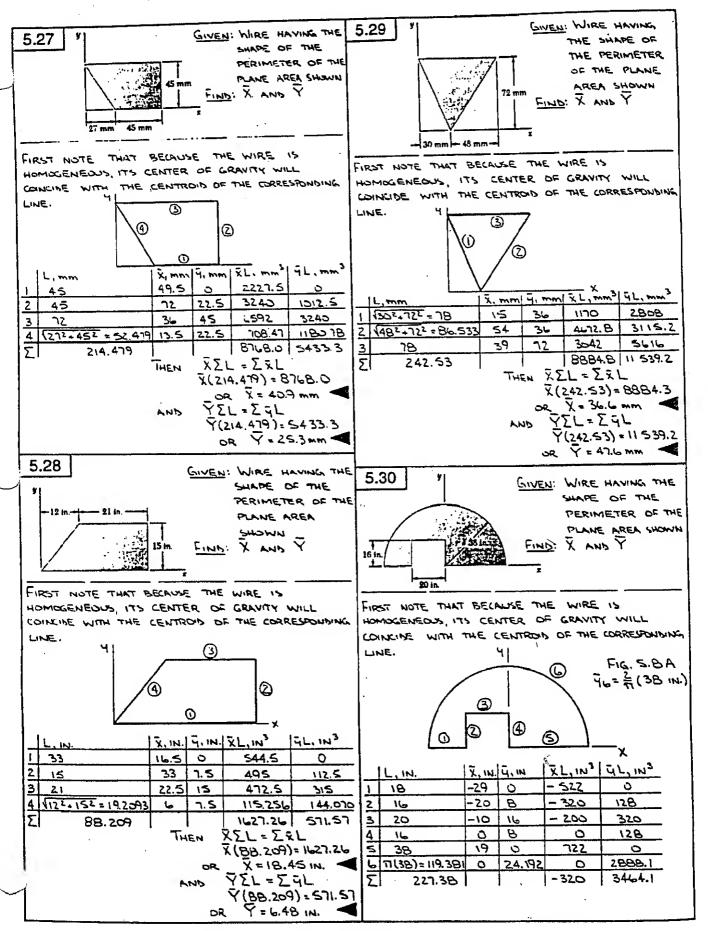
5.17 and 5.18 CONTINUED FROM THE SOLUTION TO PROBLEM 5.17 HAVE $Y = \frac{2}{3} \frac{r_2^3 - r_1^3}{r_2^2 - r_1^2} \frac{\cos \alpha}{2} - \alpha$ $= \frac{C_5 + L'}{C_5 - L'_5} = \frac{C_5 + L'}{(L^5 - L')(L^5 + L'_5)}$ $\frac{C_5 - L'_5}{C_5 - L'_5} = \frac{(L^5 - L')(L^5 + L'_5)}{(L^5 - L')(L^5 + L'_5)(L^5 + L'_5)}$ 72 = C + D LET L' = L-V THEN $\frac{C_{2}-C_{2}}{C_{2}-C_{2}} = \frac{(C+D)^{2}+(C+D)(C-D)+(C-D)^{2}}{(C+D)^{2}+(C+D)^{2}+(C+D)^{2}}$ $= \frac{3r^2 + \Delta^2}{2r}$ IN THE LIMIT AS TITE, A - O. THEN $\frac{L_{5}-L_{3}}{L_{5}-L_{3}}=\frac{5}{3}L$ $=\frac{2}{3}\times\frac{5}{7}\left(L^{1}+L^{2}\right)$ SO THAT Y = 3 + 3 ((1 + 12) COSA OR Y = 2(1,+12) COSK WHICH AGREES WITH ED. (1). 5.19 GIVEN: PLANE AREA FIND: Y 1 3 b2h 2 えりり 5 2 (p1+p2)H 1亡(251+62)か THEN YEA = SGA USING FIG. S.BB, Y OF AN ARC OF RADIUS $\frac{\nabla \left[\frac{1}{2}(b_1+b_2)h\right] = \frac{1}{6}(2b_1+b_2)h^2}{OR} = \frac{2b_1+b_2}{b_1+b_2} \frac{h}{3}$

60 mm {



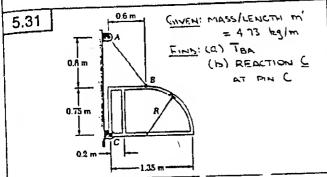


X=18.45 IN. 78L=5 21

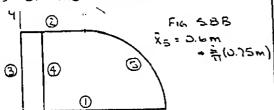


5.30 CONTINUED

THEN $\bar{X} \Sigma L = \Sigma \bar{x} L$ $\bar{X}(227.38) = -320$ $\Box R \quad \bar{X} = -1.407 \text{ in.}$ $\bar{Y} \Sigma L = \Sigma \bar{y} L$ $\bar{Y}(227.38) = 3464.1$ $\Box R \quad \bar{Y} = 15.23 \text{ in.}$



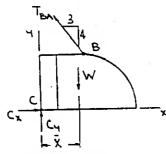
FIRST NOTE THAT BECAME THE FRAME IS
FABRICATED FROM UNIFORM BAR STAK, ITS
CENTER OF CRAVITY WILL COINCIDE WITH THE
CENTROID OF THE CORRESPONDING LINE.



١	L.m 1	\bar{x}, m	TL. m3
ī	1.35	3.675	0.911 25
2	ما.ن	۵.3	018
3	ა. 15	O	2
4	0.15	0.2	0.15
5	3 (0.75) = 1.17B10	1.07746	1.26336
Σ	4.628 10	_	2 5106

THEN XZL = ZXL X (4.22810) = 2 5106 OR X = 0 542 47 m

THE FREE-BODY DIAGRAM OF THE FRAME IS



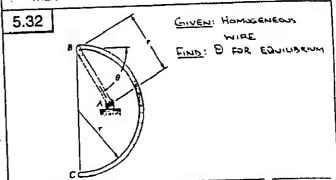
WHERE W = (m' [L) 9 = 4.73 kg/m * 4.628 10 m * 9.81 52 = 214.75 N

EQUILIBRIUM THEN REQUIRES -. (LONTINUES)

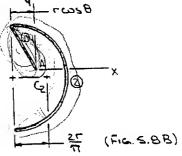
5.31 CONTINUED

(a) EM=0: (1.55m)(3TBA) -(0.54247m)(214.75N)=0 OR TBA=125.264N OR TBA=125.3N

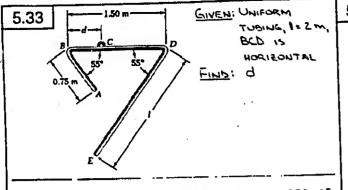
(b) $\Sigma F_{x} = 0$: $C_{x} = \frac{3}{3}(125.264 \text{ N}) = 0$ or $C_{x} = 75.158 \text{ N} - \frac{4}{3}(125.264 \text{ N}) - (214.75 \text{ N}) = 0$ $\Sigma F_{y} = 0$: $C_{y} + \frac{4}{3}(125.264 \text{ N}) - (214.75 \text{ N}) = 0$ $\Sigma F_{y} = 0$: $C_{y} + \frac{4}{3}(125.264 \text{ N}) - (214.75 \text{ N}) = 0$ THEN... $C_{x} = 137.0 \text{ N} \triangle 56.7^{\circ}$



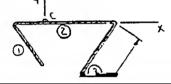
FIRST NOTE THAT FOR EQUILIBRIUM, THE CENTER OF GRANTY OF THE WIRE MUST LIE ON A VERTICAL LINE THROUGH A. FURTHER, BECAUSE THE WIRE IS HOMOGENEDUS, IT'S CENTER OF GRANTY WILL CONCIDE WITH THE CENTRON OF THE CORRESPONDING LINE. THUS,



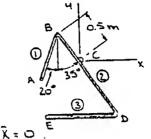
 $\begin{array}{ccc}
\overline{X} = 0 \\
\hline
1 & & & & & \\
\hline
0 & & & \\
\hline
0 & &$



FIRST NOTE THAT FOR EQUILIBRIUM, THE CENTER OF GRAVITY OF THE COMPONENT MUST LIE ON A VERTICAL LINE THROUGH (. FURTHER, BECAUSE THE TUBBLE IS UNIFORM, THE CENTER OF GRAVITY OF THE COMPONENT INILL CONCIDE WITH THE CENTRALD OF THE CORRESPONDING UNE. THUS,



5.34 CONTINUED



 $\begin{array}{lll}
\lambda = U & \\
\sum \sum \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{j=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{i=0}^{K-1} \sum_{j=0}^{K-1} \sum_{j=0$

OR - 0.096 193 + (510 35 - 1)1 = 0

This equation implies that the center of gravity of DE must be to the right of C. Then... $1^2 - 1.147151 + 0.192386 = 0$

or $0.14715 \pm \sqrt{(-1.14715)^2 - 4(0.192386)}$

5.35

-- 54

NOTE ALLEP

(62)

(4)

<u>5.34</u>

KE.

5.35 and 5.36 CONTINUED

SIMPLIFYING EQ. (2) YIELDS -- &h2-2ah+a2 = 0

THEN h = = = 1(-2a)2-4(k)(a2)

= = = [1 + (1-R)

MOTE THAT ONLY THE NEGATIVE ROOT IS ACCEPTABLE SINCE TY Q. THEN...

h= 0.10 [1- (1-010]

or h=0.513a ◀

(b) k=0.80 h= 0.80 [1- VI-080]

DR H= D. 691a

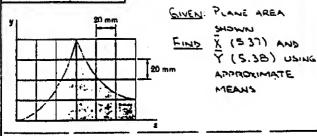
5.36 Show: Y=3h FOR THE VALUE OF h WHICH MAXIMIZES Y

REARRANGING EQ. (2) (WHICH DEFINES THE VALUE OF h WHICH MAXIMIZES Y) YIELDS $a^2 + kh^2 = 2h(a-kh)$

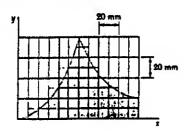
THEN SUBSTITUTING INTO EQ. (1) (WHICH DEFINES Y)... $Y = \frac{1}{3(\alpha-kh)}, 2h(\alpha-kh)$

02 7 + 3 h

5.37 and 5.38



THE AREA IS FIRST DIVISED INTO TWELVE VERTICAL STRIPS, EACH 10 MM WINE, AND THEN THE AREA :AND THE LOCATION OF THE CENTROD ARE APPROXIMATED FOR EACH STRIP. A 10+10-MM GRID IS USED TO EACILITATE APPROXIMATING THE VALUES.



(CONTINUED)

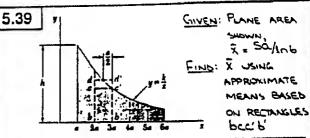
5.37 and 5.38 CONTINUED

47013	A, mm2	¥. mm	[4, mm]	EA. mm3	4K.mm3
1	15	7	١	105	15
2	45	12	3	1040	195
3	150	2.6	7	3900	1050
4	250	34	14	9000	3500
	4-00	47	2.1	18 800	8400
	450	รา	33	37 050	21450
<u>با</u>	700	<u></u>	36	44 100	25 200
8	525	74	27	38 480	14 040
0	390	83	18	32 370	7020
	295	94	15	27 730	4425
10		104	12	24940	C885
11	240	113	111	23730	2310
12 E	3992	1,13	Ì	261 265	90 485

5.37 HAVE .. XXA = ZXA X(3885) = 261 265

OR X = 67.2 mm

5.38 HAVE . YEA = EAA
Y(3885) = 90485
OR Y = 23.3 mm

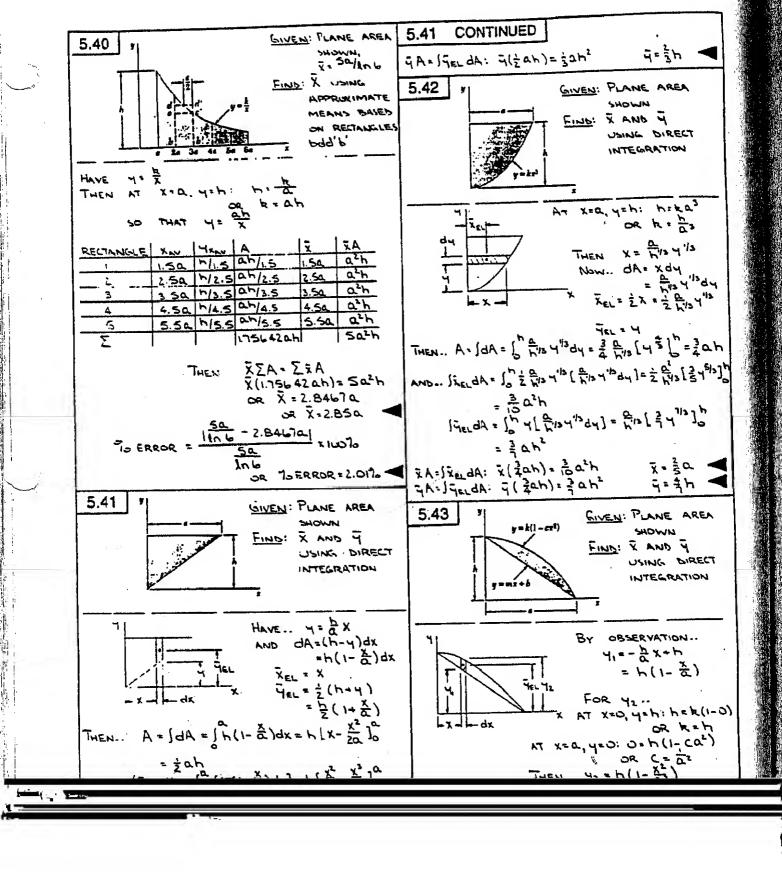


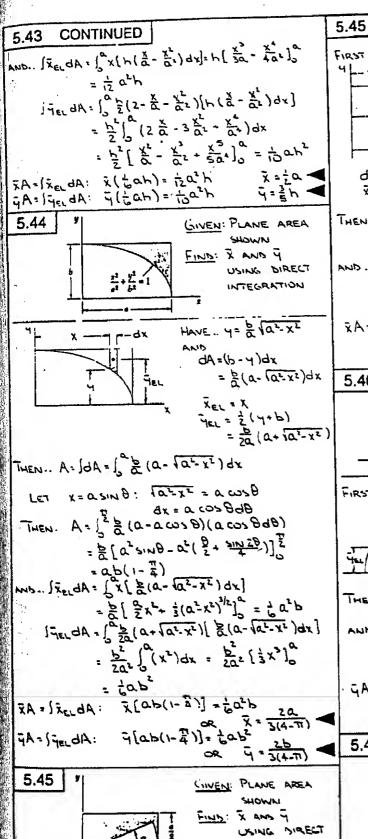
HAVE $Y = \frac{R}{X}$ THEN AT $X = \alpha$, Y = h: $h = \frac{R}{\alpha}$ SO THAT $Y = \frac{\alpha h}{X}$

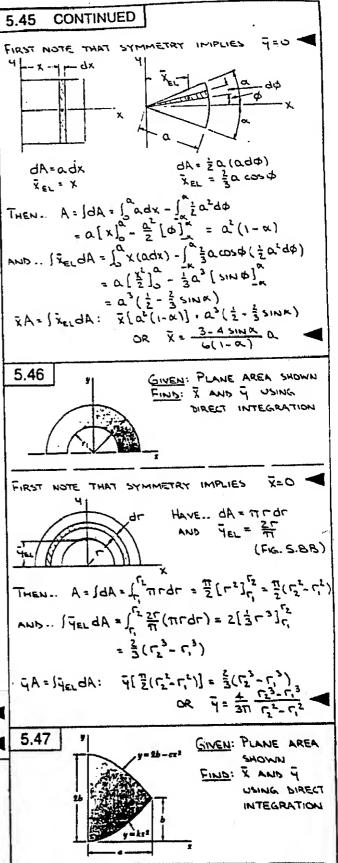
RECTANGLE	1 x 2	1 42	IA I	x	<u></u> χΑ
1120111200	2a	11/2	an/2	1.50	0.75a2h_
7	30	h/3	ah/3	2.50	0.833Q2H
3	40.	h/4	an/4	3.50	0.875a2h
	50	his	ah/s	4.50	3.9a2h
	La	7/6	anle	5.50	0.917a2h
5	-	1.0	1.45ah		4.275 a2h

70 ERROR = 1907 - 2.949301 - 1007.

OR 7. ERROR = 5.65%







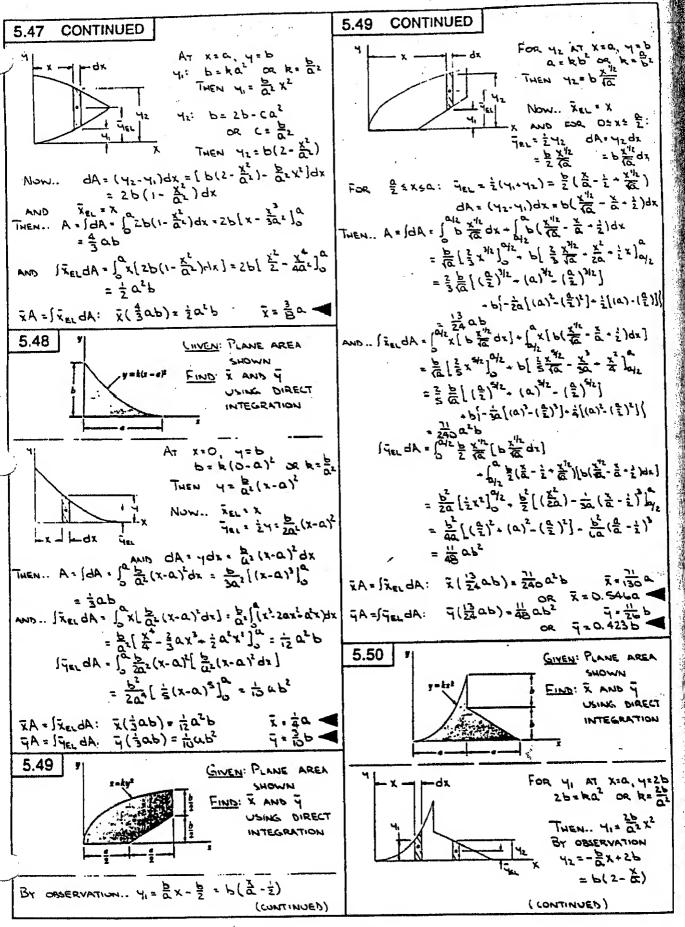
FIRST NOTE THAT SYMMETRY IMPLIES

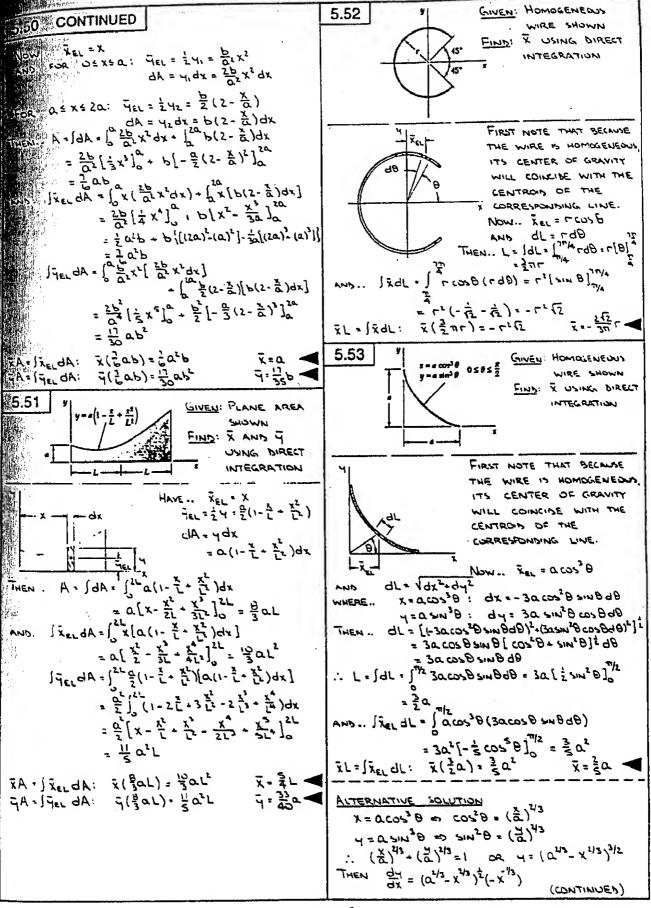
4=4

(CONTINUED)

INTEGRATION

(CONTINUED)



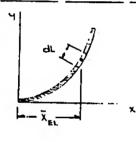


5.53 CONTINUED

Now. $\bar{x}_{\epsilon_L} = x$ AND $dL = \sqrt{1 + \left(\frac{dx}{dx}\right)^2} dx = \left(1 + \left(\alpha^{43} - x^{43}\right)^{1/2} \left(-x^{-1/3}\right)^2\right)^{1/2} dx$ THEN.. L = $\int dL = \int_{0}^{\infty} \frac{\chi^{1/3}}{\chi^{1/3}} dx = \alpha^{1/3} \left(\frac{3}{2} \chi^{3/3} \right)_{0}^{\alpha} = \frac{3}{2} \alpha$ AND .. | Xeldl = | x (213 dx) = 213 (3 x 5/3) = 302 xL= |xeLdL. x(2a)= 3a2

* 5.54 | 1

GIVEN: HOMOGENEOUS WIRE SHOWN FIND: X USING DIRECT INTEGRATION



FIRST NOTE THAT BECAUSE THE WIRE IS HOMOGENEOUS ITS CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING LINE.

HAVE AT X=Q, Y=Q Q=kQ32 OR k= 100 THEN Y= 100 X312 AND dx = 3 x 12

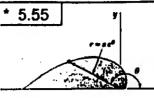
Now.. dL = \1+(\frac{dx}{2})^2 dx = \[1+(\frac{3}{2}\omega x'12)^2\]^{1/2} dx AND .

= 20 140+9x dx THEN.. L= |dL= | 20 140+9x dx $= \frac{2}{2(\overline{\alpha})} \left[\frac{1}{5} x \dot{q} (4\alpha + 9x)^{3/2} \right]_{\alpha}^{\alpha} = \frac{\alpha}{27} \left[(13)^{3/2} - B \right]$

= 1.43971Q AND. JREL dL = Jax[210 (40.9xdx]

UE INTEGRATION BY PARTS WITH U=X dV = 140.49xdx 15 = 3 (40+9x)3/2 du .dx THEN .. | XEL dL = 210 | [X - 27 (40+9x) 3/2] $= \frac{\left(13\right)^{\frac{1}{12}}}{27} \alpha^{2} - \frac{\int_{0.27}^{2} (4\alpha + 9x)^{\frac{1}{12}} dx}{\left(\frac{2}{45} (4\alpha + 9x)^{\frac{1}{12}}\right)^{\frac{1}{12}}} \alpha^{\frac{1}{12}}$ $= \frac{\Omega^2}{27} \left\{ (13)^{3/2} - \frac{2}{45} \left[(13)^{3/2} - 32 \right] \right\}$

* 0.785 46 a2 XL= | XEL dL: X (1.439 71 a) = 0.785 66 a2 OR X = 0.546a -



GIVEN: PLANE AREA SHOWN'

FIND: X AND & USING DIRECT

INTEGRATION

HAVE .. XEL : 3 T COSB AND dh = 3. F. FdB

THEN.. A: $|dA \cdot \int_{0}^{\infty} \dot{z} \, \alpha^{2} e^{2\theta} d\theta \cdot \dot{z} \, \alpha^{2} \left[\dot{z} \, e^{2\theta} \right]_{0}^{\infty}$ $= \dot{z} \, \alpha^{2} \left(e^{2\pi} - 1 \right) = 133.423 \, \alpha^{2}$

AND $\int \bar{x}_{EL} dA = \int_{0}^{\pi} \frac{1}{2} \alpha e^{\theta} \cos \theta \left(\frac{1}{2} \alpha^{2} e^{2\theta} d\theta \right)$ = 3 a3 [e 30 cos 8 d8

Use INTEGRATION BY PLATS WITH Use 38 du costo

U=0³0 du=co>0d0

du=30³0 d0 du=sin0

Then: ∫0³⁰co>0 d0 = 0³⁰ sin0 -∫sin0(30³⁰d0)

Now LET U=0³0 du=sin0d0

THEN. \230 COS DOO = 238 COS D -)(-65/35/80-)[-SO THAT $\int_{0}^{2\theta} \cos\theta d\theta = \frac{29\theta}{10} (\sin\theta + 3\cos\theta)$

1. | \$ x = L dA = \frac{1}{3} a 3 \ \frac{0.00}{10} (SNU \text{0.4.3 cos \text{0}} \]_{\text{0.5}}^{\text{7}} $=\frac{\alpha^3}{30}\left(-3e^{3\pi}-3\right)=-1239.26\alpha^3$

ALSO. I FEL dA = 1 3 200 SINB (202028 dB) = 1 03 (" c 30 SINB dB

USE INTEGRATION BY PARTS WITH GD = SINB dB

THEN .. $\int e^{3\theta} \sin \theta d\theta = e^{3\theta} \cos \theta - \int (-\cos \theta)(3e^{3\theta} d\theta)$ Now LET $u = e^{3\theta} \cos \theta - \int (-\cos \theta)(3e^{3\theta} d\theta)$

THEN .. 1 & 30 SIN Odb = - & 30 COSD + 3[& 30 SIN O

[(Bb sexBur)] (8 mis & + 8 co -) = 868 mis es

XA = 1XELdA: X(133.623 a2) = - 1239.26 a3

44 = JackdA: 4 (133.623 a2) = 413.09 a3 OR 4=309a = 5.56 Signal Sign

CONTINUED 5.59

AREA = 27 (9262+ 9363+ 9464) = 271 [(22.5)(45) + (45)(72)+(22.5)((272.452)] OR AREA = 34.1 10 mm2

(b) ROTATION ABOUT THE LINE X+12 MM: VOLUME = 271(12- XAREA)A = 271(12A- ZTA) = 277 (C72 mm X2632.5 mm2) - (111 172.5 mm3)]

OR VOLUME = 492 (103 mm3

AREA = 271 X LINE L = 271 EIRLINE)L

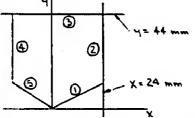
 $= 2\pi \left(\tilde{X}_1 L_1 + \tilde{X}_3 L_3 + \tilde{X}_4 L_4 \right)$ WHERE \tilde{X}_1 , \tilde{X}_3 , AND \tilde{X}_4 ARE MEASURES WITH RESPECT TO THE LINE X: 72 MM. THEN AREA = 271 [(22.5)(45)+(36)(72)

+ (42+15) (515+425)]

OR AREA = 41.9 x 10 mm2

5.60 GIVEN: PLIME AREA SHOWN FIND: YOU'ME AND WREALE AREA OF SOLIS OBTAINED BY ROTATING THE AREA rear (a) THE LINE 4 + + + + (b) THE LINE X=24 MM

FROM THE SOLUTION TO PRUBLEM 5.5 HAVE A = 1536 mm2 E x A : 4536 mm E4A = 39 648 mm3



Applying the theorems of Papous Gulbinus have (a) ROTATION ABOUT THE LINE Y = 44 mm ?

VOLUME = 271 (44 - YAREA) A = 271 (44 A - ITA)

= 271 [(44 mm)(1596 mm²) - (39 648 mm²)]

OR VOLUME = 192.1 × 10 MM 4

AREA = 2TT YUNE L = 2TE (JUNE) L = 211 (4, 6, 4 7262 + 4464 + 4566)

WHERE YI, ... , YS ARE MEASURES WITH RESPECT TO THE LINE Y= 44 mm. THEN ..

AREA = 27 [(38) (242+122)+(16)(32)+(16)(32)

+ (38)((182+122)]

OR AREA = 18.01=10 mm

(b) ROTATION ABOUT THE LINE X=24 mm: VOLUME = 271 (24 · X)A = 271 (24A - ZXA)

= ZTI [(24 mm)(1596 mm2) - (4536 mm3)]

OR VOLUME = 212A10 mm3

AREA = 2TI X LINE L = 2TI E (IX CINE) L = 277 (x, L, - x 3 L 3 + x 4 L 4 + x 5 L 5)

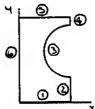
WHERE $\bar{x}_1, \dots, \bar{x}_5$ ARE MEASURES WITH RESPECT (CONITINUES)

5.60 CONTINUED

TO THE LINE X=24 mm. THEN .. AREA = 27 (12) (24 - 12) + (21)(42) + (42)(32) + (>3)((182+121)) OR AREA = 20.5 =103 mm2

5.61 GIVEN: PLANE AREA MUWN FIND: VOLUME AND SURFACE AREA OF SOUD OBTAINED BY ROTATING THE AREA **ABOUT** (a) THE X AXIS (b) THE 4 AXIS

FROM THE SOLUTION TO PROBLEM 5.7 HAVE ERA = 14 147.0 IN3 A=1146.57 IN2 EJA: 26 B97 INS



APPLYING THE THEOREMS OF PAPPUS- GULDINUS HAVE ...

(a) ROTATION ABOUT THE X AXIS:

VOLUME = $2\pi Y_{\text{max}}A = 2\pi \sum_{i} A = 2\pi (26 897 in^3)$ OR VOLUME = ILAO x 10 143

AREA = 277 Y LINE A = 277 E(GUNE)A = 271 (72 Lz + 73 Lz + 94 L4 + 95 L5 + 96 L6)

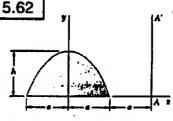
= 271 (7.5)(15)+(30)(71-15)+(47.5)(5) + (50)(30)+(25)(50)]

OR AREA - 28 4 MID IN

(b) RUTATION ABOUT THE Y AXIS: VOLUME = 271 XAREA A = 271 \(\hat{x} A = 271 (14 147.0 \) IN3) OR YOUME = 88.9 = 10 11 -

AREA = 271 XLINE L = 271 E(RUME)L = 27 (X, L, + X2 L2 + X2 L3 + X4 L4 + X & L5) = 27 (15)(30)+(30)(15)+ (30- 2015)(n-15) +(30)(5)+(15)(30)]

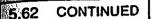
OR AREA = 15.4BAID IN .



A. GIVEN: PLANE PARABOLK AREA SHOWN FIND: VOLUME OF SOLID OBTAINED BY ROTATING THE AREA ABOUT (a) THE X AXIS (P) THE LINE AA

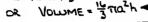
FIRST, FROM FIG. S. BA HAVE .. A= 30h 4 = 3 h APPLYING THE SECOND THEOREM OF PAPPUS-GULDINUS HAVE .. (a) ROTATION ABOUT THE X AXIS:

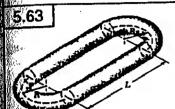
(CONTINUED)



VOLUME : 27 9 A = 27 (3h) (3ah) OR VOLUME = ISTIAL

(6) ROTATION ABOUT THE LINE AA': " VOLUME = 271(2a) (3ah)





(... d=6 mm, RELOWN, L=30 MM FIND: VOLUME V AND SURFACE AREA AL OF THE LINK

FIRST NOTE THAT THE AREA A AND THE CIRCUMFERENCE C OF THE CROSS SECTION OF HE BAR ARE

A = Td2 br = 2

DISSERVING THAT THE SEMICIRCULAR ENDS OF THE LINK CAN BE OBTAINED BY ROTATING THE CRUSS SECTION THROUGH A HORIZONTAL SEMICIRCULAR ARC OF RADIUS R. THEN, APPLYING THE THEOREMS OF PAPPUS GULSINUS HAVE .

V= 2 (VSIDE) + 2 (VEW) VOLUME: = 2(AL)+2(TRA) = 2(L+TR)A = [2[(30 mm)+7 (10 mm)]]] (6 mm)2] OR V=3470 mm3

A = 2 (A S.BE) + 2 (A END) = 2 (CL) + 2 (ARC) = 2 (L+AR)C [(mm d) T] [(mm C1) n+ (mm OE)] S =

OR A = 2320 mm2

5.64

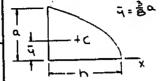
AREA .

GIVEN: FIRST FOUR SHAPES OF FIG. 5.21 FIND VOLUME OF EACH SHAPE

SECOND THEOREM OF PAPPUL Following

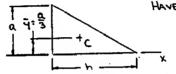
CONTINUED 5.64

(3) PARABOLOID OF REVOLUTION: THE GENERATING AREA IS A DUARTER PARABOLA



HAVE . V = 277 4 A = 211 (3a) (3ah) OR V. ZTIQ2h ◀

(4) CONE : THE GENERATING AREA IS A TRIANGLE



HAVE. V= 279 A = 271 (3)(2 ha) OR V-ina2h

5.65

GIVEN: COUNTERSUNK HOLE SHUWN FIND: VOLUME OF STEEL

REMOVED WAINS COUNTERSINKING PROCESS

THE REQUIRED VOLUME CAN BE GENERATED BY ROTATING THE AREA SHOWN ABOUT THE 4 AXIS APPLYING THE SECOND THEOREM OF PAPPUS-GULDINUS HAVE ..



V= 271 x A = 277[] + j(4)]IN. $\sqrt{\left(\frac{1}{2} \times \frac{1}{4} \ln \ln \times \frac{1}{4} \ln \ln \right)}$ OR V=0.0900 in3

ALL DIMENSIONS ARE IN INCHES

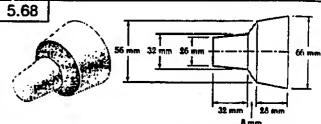
5.66

5.66 CONTINUED IS GIVEN BY_ Ac = TYL + TEAL WHERE THE INDIVIDUAL LENGTHS ARE THE LENGTHS OF THE BELT CROSS SECTION WHICH ARE IN CONTACT WITH THE PULLEY. HAVE .. Ac = TI (2 (], L,) + 92 22] = n [2(3- 2125)(3.125) + (3-0.125)(0.625)] A = 8.10 IN2 HAVE .. A = 71[2(9, L,)] = 277 (3-0.08-0.375) · (cos 50.) Ac=6.851N2 (C) 一篇 (Fig. 5.88) HAVE .. A = T (J. L.) = 3 (3 - 2 - 2) * (71 - 0.25) CR A = 7.01 IN2 4 5.67 GIVEN: BOWL SHOWN, K = 250 mm FIND: VOLUME V IN LITERS

THE VULUME CAN BE GENERATED BY ROTATING THE TRIANGLE AND CIRCULAR SECTOR SHOWN ABOUT THE Y AXIS APPLYING THE SECOND - THEOREM OF PAPERS-GULDINUS AND USING 3 FIG. 5.BA, HAVE.. 0 (CONTINUED)

CONTINUED 5.67

 $V = 2\pi \bar{X} A = 2\pi \sum_{x} A = 2\pi (\bar{x}_{x} A_{x} + \bar{x}_{x} A_{x})$ $= 2\pi \left[\left(\frac{1}{3} * \frac{1}{2} R \right) \left(\frac{1}{2} * \frac{1}{2} R * \frac{13}{2} R \right) + \left(\frac{2R \times 1030}{30} \cos 30^{\circ} \right) \left(\frac{\pi}{6} R^{2} \right) \right]$ $= 2\pi \left(\frac{R^{3}}{16 (3)} + \frac{R^{3}}{2(3)} \right) = \frac{3(3)}{16} \pi R^{3}$ = $\frac{36}{8}\pi (0.25 \text{ m})^3 = 0.031883 \text{ m}^3 \cdot \frac{10^31}{1 \text{ m}^3}$ OR V=31.9 9 4



GIVEN: LAMP SHADE SHOWN, DENSITY P . 2800 M. THICKNESS L = 1 mm

FIND MASS M

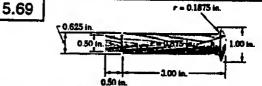
THE MASS OF THE SHADE IS GIVEN BY m=pV=pAt WHERE A IS THE SURFACE AREA OF THE SHADE. THIS AREA CAN BE GENERATED BY ROTATING THE LINE SHOWN ABOUT THE X AXIS. APPLYING THE FIRST THEOREM OF PAPPUS-GULDINA

 $A = 2\pi \overline{Y} L = 2\pi \overline{Z} \overline{q} L = 2\pi (\overline{q}_1 L_1 + \overline{q}_2 L_2 + \overline{q}_3 L_3 + \overline{q}_4 L_4)$ $= 2\pi \left[(\frac{13}{2})(13) + (\frac{13+16}{2})(\overline{432^2 + 3^2}) \right]$ + (16+28)((B2+122)+(28+33)((282+52))

= 271 (1735.33 mm2)

THEN .. M = 2800 m = [271(1735,33mm2)] = 1 mm = 10 mm

DR m = 0.0305 kg €



GIVEN: 20,000 PEGS HAVING SHAPE SHOWN, 2 COATS OF PAINT, I GALLON PAINT / 100 HL

FIND: NUMBER OF GALLONS NEEDED

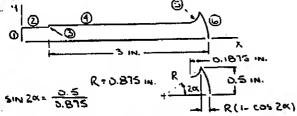
THE NUMBER OF GALLONS OF PAINT NEEDED IS GIVEN BY

NUMBER OF GALLOUS . (NUMBER OF PEGS)GURFACE AREA OF 1 PEG/ 100 (E) (ETMOD S)

(CONTINUED)

5.69 CONTINUED

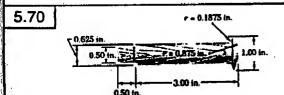
OR NUMBER OF CALLONS & 400 As (As - \$t^2)
WHERE AS IS THE SURFACE AREA OF ONE PEC.
A. CAN BE GENERATED BY ROTATING THE LINE
SHOWN ABOUT THE X AXIS. USING THE EIRST
THEOREM OF PAPPUS - GULDINUS AND FIG. 5.88,
WAVE --



100	As = 27 YL = 27 Eq	L	
à l	L, IN	9.10.	4L, 102
4	0.25	0.125	0.03125
,	0.5	0.25	0.125
4	J.0625	052+02152=75BIS2	0.0175781
4	? -0.875(1-c0534.850) -0.1275 = 2.6556	0.3125	o.829 88
5	2 · 01875 - 5.294 52	3.5 - <u>2-0.18)5</u> - 0.380 63	CO1 511.0
٥	Za(0.875)	0.875 3IN 17.425"	2.137314
	L		•

ZqL=1.25312 m² THEN.. As = 271 (1.25312 IN²)= 144 m2 = 0.054678 ft²

FINALLY.. NUMBER OF GALLONS 4000 0.054678 = 21.87 GALLONS
ORDER 22 GALLONS



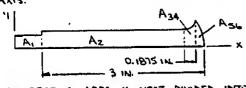
GIVEN: PEG HAVING THE SHAPE SHOWN, INITIAL

SIZE OF DOWEL .. I IN. DIA. * 4 IN. LONG

FIND: PERCENT (VOLUME) OF DOWEL THAT

BECOMES WASTE

TO CARTAIN THE SOLUTION IT IS FIRST NECESSARY TO DETERMINE THE VOLUME OF THE PEG. THAT VOLUME CAN BE GENERATED BY ROTATING THE AREA SHOWN ABOUT THE X AXIS.



THE GENERATING AREA IS NEXT DIVIDED INTO SIX

5.70 CONTINUED

OSM. AS INDICATED.

AS A4 REAL PROPERTY ALL PROPERTY ALL

OR ZX = 34.850° X = 17.425°

I PPLYING THE SECOND THEOREM OF PAPPUSGULDINUS AND THEN USING FIG. S.BA, HAVE...

عا	COLUMNS AND THEM STATE		
١	A, IN2 VARG = 271 YA = 271 EGA	9, 10.	9A,1N3
٠l	3510.25.0.125	0.125	0.05-25
2	[3-0.875(1-cos.34.850)-0.1875] ~ (0.3125) = 0.829 87	0.15625	0.129667
7	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	0.25	7053438
4	-\$(0.1815) =-0.051615	0.5- 4x0.1815	-0.011CA
		= 0.42042 2= 0.875 34417.425	
5	a(0.815)2	300 4 SIN 17.425	0.04005
_ _	¿(0.875 cos34.850°)(0.5°)	3(0.5)	-0.029920
	= -0.179517	-0.1666	
-	7-1	- 5 5 752 3	

EqL = 0.167 252 IN3
THEN .. VAGE = 271 (0.167252 IN3) = 1.05088 IN3

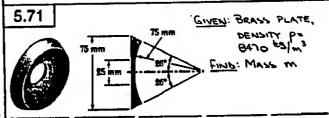
Now .. VDOWEL = 7 (BIAMETER) (LENGTH) = 7 (1 111.) (4 111.)

THEN .. YOWASTE = VENEL = 10070

= VENEL - VPEC = 10070

VENEL = (1- 1.05088) × 10070

OR TO WASTE . LL. 5%



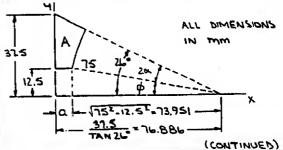
THE MASS OF THE ESCUTCHEON IS GIVEN BY

IN = PV

WHERE V IS THE VOLUME OF THE PLATE. V CAN
BE GENERATED BY ROTATING THE AREA A

ABOUT THE X AXIS.

Y

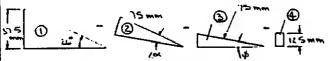


5.71 CONTINUED

HAVE.. $\alpha = 76.886 - 73.951 = 2.935 \text{ mm}$ AND.. $\sin \phi = \frac{12.5}{2.5} \implies \phi = 9.5941$

THEN 2x = 26 - 9.5941 = 16.4059

THE AREA A CAN BE OSTAINED BY COMBINED THE FOLLOWING FOUR AREAS AS INDICATED.

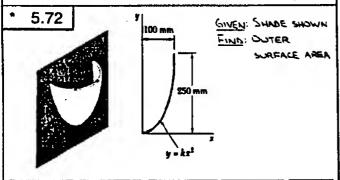


APPLYING THE SECOND THEOREM OF PAPENS.
GULDINUS AND THEN USING FIG. S.BA, HAVE...
V = 271 YA = 271 Z G A

1	A. mm2	14 · 211 24 A	9A, mm 3
1	2×76.286×37.5	\$(37.5) + 12.5	E1.050 BI
2	-K(75)2	2(75) SIN B. 203, SIN (B. 203-95Mi)	-12 245.30
3	- 2.73.951 × 12.5	当(12.5)・4.1しい	- 1925.81
4	- 2.935 + 12 5 = - 36, 688	±(12.5) = 6.25	- 229.30
_			

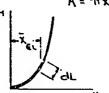
EqA = 3599.72 mm ? THEN . V = 27 (3599.72 mm) = 22 617.7 mm? m = 8470 22 . 22 617.7 mm? M = 0.1916 22 617.7 mm?

OR M= 191.69 4



FIRST NOTE THAT THE REDURED SURFACE AREA A CAN BE GENERATED BY ROTATING THE PARABOLK CROSS SECTION THROUGH TI RADIANS ABOUT THE Y AXIS APPLYING THE FIRST THEOREM OF PAPPUS GULDINUS HAVE

A = TIRL



Now.. AT x = 100 mm, y = 250 mm
250 = k(100)2

OR RED.UZS mm

WHERE $\frac{dy}{dt} = 2kx$

THEN. $dL = \sqrt{1+4k^2x^2} dx$ HAVE. $\bar{x}L = \sqrt{x_{EL}} dL = \sqrt{x_{EL}} \sqrt{(1+4k^2x^2)} dx$

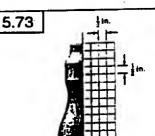
5.72 CONTINUED

 $\overline{\chi} = \left[\frac{1}{3} \frac{1}{4 \pi^2} \left(1 + 4 \pi^2 \chi^2 \right)^{3/2} \right]_0^{100}$ $= \frac{1}{12} \frac{1}{(0.025)^2} \left\{ \left(1 + 4(0.025)^2 (100)^2 \right)^{3/2} - (1)^{3/2} \right\}$

= 17 543.3 mm2

FINALLY ... A = TT (17 543.3 mm2)

OR A = 55.1 x10 mm2



GIVEN: BOTTLE DE CROSS SECTION SHOWN, W = 0.131 lb,SPECIFIC WEIGHT $<math>X = 59.0 \text{ lb/ft}^3$

FIND: AVERAGE WALL THICKNESS &

THE WEIGHT OF THE BOTTLE IS GIVEN BY

WERE AS IS THE SURFACE AREA OF THE
BOTTLE. AS CAN BE GENERATED BY ROTATING

THE CURVE BOWDING THE CROSS SECTION ABOUT

THE VERTICAL AXIS OF SYMMETRY.

APPROXIMATING THE PORTION OF THIS CURVE

TO THE RIGHT OF THE VERTICAL AXIS WITH A

SERIES OF SHORT, STRAIGHT LINE SEGMENTS

AND THEN APPROXIMATING THE LENGTH AND

THE VALUE OF X FOR EACH SEGMENT

USING THE GIVEN GRID, AS IS THEN

DETERMINED USING THE FIRST THEOREM OF

PAPPUS - GULDNUS.

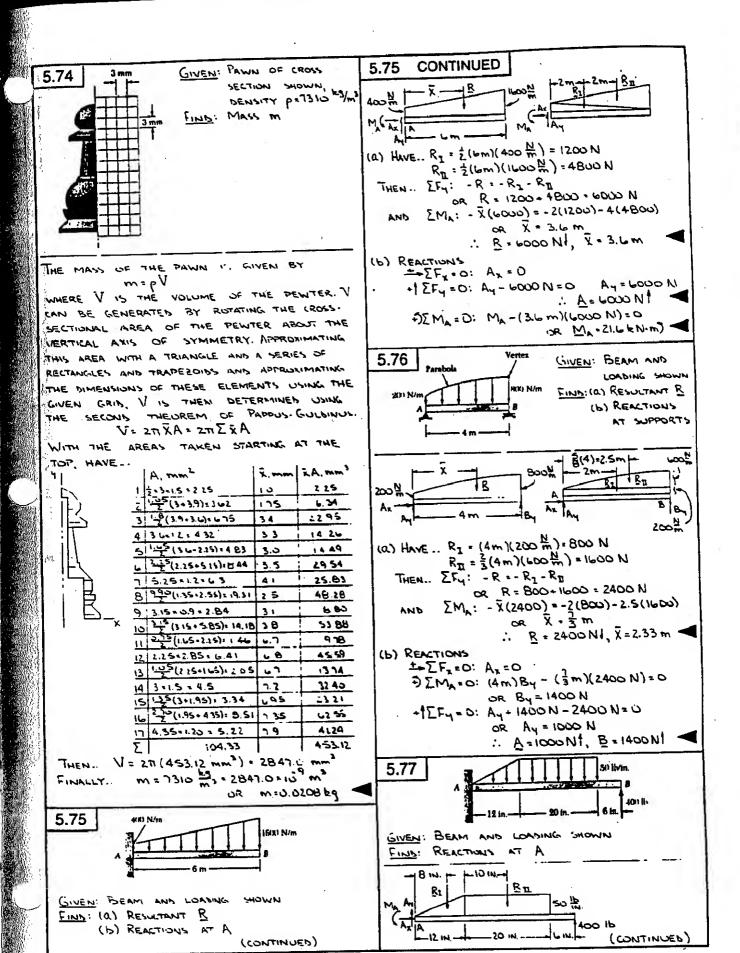
A, = 271 XL = 271 ExL

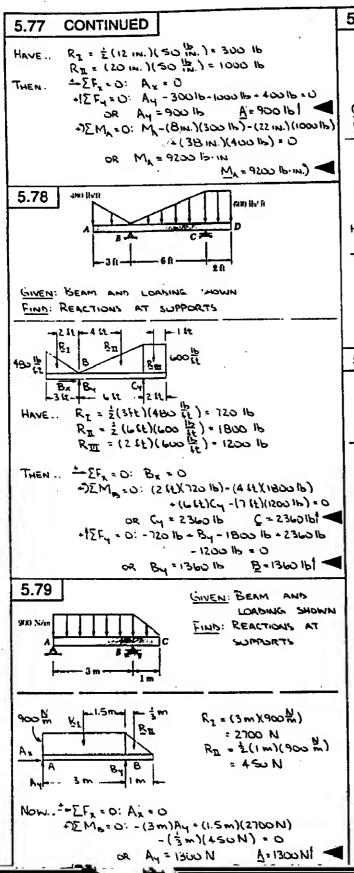
WITH THE ELEVEN SEGMENTS NUMBERED

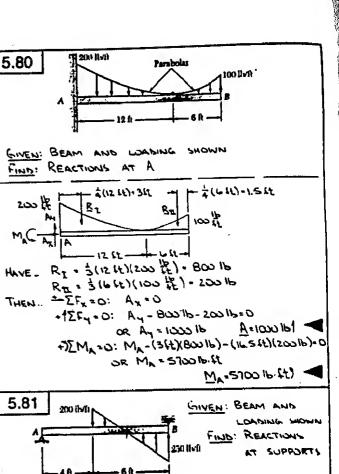
<u></u> 5π	ARTING	TA .	THE .	TOP, HAVE
Γl		L, 1N.	X, IN.	KL, IN2
1 }	1	عاد.ن	D.38	0.2888
ا لو إ	2	0.48	ع1.0	0.3448
i I	3	ა.98	3.98	J. 8624
1	4	1.06	1.20	1.272
/	5	ა.36	1.08	<u>6888.c</u>
!	L	1.12	89.0	1.0976
	7	I-7B	1.32	2.3496
1 +	В	2.50	بياماءا	4.15
<u></u>	9	1.12	1.74	1.9488_
ļ, —	X 10	3.48	1.68	0.8064
	11	1.56	3.7B	1.2168
	Σ			14.7460

THEN .. As = 27 (14.7460 IN2) = 92.652 IN2

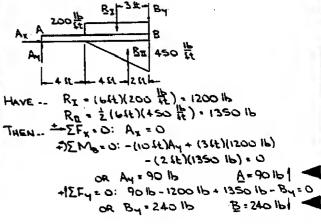
FINALLY.. 0.131 16 = 59.0 16 = 92.652 1N2 (12 11) t OR t=0.0414 IN.

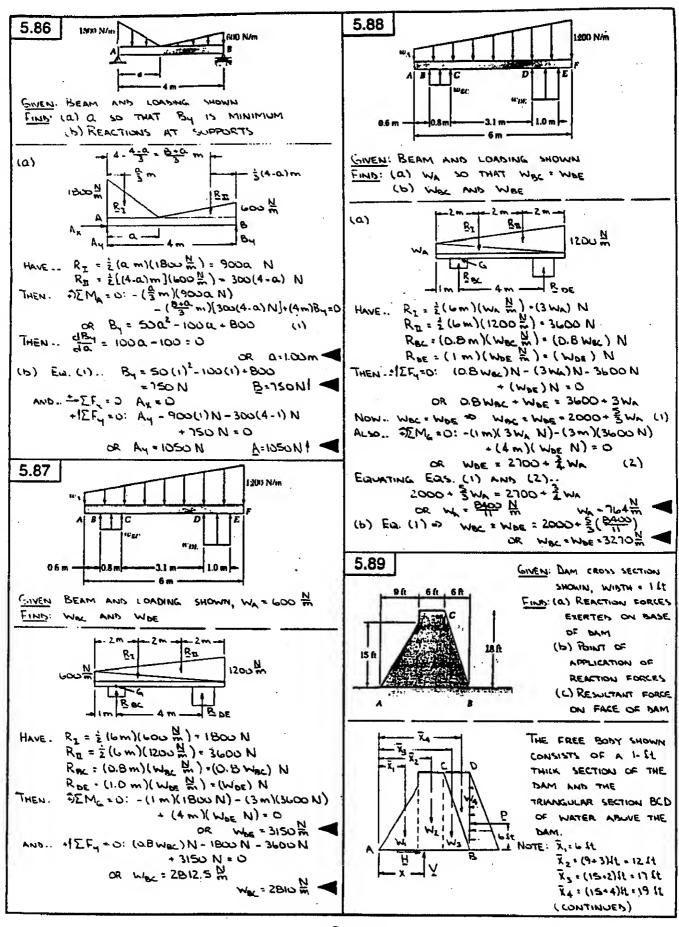


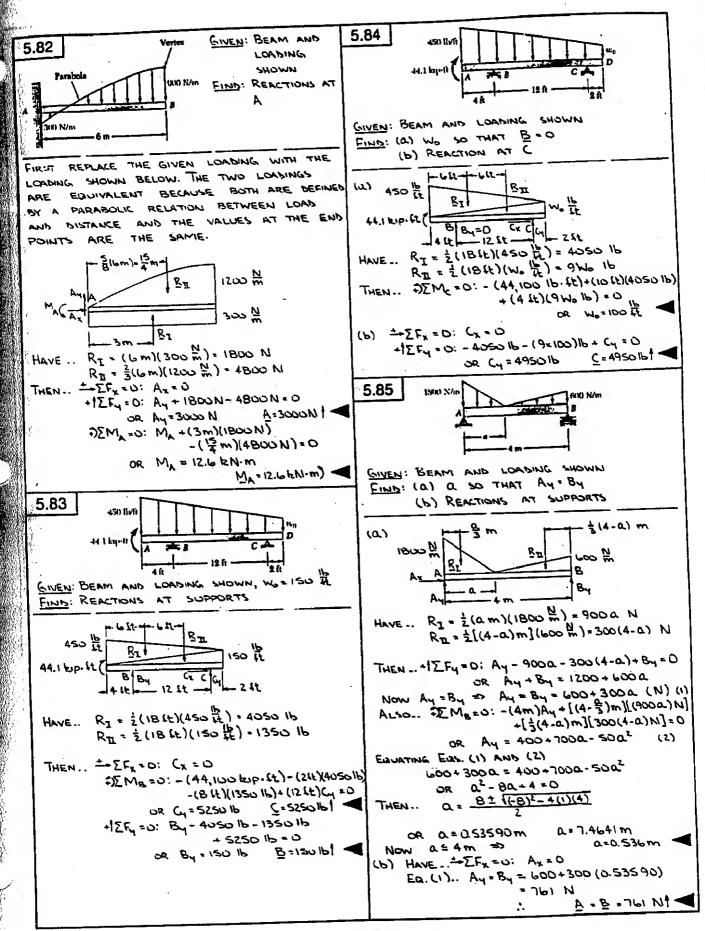




FIRST REPLACE THE GIVEN LOADING WITH THE LOADING SHOWN BELOW. THE TWO LOADINGS ARE EQUIVALENT BECAUSE BOTH ARE DEFINED BY A LINEAR RELATION BETWEEN LOAD AND DISTANCE AND THE VALUES AT THE END POINTS ARE THE SAME.









(a) Now.. W = 8V SO THAT $||h||_1 = (150 ||f|_2)|_2^2 (9 \text{ tr})(15 \text{ tr})(11 \text{ tr})|_2 = 10, 125 \text{ lb}$ $||h||_1 = (150 ||f|_2)|_2^2 (9 \text{ tr})(15 \text{ tr})(11 \text{ tr})|_2 = 10, 125 \text{ lb}$ $||h||_2 = (150 ||f|_2)|_2^2 (|h|_2)(11 \text{ tr})|_2 = 100 \text{ lb}$ $||h||_2 = (150 ||f|_2)|_2^2 (|h|_2)(11 \text{ tr})|_2 = 310.9 \text{ c} \text{ lb}$ $||h||_2 = (62.4 ||f|_2)|_2^2 (|h|_2)(11 \text{ tr})|_2 = 310.9 \text{ c} \text{ lb}$ $||h||_2 = 10, 109.9 \text{ lb}$

(b) HAVE.. \$\int N = 57,7946 | b \ \ \(\frac{1}{2}\) \(\frac{1}\) \(\frac{1}{2}\) \(\frac{1}{2

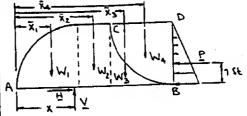
UR .. 37,794.6x - 60,750 - 194,400-137,700

OR X=10.48 ft

(C) LUNSINER WATER SECTION BCD AS THE FREE BODY

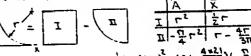
HAVE EF=0

5.90 CONTINUED



NOTE: $\bar{X}_1 = (21 - \frac{4 + 21}{377})$ ft = 12.0873 ft $\bar{X}_2 = (21 + 4)$ ft = 25 ft $\bar{X}_4 = (50 - \frac{4 + 21}{377})$ ft = 41.087 ft

FOR AREA 3 FIRST NOTE ..



THEN .. $\bar{\lambda}_3 = 29 LL + \left[\frac{\frac{1}{2}(21)(21)^2 + (21 - \frac{4*21}{377})(-\frac{7}{4}*21^2)}{(21)^2 - \frac{7}{4}(21)^2} \right] H$

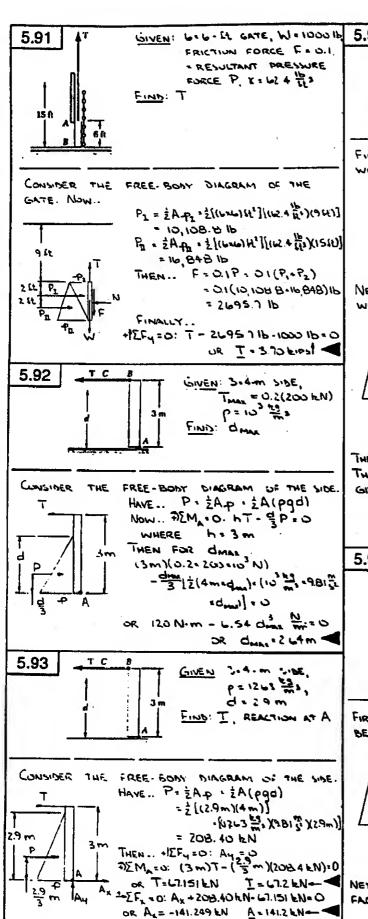
= (29 + 4.6907) \$2 - 33.691 \$2

(a) Now.. W = EV 30 THAT

W = (150 1/2)[2(21 LE) (1 LE)] = 51,954 16

W2 = (150 1/2) [(8 LE)(21 LE)(1 LE)] = 25,200 16

W2 = (150 1/2) [(8 LE)(21 LE)(1 LE)] = 25,200 16

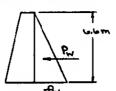




GIVEN: Po = 1.76x103 kg WIDTH's Im. dy = 2 m FIND: PERCENTAGE

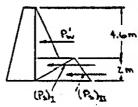
INCREASE OF FORCE ON DAM FACE BECAUSE OF SILT

FIRST DETERMINE THE FORCE ON THE DAM FACE WITHOUT THE SILT. HAVE ..



Pw = 2A-pw = 2A(pgh) = 2[(b.bm)(1m)] · [(10 3 kg)(9.81 50)(66 m)] = 213. LL KN

NEXT DETERMINE THE FORCE ON THE DAM FACE WITH THE SILT. HAVE ..



Pw = 2 [(4. hm)(1 m)] · [(10) 10 1 (9.8) (4.6 m)] = 103.79 EN (B) = 2[(2m)(1m)][(1.76-10) m] ·(3.BI] /(4.6m)] = 79.42 KN

(P3) = 2[(2m)(1m)][(1.76=10 m x (9.81 /2)(6.6 m)] +113.95 KN

THEN. P'= PW + (Ps), + (Ps), = 297.16 kN THE PERCENTAGE INCREASE TO INC. IS THEN GIVEN BY .. P'- Pw = 100% = (297.16-213.66) = 100.

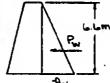
OR % INC. = 39.170



GIVEN: (FBASE) MAX = 1.2% FORCE OF WATER, Parlinenis kgs, WIDTH = I m. RATE IS AT WHICH SILT IS DEPOSITED = 12 mm/YEAR

FIND: NUMBER OF YEARS IN UNTIL DAM BECOMES UNSAFE

FIRST DETERMINE THE FORCE ON THE DAM FACE BEFORE MY SILT IS DEPOSITED HAVE ..



Pu = 2A + = 2A (pgh) = { ((6.6m)(1 m)} -{(10.6m)(1.81 cg)(6.6m)} = 213.66 kN

THE MAXIMUM ALLOWED FORCE PALLOW ON THE DAM IS THEN .. PALOW = 1.2 PW = 1.2 (213.66 kN) = 256.39 kN NEXT DETERMINE THE FORCE P' ON THE DAM FACE AFTER A DEPTH & OF SILT HAS SETTLED. . (CONTINUES)



P. = 2[(b.b-d)m. (1m)] · [(10 m;)(9.81 5 x x L b-d)m] (6.6-d)m = 4,905(6.6-d)2 kN · [(1.76 +10 m))(9.81 m) · (6.6-d)m] $(L^2)^{\mathrm{T}} - (L^2)^{\mathrm{D}}$ = 8.6328(6.6d-d2) KN (Ps) = 2 ((d) m = (1 m) (9.81 52) a (6.6 m) = 56.976 d kN

THEN P' = PW . + (Pa) I + (Pa) II = (4905(6.6-d)2+ 8.6328(6.6d-d2) + 56.976d] KN

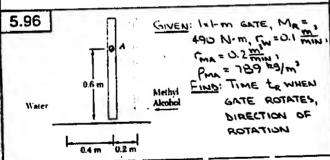
= (213.66 + 49.206d - 3.7278d2) kN NOW REDURE THAT P' = PALLOW TO DETERMINE THE MAXIMUM VALUE OF d.

: (213.66+49.206d-3.7278d2) kN=25639 kN 3.7278 d2 - 49.206d + 42.73 = 0

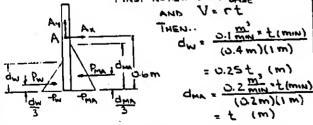
d = 49.206 = 1(-49.206)2-4(3.7278)(42.73) THEN .. 2 (3.7278)

d= 0.934 56 m AND d= 12.2652 m G= CN Now, deble m AND 0.934 56 m = 12 × 10 TEAR " N THEN

N = 77.9 YEARS



CONSIDER THE FREE-BODY DIAGRAM OF THE GATE. FIRST NOTE .. V = ABASE d AND Vert THEN



Now. P= 2Ap = 2A(pgh) 50 THAT
Pw = 2[(0.25t)m-(1m)][(10 m3 X9.B1 = X0.25t)m] = 306.56 th N

PML = 2[(+)m= (1m)][(789 mg)(9.81 mg)(+)m] = 3870t2 N

NOW ASSUME THAT THE GATE WILL ROTATE CLUCKWISE AND WHEN dMX & O. 6 M. WHEN (CONTINUED)

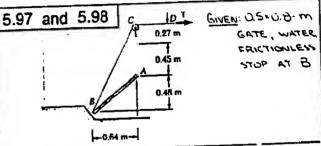
CONTINUED 5.96

ROTATION OF THE GATE IS IMPENDING, REQUIRE EMA: MR = (0.6m-3dm)PMA-(0.6m-3dw)Pw SUBSTITUTING .. 490 N·m = (0.6-3 t) m = (3870t2) N -(0.6-3-0.25t)m = (306 56 22)N SIMPLIFYING .. 1264.45 t3 - 2138.1 t2 + 490 = 0 SOLVING (POSITIVE ROOTS ONLY) .. t = 0.594 51 min AND t = 1.524 11 min

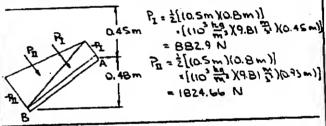
NOW CHECK ASSUMPTION USING THE SMALLER ROUT. HAVE ...

dma =(t)m = 0.59451 m < 0.6 m : t=0.594 SI min = 35.75

AND THE GATE ROTATES CHICKWISE



FIRST CONSIDER THE FORCE OF THE WATER ON P= 2Ap = 2A(pgh) so THAT. THE GATE. HAVE

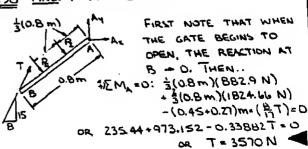


FIND: REACTIONS AT A AND B WHEN TO 5.97 FM P. SBB) (MB. D. 3 (0.8 m) (BB2.9 N) \$(0.8m) + 3(0.8 m)(1824.66 N) -(QBm)B=0 OR B = 1510.74 N

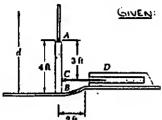
agm OR B = 1511 N 1 53.1" 12F = 0: A + 1510.74N - 882.9N - 1824.66 N = 0

OR A-1197 N A 53.1°

5.98 FIND: T TO OPEN GATE







GIVEN: 4.2- St GATE, K=BZB T. SPRING IS UNDEFORMED WHEN GATE IS VERTICAL WATER

FIRST DETERMINE THE FORCES EXERTES ON THE GATE BY THE SPRING AND THE

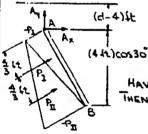
WATER WHEN B IS AT THE END OF THE

CYLINDRICAL PORTION OF THE FLOOR."

312

SIN B = 4 HAVE .. 0 = 30° Yop = (3 (t) TAN 30° THEN For = Rxsp AND = B28 1 . 3 H . TAN 30 = 1434,14 lb

Assume d= 4 St



HAVE .. P = 2A-P = 2A(Xh) THEN. Pz = 2[(+ ft)(2(t)]

·[(L2.4 片)(d-4)代] : 249.6(d-4) 1b

Pn = 2[(4 4)(26)] =[(4.4 [2)(d-4+4cos30)] = 249 6(d-0 53590) 1b

5.99 Fing: d. W=0

Using the above free-body diagrams OF THE GATE, HAVE ..

\$EMA = 0: (4 ft)[249.6(d-4) 15]

+(\$1t)[249.6(d-0.53590)16] - (3ft)(1434.14 lb) = 0

OR (332.8 d-1331.2) + (665.6d-356.70)

- 4302.4 = 0 or d=6.00 st

d > 4 ft = ASSUMPTION CORRECT

: d. 6.00 12

5.100 FIND: d. W. 1000 16

Using the above free-body biagrams of THE GATE, HAVE..

FIEM = 0: (3/1)[249.6 (d-4) 16]

+(= ft)[249.6 (d-0.535 90) 16]

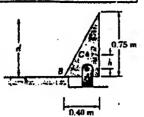
- (3 ft)(1434.14 fb)-(1 ft)(1000 fb) = 0

OR (332.8 d-1331.2) + (665.6 d-356.70)-4302.4 - 1000 : 0

or d = 7.00 ft d2 4 ft & ASSUMPTION CURRECT

:. d= 7.00 ft

5.101 and 5.102



GIVEN: PRISMATICALLY SHAPED GATE. WATER

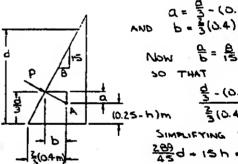
FIRST NOTE THAT WHEN THE GATE IS ABOUT TO OPEN (CLOCKWISE ROTATION IS IMPENDING), By -O AND THE LINE OF ACTION OF THE RESULTANT P OF THE PRESURE

PIN AT A. IN ADDITION, IF IT IS ASSUMED THAT 1(0.75m) . J.25m THE GATE IS

FORCES PASSES THROUGH THE

HOMOGENEOUS THEN ITS

CENTER OF GRAVITY (COINCIDES WITH THE CENTROID OF THE TRIANGULAR AREA. THEN ...



\$ (0.4 m)

a = 3 - (0.25-h) AND b= 3(0.4) - 13(3)

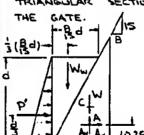
> TAHT OC 旲 - (0.25-ト)

> > (1)

SIMPLIFYING YIELDS 500 4 12 H = 30-P

ALTERNATIVE SOLUTION

COUSIDER A FREE BODY CONSISTING OF A I-M THICK SECTION OF THE GATE AND THE TRIANGULAR SECTION BDE OF WATER ABOVE



Now... $P' = \frac{1}{2}A - p' = \frac{1}{2}(dx + m)(pqd)$ = $\frac{1}{2}pqd^{2}$ (N)

W = pgV = pg (= = = = d = d = 1 m)

(025-h)m --- 3(0.4 m)

THEN WITH By = 0 (AS EXPLAINED ABOVE) HAVE .. DEM = 0: (10.4) - 1(是d)(音 pgd)

-[g-(0.25-h)](z pgd)=0

SIMPLIFYING YIELDS .. 289 d+ 15h = 70.6 AS ABOVE.

(CONTINUED)

5.101 and 5.102 CONTINUED

5.101 Find: d, h= 0.10 m

2003-17071NG INTO EW. (1) ...

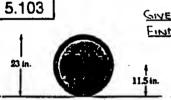
289 d + 15(0.10) = 20.6

OR d=0.683m

5.102 Find: h. d= 0.75 m

 $\frac{269}{45}(0.75) + 15h = \frac{20.6}{12}$

OR h=0.0711m 4



GIVEN: WINTH = 30 IN., WATER

FIND: RESULTANT R OF

PRESSURE FURCES

ACTING ON DRUM

CONSIDER THE ELEMENTS OF WATER SHOWN. THE
RESULTANT OF THE WEIGHTS OF WATER ABOVE
EACH SECTION OF THE DRUM AND THE
RESULTANTS OF THE PRESSURE FORCES
ACTING ON THE VERTICAL SURFACES OF THE
ELEMENTS IS EQUAL TO THE RESULTANT
HYDROSTATIC FORCE

P₁

ACTING ON THE DRUM.

THEN.. $P_1 = \frac{1}{2}A_1 - \frac{1}{2}A(xh)$ $= \frac{1}{2}[(\frac{1}{12})H_1(\frac{13}{12})ft]$ $= ((62.4 \frac{1}{12})(\frac{13}{12}ft)]$

= 286.542 lb $P_{\pi} = \frac{1}{2}A_{-}P_{\pi} = \frac{1}{2}A(kh)$ = $\frac{1}{2}[(\frac{30}{12})H + (\frac{11.5}{12})H]$ = $[(62.4 \frac{11.5}{12})(\frac{11.5}{12}H)]$

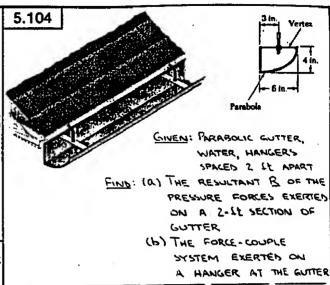
 $M' = RA' = (rs.4 \frac{17}{12})[(\frac{115}{115})_r tf_r - \frac{1}{4}(\frac{115}{115})_r tf_r](\frac{15}{15}tr)$

 $W_3 = 8V_3 = (62.4 \frac{16}{12}) \left(\frac{7}{12} \right)^2 H^2 \left(\frac{30}{12} \right) t$ = 112.525 Ib

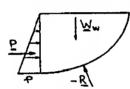
THEN. : \$\frac{+}{\sum_{\chi}} \text{R}_{\chi}: R_{\chi} = (286.542-71.635)16 = 214.91 16
+\frac{1}{\sum_{\chi}} R_{\chi} = (-30.746+255.80 + 112.525) 16
= 337.58 16

FINALLY .. R = VR + Ry TAND = Rx = 400.18 16 D = 57.5

1. R = 400 16 1 57.5° €



(a) Consider a 2-12-long parabolic section of water. Then...



P= ½A.p = ½A(xh) • ½[(½4)(264][(624]2)(426) = 6.9333 lb W= XV = (624]2)[3(126)(126)

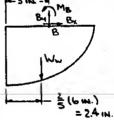
NOW.. \(\subseteq \frac{1}{2} = 0 : \left(-\frac{R}{2} \right) \frac{P}{2} \rightarrow \frac{W}{2} \)

THAT \(R = \frac{1}{2} \subseteq \frac{W}{2} \)

= 15.5034 \(\text{lb} \)

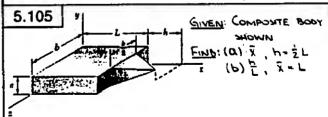
\(\text{R} = 15.50 \)
\(\text{lb} \)
\(\text{V} = 3.4^\circ
\)

(b) CONSIDER THE FREE-BOST DIAGRAM OF A
2-14-LONG SECTION OF WATER AND GUTTER.



INE FORCE- COUPLE SYSTEM EXERTED ON THE HANGER

13.87 16 1, 8.32 16-IN.)



	V	x -	Vx
RECTANGULAR PRISM	Lab	之上	± L2ab
PYRAMID	3a(2)h	L+ 4h	6abh(L+4h)

THEN.. $\Sigma V = ab(L+bh)$ $\Sigma \bar{\chi} V = bab[3L^2 + h(L+bh)]$ (continues)

5.105 CONTINUED

Now.. $\bar{X} \sum V \cdot \sum \bar{x} V$ so THAT $\bar{X} \left[ab(L + \dot{b}h) \right] = \dot{b}ab(3L^2 + bL + \dot{b}h^2)$ or $\bar{X} \left[1 + \dot{b} \stackrel{?}{E} \right] = \dot{b}L(3 + \stackrel{?}{E} + \dot{a} \stackrel{?}{E} \stackrel{?}{E})$ (1)

(a) \bar{X} : WHEN $h = \bar{z}L$ SUBSTITUTION \bar{C} : \bar{z} INTO EQ. (1)... $\bar{X}[1+b(\bar{z})] = bL[3+(\bar{z})+\bar{4}(\bar{z})^2]$

OR $\bar{X} = \frac{51}{104} L$

X = O. 548 L

(b) \(\hat{L}^{2} \) WHEN \(\hat{X} \cdot \L
\)
SUBSTITUTING INTO EQ. (1)...
\(\left(\frac{1}{L} \right) = \frac{1}{L} \left(\frac{1}{2} + \frac{1}{L} \right) \)

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{2} + \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L} \right) = \frac{1}{L} \right) \\

OR... \(\left(\frac{1}{L}

5.106

| Given: Composite som
| Shown | Finite: (a) \(\tilde{q} \), \(\tilde{q} \) = 0.4a

	V	4	4 V
HEMISPHERE	57a3	- <u>ફે</u> a	-A TRA
SEMIECLIPSION	-37(8)+ =- == ==	-Bh	+ icnathi

THEN.. $\Sigma V = \frac{\pi}{6} \alpha^{2} (4\alpha - h)$ $\Sigma \vec{q} V = -\frac{\pi}{16} \alpha^{2} (4\alpha^{2} - h^{2})$ 5.108 NOW... $\Upsilon \Sigma V = \Sigma \vec{q} V$ So THAT $\Upsilon [\mathcal{F} \alpha^{1} (4\alpha - h)] = -\frac{\pi}{16} \alpha^{2} (4\alpha^{2} - h^{2})$ OR $\Upsilon (4 - \frac{\pi}{6}) = -\frac{\pi}{6} \alpha [4 - (\frac{\pi}{6})^{2}]$ (1)

(a) $\bar{Y} = \hat{x}$ WHEN $h = \frac{1}{2}$ Substituting $\bar{\Omega} = \frac{1}{2}$ into Eq. (1). $\bar{Y}(4 + \frac{1}{2}) = -\frac{1}{12}a$ $\bar{Y} = -\frac{45}{112}a$ $\bar{Y} = -\frac{45}{112}a$ $\bar{Y} = -\frac{45}{112}a$

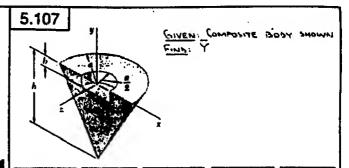
(b) $\frac{\pi}{a}^2$ WHEN $\frac{7}{4} - 0.4a$ SUBSTITUTING INTO EQ. (1)...

(-0.4a)(4- $\frac{\pi}{a}$) = - $\frac{\pi}{a}$ a.[4-($\frac{\pi}{a}$)²]

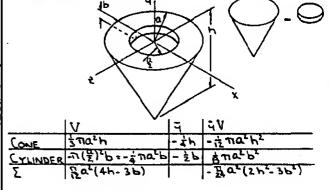
OR 3($\frac{\pi}{a}$)² - 3.2($\frac{\pi}{a}$) +0.8 =0

THEN... $\frac{\pi}{a}$ = $\frac{5.2^{\frac{1}{2}}\sqrt{(-3.2)^2-4(3)(0.8)}}{2(3)}$ = $\frac{3.2^{\frac{1}{2}}0.8}{a}$

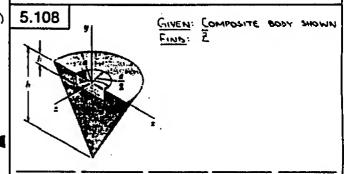
UR A S AND A S



FIRST NOTE THAT THE VALUES OF Y WILL BE THE SAME FOR THE GIVEN BODY AND THE BODY SHOWN BELOW. THEN.



HAVE .. $\overline{Y} \sum V = \sum \overline{q} V$ THEN .. $\overline{Y} \left[\frac{\pi}{12} \alpha^{L} (4h - 3b) \right] = -\frac{\pi}{24} \alpha^{2} (2h^{2} - 3b^{2})$ OR $\overline{Y} = -\frac{2h^{2} - 3b^{2}}{2(4h - 3b)}$



FIRST NOTE THAT THE BODY CAN BE FORMED BY REMOVING A HALF-CYLINDER FROM A HALF-CONE.

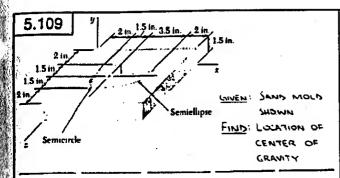


· · · · · · · · · · · · · · · · · · ·	IV	1	VzV
HALF-CONE	tπa ⁱ h	- A *	− 🔓 Q³ h
HAUS- CYLINGER	-3(E)2P=-BacP	雅(生) 統-	15 azp
Σ	= Q1 (4h - 3h)		-1203(2h-b)

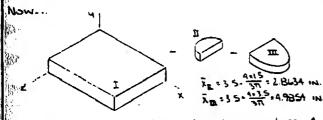
FROM SAMPLE PROBLEM 5.13

HAVE . ZZV . ZEV

THEM .. = [= 02 (4h-3b)] = - 12 03 (2h-b)



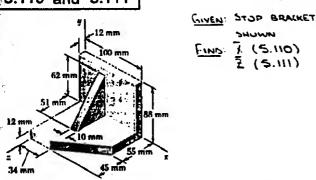
FIRST ASSUME THAT THE MOLD IS HOMOGENEOUS SO THAT ITS CENTER OF GRANTY WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING VOLUME, SYMMETRY THEN IMPLIES \$\overline{Z} \cdot 3 5 in.



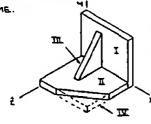
	V. 1N3	X.IN	9. IN	xV.1N4	4 V. IN
	(9)(1.5)(7) = 94 5	4.5	ن.15	425.25	10.815
		2.8434	1.125	-7 5900	- 2.9820
	- 2(3.5)(1.5) 0.75) 0.1850				-4.9581
Σ				386.83	
15%	*				

AND YEV=EYV: Y(BS. WA IN) = 60.935 IN

5.110 and 5.111



FIRST ASSUME THAT THE BRACKET IS HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROIS OF THE CORRESPONDING VOLUME.



Xm = 34+2(10) = 39 mm Zm = 12+2(88)=56 mm

XX = 34+3(66)=18 mm 2X = 55+3(45)=85 mm

(CONTINUED)

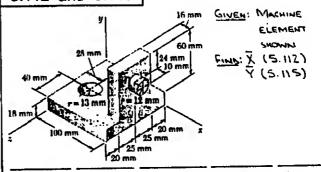
5.110 and 5.111 CONTINUED

	V. mm3	X, mm	Ł, mm	XV, mm	2 V. mm+
	(100)(88)(12)=105 600	50	د	5 2B0 000	L33 600
	(100)(12)(88):105 600		56	5 280 000	5913 600
	といろしなしまりょうち 810		29	616 SAD	458 490
	- ¿(66)(12)(45) = -17 BZO		85	-1 389 960	-1 514 700
Σ				9 786 430	5 490 990

5.110 Have.. $\bar{X} = \bar{X} = \bar$

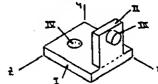
5.111 HAVE. ŽŽV : ŽŽV Ž(209 190 mm³): 5 490 990 mm³ OR Ž=26.2 mm ◀

5.112 and 5.115



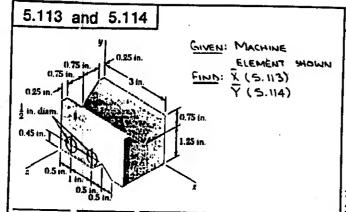
FIRST ASSUME THAT THE MACHINE ELEMENT 15
HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL
CONCIDE WITH THE CENTROIS OF THE CORRESPONDING
VOLUME:

41
41
41



İ	V.mm²	X.mm	4, mm	xV.mm	= V. mm4
Ī	(100)(18)(90)=162 000	50	9	8 100 000	
	(16)(60)(50)= 48000	92	4B	4 416 000	2 304 000
	TI(12)2(10) = 45239	105	54	475 010	244 290
	-7(13)L(1B) - 9556.7	28	٩	- 267 590	- 86 010
Σ	204 967.2			12 723 420	3920 280

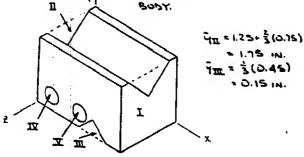
5.115 HAVE .. \(\bar{Y}\bar{E}V \cdot \bar{Z}\bar{V}\)
\(\bar{Y}(204.967.2 \text{ mm}^3) = 3.920280 \text{mm}^3\)
\(\sigma \bar{Y} \cdot \bar



FIRST ASSUME THAT THE MACHINE ELEMENT IS HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL COINCINE WITH THE CENTROID OF THE CORRESPONDING VOLUME. ALSO NOTE THAT THE TWO HOLES AND THE Y-NOTCH EXTEND THROUGH THE

- 1.75 IN.

+ 0.15 IN.

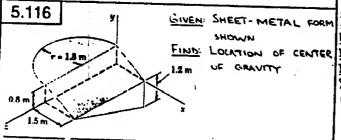


_	V. 1N 3	X.IN.	Q.IN.	XV. 1N4	4V. 14
	(3)(2)(2) = 1/2	1.5	1	1B	172
\overline{u}		1.5	1.75	- 2.53125	- 2.9531
亚	- ±(1)(0.45)(2)=-0.45	2	0.15	-0.90	-0.0675
巫	- n(2)2(2)=-0.39270	0.5	0.45	-0.19635	-0.17672
V	صريمور.c-= (ع) عرابًا) ته -	1.5	0.45	-0.58905	-0.17672
Σ	וררט.פ			13.7834	8.6260

5.113 HAVE _ X Z V + Z X V X(9.0171 INS) = 13.7834 INA OR \$ 1.518 IN.

5.114 HAVE .. YEV - ZIV Y (9.0771 IN3)= 8.6260 IN Ÿ =0.950 in. ◀

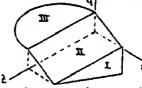
5.115 SEE SOLUTION TO PROBLEM 5.112



FIRST ASSUME THAT THE SHEET METAL IS (CONTINUED)

5.116 CONTINUED

HUMOGENEUUS SO THAT THE CENTER OF GRAVITY OF THE FORM WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING AREA.

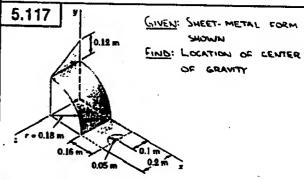


41 =-3 (1.2) =-0.4 m = = 1 (3.6) = 1.2 m XIII = - 4(1.B) = - 7.4 m

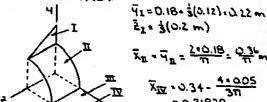
\(\frac{\bar{\pi}_m \bar{\pi}_m \bar{\pi}_ = (3.6)(1.2) = 2.16 1.5 -0.4 1.2 3.24 (3.6)(1.7) = 6.12 | 0.75 | 0.4 | 1.8 | 4.59 2.448 11.016 III 7(1.8)2=5.0894 - 25 0.8 1.8 -3888 4.0715 9.1609 13.3694 3.942 5.6555 22.769

HAVE. X & V = & x V: X (13.3694 m2) = 3.942 m3 OR X = 0.295 m ΥΣV- ΣqV: Υ(13.3694 m²) = 5.6555 m²

OR Y= 0.423 m 2 [V = [2] V :] (13.3694 m2) = 22.769 m3 OR = 1.703 m



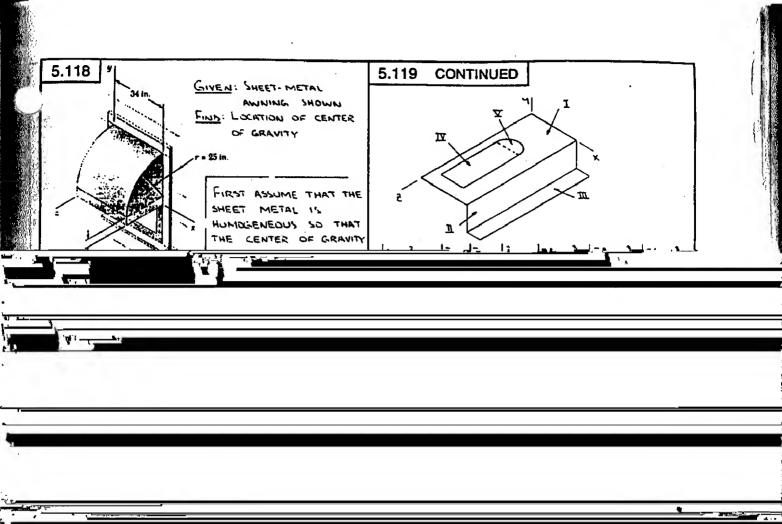
FIRST ASSUME THAT THE SHEET METAL IS HOMOGENEOUS SO THAT THE CENTER OF GRAVITY OF THE FORM WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING AREA.



	A.m2	X,m	9.1	2 m	xA.m3	=A m2	3A 3	
	\$(0.2\x0.12) = 0.DIZ	10	022	2.2	0	0.00264	0.000B	
1	1 (0.18)(0.2)= CO181	0.35				0.00048	0.005655	
11		0.26	101		0.00832		0.0032	
V	-7(0.05) = -0.0012511	0.31878	0	0.1	-aonzse		£4£000.0-	
	0.096655				0.03548	0.00912	0.009 2 L2	
н	0.096655							

OR X+0.1402m YEV= EqV: Y(0.096 622 m2) = 0.00912 m3

OR Y=0.0944m 2ΣV- Σ=V: 2(0.696622 m²) = 0.009 262 m² OR = = 0.0959m



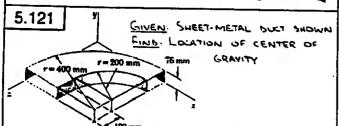
5.120 CONTINUED

A2 = A4 = A6 = A10 = 72 = 6 = 60 = 565.49 mm²
A6 = 71 = 5 = 60 = 942.48 mm²

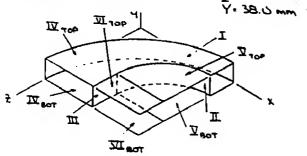
	A. mm2	X,mm	9.mm	XA, mm3	GA, mm3
1	(74)(4): 4440	0	43	D,	190 920
<u>z</u>	565.49	2.1803	2.1803	1233	1 2 33
3	(30)(60): 1800	21	0	37800	0
4	545.49	39.820	EUGI S	22518	1233
5	(64)(65)+4140	42	40.5	173 880	167670
6	942.48	47	78.183	44 297	73686
7	(49X60): 4140	52	40.5	215280	167670
8	545.49	54.180	2.1603	30638	1233
	(751(60) - 4500	95.5	0	429750	0
10	545.49	136.820	E091 5	טרצ רר	1233
Σ	22 224.44			1 032 744	LOA KIR

HAVE .. $\bar{X} \Sigma A = \Sigma \bar{x} A$: $\bar{X} (22 224.44 \text{ mm}^2) = 1 032 76L \text{ mm}^3$ OR $\bar{X} = 46.5 \text{ mm}$ $\bar{Y} \Sigma A = \Sigma \bar{y} A$: $\bar{Y} (22 224.44 \text{ mm}^2) = 604 878 \text{ mm}^3$

OR Y = 27.2 mm



FIRST ASSUME THAT THE SHEET METAL IS
HOMOGENEOUS SO THAT THE CENTER OF CRAVITY
OF THE DUCT WILL COINCIDE WITH THE CENTROIS
OF THE CORRESPONDING AREA. NOW NOTE THAT
SYMMETRY IMPLIES



 $\bar{X}_{I} = \bar{\hat{\xi}}_{I} = 400 - \frac{2 \times 400}{77} = 145.352 \text{ mm}$

XI = 400 - 2220 = 212.68 mm EI = 300 - 2220 = 172.676 mm

XX = 2X = 400 - 4x400 = 230.23 mm

 $\bar{X}_{\Sigma} = 400 - \frac{4 \times 200}{3\pi} = 31.212 \text{ mm}$ $\bar{\xi}_{\Pi} = 300 - \frac{4 \times 200}{3\pi} = 21512 \text{ mm}$

ALSO NOTE THAT THE CURRESPONDING TUP AND BOTTOM AREAS WILL CONTRIBUTE EQUALLY WHEN DETERMINING X AND Z. THUS...

(CONTINUES)

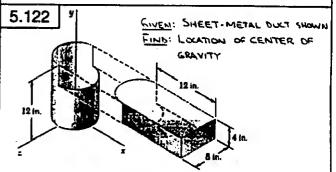
5.121 CONTINUED

	A. mmz	X. mm	Z,mm	XA. mm3	2A, mm3
	3 (400)(76)=47 752		-	6 940 BSO	
Ī	2(200)(76)=23 876	272.68	172.676	6510 510	4 122 810
111	(100)(76)+7600	200	350	1 320 000	2 440 000
V	2- \$ (400) = 251 521	230.23			57 843 020
		315.12			-13 516 420
应	-2(100+200)+-40 000	300		-12 000 000	
Σ.	227 723				44 070 260

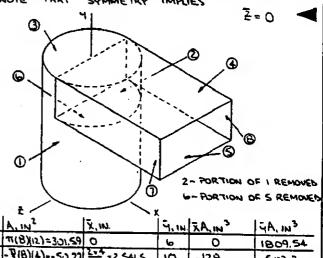
HAVE.. XEA = ExA: X(227 723 mm²) = 41 034 760 mm OR X = 180.2 mm ◀

Ē ΣΑ = ΣἔΑ: Ē (227 723 mm²) = 44 070 260 mm²

DR Ē = 193.5mm ◀



FIRST ASSUME THAT THE SHEET METAL IS
HOMOGENEOUS SO THAT THE CENTER OF GRAVITY
OF THE DUCT ASSEMBLY WILL COINCIDE WITH THE
CENTROIS OF THE CURRESPONDING AREA. NOW
NOTE THAT SYMMETRY IMPLIES

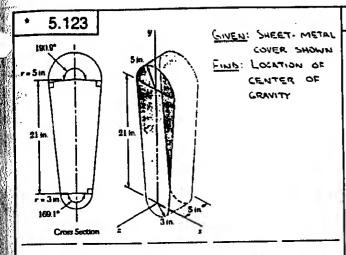


_	A. INZ	X, IN.	4.1N	XA, IN 3	EM. AF.
L	7(B)(12)=301.59	0	6	0	1809.54
۷_	16)(4)=-50.27	2 = 2.5ALS	10	-128	-502.7
	1 (4) = 25.13	-4-4 1.19765	12	- 42.667	301.56
	(15)(8).96	b	12	576	1152
<u> </u>	(12)(B)=96	و	0	576	748
_	-2(4)2-25.13	124 = 1.6965	8	- 42.667	- 201.04
	(12)(4)-48	ب	10	288	480
	(12)(4).48	6	õ	288	480
٤	25.92			1514.666	4287.36

HAVE .. XEA - EXA: X (539.32 IN2) - 1514. LLG IN2

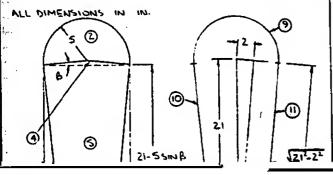
ΥΣΑ • Σ ¬ A: Υ(539.32 IN2) • 4287.32 IN2

OR Y . 7.95 IN.



FIRST ASSUME THAT THE SHEET METAL IS
HUMOGENEOUS SO THAT THE CENTER OF GRAVITY
OF THE COVER WILL COINCIDE WITH THE
CENTROIS OF THE CORRESPONDING AREA. NOW
NOTE THAT SYMMETRY IMPLIES

X = 0



5.123 CONTINUED

$\ddot{q}_{5} = \frac{1}{2}(21 - 2 \sin 5.45^{\circ})$ $-3 \sin 5.45^{\circ}$ $= 10.120 \text{ in}$ $\ddot{q}_{6} = \ddot{q}_{7} = \frac{1}{3}(21 - 2 \sin 5.45^{\circ})$ $-3 \sin 5.45^{\circ}$ $= 6.652 \text{ in}$ $\ddot{q}_{6} = -\frac{3 \sin \left(\frac{1991^{\circ}}{2}\right)}{\left(\frac{1991^{\circ}}{2}\right)^{\circ} \left(\frac{1991^{\circ}}{2}\right)}$	$A_{5} = (21-2\sin 5.45^{\circ})$ $= 2(5\cos 5.45^{\circ})$ $= 207.2 \text{ in}^{2}$ $A_{6} = A_{7} = -\frac{1}{2}(2\cos 5.45^{\circ})$ $= (21-2\sin 5.45^{\circ})$ $= -20.72 \text{ in}^{2}$ $A_{8} = [(149.1^{\circ} - \frac{17}{180^{\circ}})(3)](5)$ $= 44.27 \text{ in}^{2}$
= - 2.024 IN. $\frac{1909^{\circ}}{79}$ = 214 $\frac{5 \sin(\frac{1909^{\circ}}{2})}{(\frac{1909^{\circ}}{2} + \frac{1909^{\circ}}{190})}$ = 23.99 IN. $\frac{7}{10} = \frac{7}{10} = \frac{7}{10}$ = 10.120 IN.	Ag = [(1909 = 1800)(5)](5) = 83.30 in ² Aio = Aii = ((21222)(5) = 104.52 in ²

				_	
	A. INZ	J. 1N.	Z. IN.	9A, 143	ZA, 1N3
$\overline{}$	13.281	- 1. 3492	-5	-17.919	-66.41
2	41.65	22.99	- 5	951.5	- 204.3
3	- U. 850A		-5	0.162	4.255
4	2.364	20.6B	-5_	48.89	-11.850
5	201.2	10.120	- 5	2597	-1036.0
وا	-20.72	لککها.ط	- 5	-137.83	103.60
7	- 20.72	6.62	- 5	-137.83	103.60
8	44.27	-2.024	-2.5	- 89.60	-110.6B
9	83.30	23.99	-2.5	199B.4	-208.3
10		10.120	-2.5	1057.7	- 241.3
11		10.120	-2.5	1057.7	- 261.3
Ξ	558.8			6834	-1952.7
H		£3 = Α3	$\mathbf{Y}: \mathbf{A}$	(558.8	1112) - 6834 1113
,,,		_ ,			7 12 22 m 🚄

Y=12.23 IN.

5.124 CONTINUED

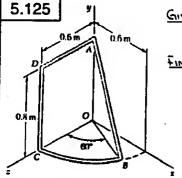
_	L.m	Ž,m	4.50	5.10	XL, m2	Jul.ma	žL,m2
<u>L</u>	2.6	1.2	05	0	3.12	1.3	٥
2	₹ . 2 4 . 1211	4.8	0	a la	5.76	0	5.76
3	24	0	0	1.2	0	0	2.88
4	1.0	0	ა.5	0	Ö	٥.5	ی
Σ	9,7699				8.88	1.8	8.64

HAVE .. ズ EL= E末L: X(9.7699 m)= 8.88 m² OR X= 0.909 m

781-891: Y(97699m)=1.8m2

OR Y = 0.1842m 2εL = εξL: 2 (9.769 m) = B.64 m2

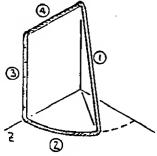
OR 2 = 0.884 m



GIVEN: UNIFORM WIRE BENT INTO THE SHAPE SHOWN

FIND: LOCATION OF CENTER DE GRAVITY

FIRST ASSUME THAT THE WIRE IS HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROID OF THE CORRESPONDING LINE.



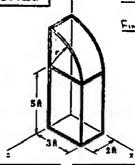
x,=0.3 sin 60 = 0.1513 m £, = 0.3 cos 60 + 0.15 m \$ 2 = \(\frac{\alpha}{2000 \text{min}} \) = \(\frac{\pi}{200} \text{m} \) = \(\frac{\pi}{2000 \text{m}} \text{m} \) ξ₂ = (3.6 31030) cos 30 = 3.9 13 m

_	L.M	x. m	4,00	2,10	XL.m2	4L.m2	ZL, m2
7	1.0	0.1513	0.4	0.15	D.259B1	0.4	0.15
2	0.27	2.9	0	55/2	0.18	0	3.31177
3	0.8	0	0.4	0,6	0	0.32	0.48
4	ა. ს	0	0.8	0.3	0	5.48	0.18
٤	3.0283				0.43981	1.20	1.12177

HAVE. XEL= EXL: X(3.0283m)=0.43981 m2 OR X = 0.1452 m

YEL-EqL: Y(3.0283 m) = 1.20 m²

02 Y=2396m 2ΣL=Σ=L: 2(3.0283 m)=1.1217 m²
οα 2=0.370 m? 5.126



GIVEN: PORTION OF GREENHOUSE FRAME SHOWN

FIND: LOCATION OF CENTER OF GRAMTY

> FIRST ASSUME THAT THE CHANNELS ARE HOMOGENEOUS SO THAT THE CENTER OF GRAVITY OF THE FRAME WILL COINCIDE WITH THE CENTROD OF THE CORRESPONDING LINE.

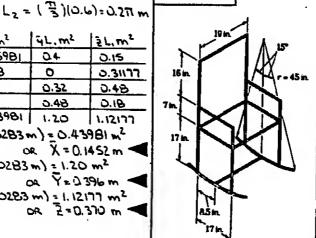
X8 = X9 = 2+3 = 4 1t 4B = 49 = 5+ 23

	, Ł 🛡	$-\omega$	' X				
	L. \$2		4.12	2, 19	1. 42°	46, 422	£ 602
<u></u>	2	3	5	١	Ь	ত	2
2	3	1.5	0	2	4.5	0	ب
3	5	3	2.5	ે	15	12.5	0
4	5	3	2.5	2_	15	12.5	10
5	В	0	4	2	0	32	16
ما	2	3	5	1	6	10	2
7	3	1.5	5	2	4.5	15	6
8	7-3=47124	**	6.9099	0	9	32,562	υ
9	E-3-4.7124	*	6.939	2.	9	32,562	9.4148
10	2	a	В	1	0	16	2
Σ	39.424B				69	163.124	53.4248
	= = =	- . (-	~ ·			. *

HAVE.. X [= [x (39.4248 ft) = L9 ft2 OR X = 1.750 St YEL = ΣqL: Y(39.4248 ft) - 163.124 62 Y = 4.14 lt OR

₹ΣL = Σ = L: 2(39.4248 ft) - 53.4248 ft Ž = 1.355 }t ≺

5.127



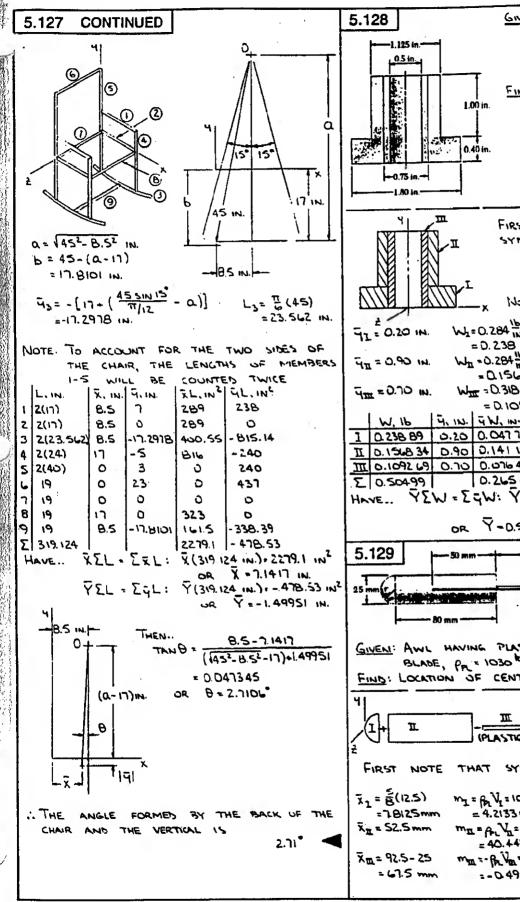
ROCKER AND THE GROWNS.

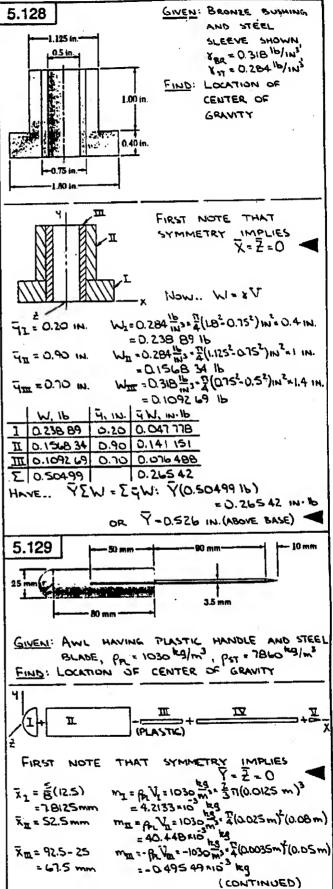
GIVEN: ROCKING CHAIR FRAME MOWN FIND: ANGLE BETWEEN

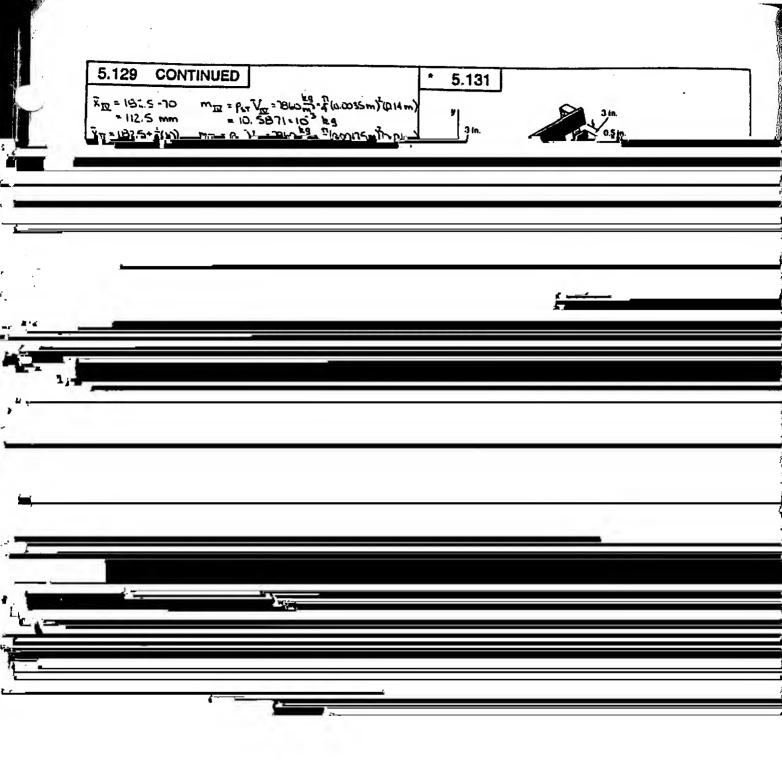
CHAIR BACK AND VERTICAL

FIRST ASSUME THAT THE tubing is homogeneous SO THAT THE CENTER OF GRAVITY OF THE FRAME WILL COINCIDE WITH THE CENTROID DE THE CORRESPONDING LINE ALSO, NOTE THAT THE CENTER OF GRAVITY MUST LIE ON A VERTICAL LINE THAT PASSES THROUGH THE POINT OF CONTACT OF A

(CONTINUED)







5.131 CONTINUED

THEN .. EW = 230.18 16

E & W = 2636.2 IN.16 8.0001- WE3

X (230.18 1b)=2636.2 IN.16 XΣW= ExW: OR X = 11.45 IN.

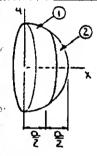
YEN . EAW: Y(230.18 16)=-1000.89 will

OR Y = -4.35 IN.

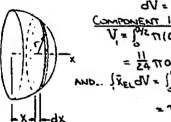
5.132

GIVEN: A HEMISHERE WHICH IS CUT OWT OTH COMPONENTS OF EDUAL INISTH AS SHOWN

FIND: X OF EACH COMPONENT



CHOOSE AS THE ELEMENT OF VOLUME A DISK OF RADIUS T AND THEKNESS dx. THEN dis mezdx, XEL = X THE EQUATION OF THE GENERATING CURVE 15 X2+42 Q2 SO THAT C2 Q2-X2 AND THEN dV = 17 (a2-x2) dx



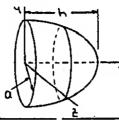
 $\int_{0}^{\infty} \frac{1}{\sqrt{2}} \int_{0}^{\infty} \frac{1}{\sqrt{2}} \left(\frac{1}{\sqrt{2}} - \frac{1}{\sqrt{2}} \right) dx = \int_{0}^{\infty} \frac{1}{\sqrt{2}} \int_{0}^{\infty} \frac{1}$ $\frac{1}{2} = \frac{11}{24} \pi \alpha^3$ AND. $\sqrt{x_{EL}} = \sqrt{x_{EL}} = \sqrt{x_{EL}} = \sqrt{x_{EL}}$ $=\pi[\alpha^{2}\frac{\chi^{2}}{2}-\frac{\chi^{4}}{4}]^{\alpha/2}$

Now .. X, V, = [x = dV: X, (14 na3) = = na4

 $\int_{\Omega} \frac{dx}{dx} = \frac{1}{2} \left[\left(\frac{x}{\alpha} - x_F \right) dx = \frac{1}{2} \left[\left(\frac{x}{\alpha} - \frac{3}{2} \right) \right] dx - \frac{3}{2} \left[\left(\frac{x}{\alpha} - \frac{3}{2} \right) \right] dx - \frac{3}{2} \left[\left(\frac{x}{\alpha} - \frac{3}{2} \right) \right] dx$

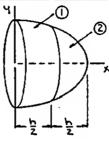
Now.. $\bar{\chi}_2 \bar{V}_2 = \int_{\bar{k}} \bar{\chi}_{EL} dV$: $\bar{\chi}_2 \left(\frac{5}{24} \pi \alpha^3 \right) = \frac{9}{107} \pi \alpha^4$ or $\bar{\chi}_2 = \frac{27}{40} \alpha$

5.133

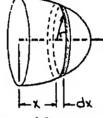


GIVEN: A SEMIELLIPSOID OF REVOLUTION WHICH IS CUT INTO TWO COMPONENT'S OF EDWAL WINTH AS MOWN

FIND: X OF EACH COMPONENT



CHOOSE AS THE ELEMENT OF VOLUME A DISK OF RASIUS AND THICKNESS dx. THEN dV=nr2dx, XEL=X THE EDUATION OF THE GENERATING CURVE 15 12 + 42 =1 50 THAT L= WI(H=Xs) WHO THEN $dil = \pi \frac{\sigma_r}{\sigma_r} (\mu_s - x_r) dx$



N = INE W FS (PS-XS) dx = TT AZ [h x - X3] h/2 $=\frac{54}{11} \mu \sigma_5 \mu$

= 1 4 4 0 5 4 5 - 4 3 45 we (4, x, x,)qx]

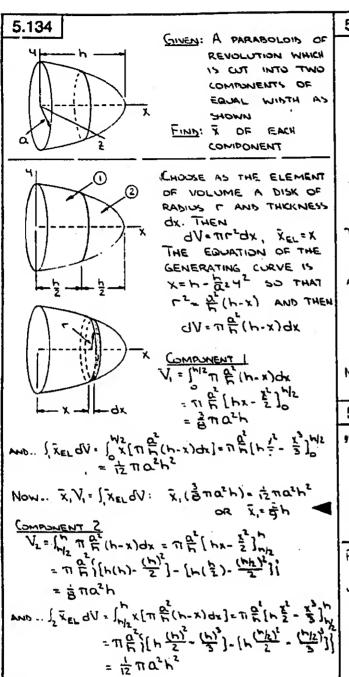
Now.. X, V, = J, XeLdV: X, (24 Ta2h) = 3 Ta2h2

or X, = 24 H

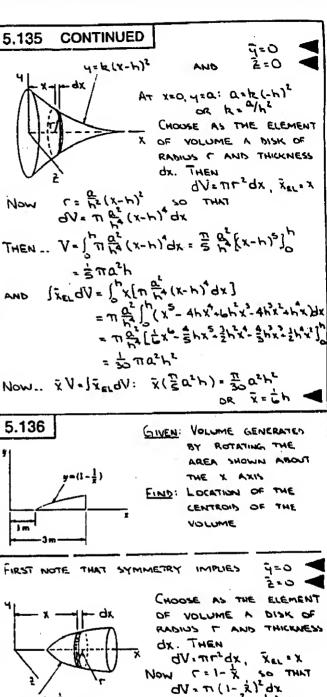
No - (Ho L & (Ho - x)) dx = 4 / 2 [Ho x - 3] Ho = 4 \frac{\mu_F}{\sigma_F}\left\[\P_z(\mu) - \frac{3}{(\mu)_3}\right\] - \left\[\P_z(\frac{5}{\mu}) - \frac{2}{(\mu)^5}\right\] = 3 Tath

 $= \frac{\mu^{2}}{\sigma_{r}} \left\{ \left[\mu_{r}, \frac{5}{(\nu)_{r}} - \frac{4}{(\nu)_{r}} \right] - \left[\mu_{r}, \frac{5}{(\nu)^{2}} - \frac{4}{(\nu)^{2}} \right] \right\}$ $= \frac{\mu}{\nu^{2}} \left[\mu_{r}, \frac{5}{x_{r}} - \frac{4}{x_{r}} \right]^{\nu/3}$ $= \frac{\mu}{\nu^{1/3}} \frac{\nu^{2}}{\sigma_{r}} \left[\mu_{r}, \frac{5}{x_{r}} - \frac{4}{x_{r}} \right]^{\nu/3}$ = = = m a2h2

Now .. \$\bar{x}_2 \bar{V}_2 = \int_1 \bar{x}_{eL} dV : \bar{X}_2 (\frac{5}{24} \pi a^2 h) = \frac{9}{14} \pi a^2 h^2 OR X2 = 40 h

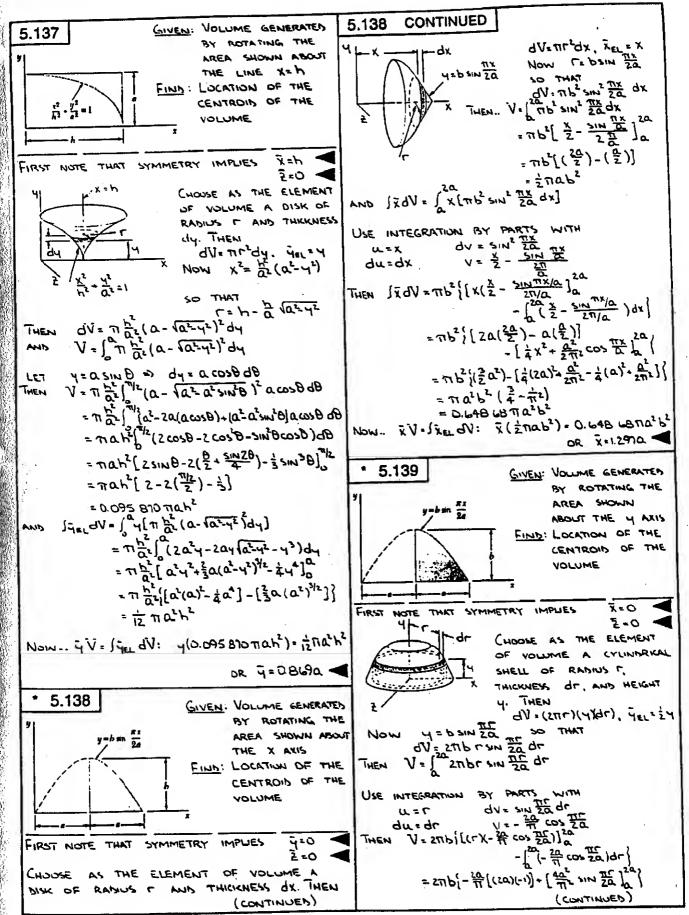


Now .. \(\bar{x}_2 V_2 = \sigma^2 \hat{k} = \dV: \bar{x}_2 (\bar{B} \pi a^2 \hat{h}) = \frac{1}{12} \pi a^2 \hat{h}^2 \)



* + (1- × + × z) dx

事が(<u>に3-21からを</u>)-(1431<u>を行きす</u>)〕



5.139 CONTINUED

= 8 a b (1- #)

ALSO $|\vec{q}_{el} dV| \cdot \int_{0}^{2\alpha} (\frac{1}{2}b \sin \frac{\pi r}{2\alpha})(2\pi b r \sin \frac{\pi r}{2\alpha} dr)$ = $\pi b^{2} \int_{0}^{2\alpha} r \sin^{2} \frac{\pi r}{2\alpha} dr$

USE INTEGRATION BY PARTS WITH

U= C

dv: SIN TIFO

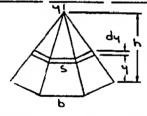
du: dr

V= \frac{7}{2} - \frac{5in}{271/0}

THEN. I GEL div = $\pi b^2 \left\{ (r) \left(\frac{r}{2} - \frac{s_{111}\pi r/\alpha}{2\pi/\alpha} \right) \right\}_{\alpha}^{2\alpha}$ $- \int_{\alpha} \left(\frac{r}{2} - \frac{s_{111}\pi r}{2\pi/\alpha} \right) dr \right\}$ $= \pi b^2 \left\{ \left(2\alpha \right) \left(\frac{2\alpha}{2} \right) - \left(\alpha \right) \left(\frac{\alpha}{2} \right) \right\}$ $- \left[\frac{r^2}{2} + \frac{\alpha}{2\pi} c \cos \frac{\pi r}{\alpha} \right]_{\alpha}^{2\alpha} \right\}$ $= \pi b^2 \left\{ \frac{3}{2} \alpha^2 - \left[\frac{(2\alpha)^2}{4} + \frac{\alpha}{2\pi} c - \frac{(\alpha)^2}{4} + \frac{\alpha^2}{2\pi} c \right] \right\}$ $= \pi a^2 b^2 \left(\frac{3}{4} - \frac{\pi}{\pi} c \right)$ $= 2.0379 \alpha^2 b^2$

Now .. & V = Sqee dV: \(\(\sigma \) = 2.0379 a262 \\
OR \(\quad = 0.3746 \)

5.140 GIVEN: A REGULAR PYRAMID OF
HEIGHT H AND N SIDES
SHOW: $\hat{q} = \frac{1}{2}$ ABOVE THE BASE



CHOOSE AS THE
ELEMENT OF VOLUME
A HORIZONTAL SLICE
OF THICKNESS DY FOR
ANY NUMBER N OF
SIDES, THE AREA OF
THE BASE OF THE

DYRAMIS IS GIVEN BY

ARMS = kb^2 WHERE k = k(N); SEE NUTE BELOW USING

SIMILAR TRIANGLES HAYE $\frac{2}{5} = \frac{1}{11}$

THEN .. div = Asing dy = k be (h-y) dy

AND V = 6 k be (h-y) dy = k be [-3(h-y) dy

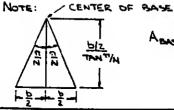
= 3 k be h

Acos. Tel = h be so THEN be h a-2hylong) dy

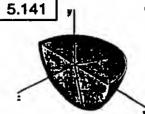
[Tel dl o] y [& hz (h-y) dy] = k hz [(h y-2hylong) dy

= k b2[2h42-3h43-4h4] m = 12k b2h2

Now.. 41= 14EL dV: 4 (3 kb2h) = 12 kb2h2 OR 4= 4h Q.E.D.



 $A_{BASE} = N \left(\frac{1}{2} a b a \frac{b/z}{TAN} \eta_N \right)$ $= \frac{N}{4 TAN} \eta_N b^2$ $= b(N) b^2$



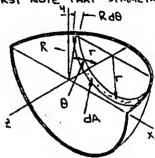
GIVEN: ONE HALF OF A THIN, UNIFORM HEMILPHERICAL SHELL

FIND: LOCATION OF CENTROIS

USING BIRECT

INTEGRATION

FIRST NUTE THAT SYMMETRY IMPLIES ROO



THE ELEMENT OF AREA DA DF THE SHELL SHOWN IS OBTAINED BY CUTTING THE SHELL WITH TWO PLANES PARALLEL TO THE XY PLANE. NOW DA = (TT)(RdD), YEL = TT

WHERE TORSIND

THEN $A = \int_{R_{2}}^{R_{2}} dA = \pi R^{2} \sin\theta d\theta$, $\int_{R_{2}}^{R_{2}} \frac{2R}{\pi} \sin\theta d\theta$ $= \pi R^{2} \int_{R_{2}}^{R_{2}} R^{2} \sin\theta d\theta = \pi R^{2} \left[-\cos\theta\right]_{0}^{R_{2}}$

MD $|\vec{A}_{EL} dA = \int_{a}^{a} |\vec{b}| \left(-\frac{\pi}{2} \sin \theta\right) (\pi R^2 \sin \theta d\theta)$ $= -2R^3 \left[\frac{\delta}{\theta} - \frac{\sin 2\theta}{4}\right]_0^{3/2}$ $= -\frac{\pi}{2}R^3$

Now. $\vec{q}A = |\vec{q}_{EL}dA|$: $\vec{q}(\pi R^2) = -\frac{\pi}{2}R^3$ $= \frac{\pi}{2}R^3$ Symmetry implies $\hat{z} = \hat{q}$: $\hat{z} = -\frac{\pi}{2}R$

5.142





GIVEN: PUNCH BOWL OF UNIFORM WALL THICKNESS

L, R = 250 mm, L &C R

FIND: LOCATION OF THE CENTER OF GRAVITY OF (A) THE BOWL

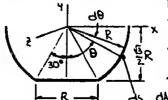
(b) THE PUNCH

(a) Bowl

FIRST NOTE THAT SYMMETRY IMPLIES

Ž=0 <

FOR THE COORDINATE AXES SHOWN BELOW. NOW ASSUME THAT THE BOWL MAY BE TREATED AS A SHELL; THE CENTER OF GRAVITY OF THE BOWL WILL COINCIDE WITH THE CENTROID OF THE SHELL.



FOR THE WALL'S OF
THE BOWL, AN ELEMENT
OF AREA IS OBTAINED
THE ARC
AS ABOUT THE Y AXIS.
THEN
CHAMIC (ZTR SIN B)(RCB)

(CONTINUES)



AND Twace Awall ' Sign wall da 'Sign (-R cos 6)(27) R2 sin 6 d6) = TIR3 [cos 6) M2 = TIR3 [cos 6] M2 = -7 TIR

BY DBSERVATION. ABOVE = 4R2, TORSE = - 1 NOW. . TEA = ETA CR. . T(TISR+TR2) = - 7TR2+TR2(- 5R) OR . T=-0.487 WBR R= 250 mm . T=-1219 mm

(b) PUNCH

FIRST NOTE THAT SYMMETRY IMPLIES \$20

AND THAT BECAUSE THE PUNCH IS HOMOGENEOUS, IT'S CENTER OF GRAVITY WILL COINCIDE WITH THE CORRESPONDING VOLUME

CHOUSE AS THE

ELEMENT OF VOLUME

A DISK OF RABIUS

X AND THICKNESS

dy dy. Then

5.143 CONTINUED

OR C = 200

: 4 = 4 - 180 x - 200 t

= -4 (1+45 x + 50 t) WHERE ALL

DIMENSIONS ARE IN FEET

CHOOSE AS THE

ELEMENT OF VOLUME

A FILAMENT OF BASE

IYI. THEN

IV. THEN

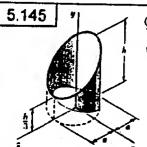
dV-141dxd2, XeL = X

THEN $V = \int_{30}^{30} \int_{4}^{4} (1 + \frac{1}{45} \times - \frac{1}{50} \cdot 2) dx dx$ $= \frac{1}{4} \int_{30}^{30} \left[x + \frac{1}{40} \times 2 + \frac{3}{50} \times 1 \right]_{30}^{30} dx$ $= \frac{1}{4} \int_{30}^{30} \left[x + \frac{1}{40} \times 2 + \frac{3}{50} \times 1 \right]_{30}^{30} dx$ $= \frac{1}{4} \left[30 + \frac{(30)^{3}}{30} + \frac{3}{50} (30) \right] dx$ $= \frac{1}{4} \left[402 + \frac{1}{10} \cdot 2^{2} \right]_{30}^{30} = \frac{1}{4} \left[40(50) + \frac{3}{10} (50)^{2} \right]$

AND $|\vec{x}_{ex} dV| = \int_{0}^{2\pi} \int_{0}^{2\pi} |\vec{x}_{1}|^{2\pi} |\vec{x}_{2}|^{2\pi} |\vec{x}_{1}|^{2\pi} |\vec{x}_{2}|^{2\pi} |\vec{x}_{1}|^{2\pi} |\vec{x}_{2}|^{2\pi} |\vec{x}_{1}|^{2\pi} |\vec{x}_{2}|^{2\pi} |\vec{x}_{1}|^{2\pi} |$

5.144 CONTINUED

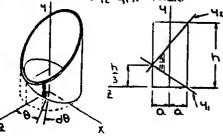
Now. $\vec{q} \ N = \begin{cases} \frac{1}{4} (1) \\ \frac{1}{4} (2) \\ \frac{1}{4} (2$



CIVEN: THE PORTION OF A CIRCULAR PIPE SHOWN FIND: LOCATION OF THE CENTROIS

on 可是h

FIRST NOTE THAT SYMMETRY IMPLIES X=0 ASSUME THAT THE PIPE MAS A UNIFORM WALL THICKNESS & AND CHOOSE AS THE ELEMENT OF NOLUME A VERTICAL STRIP OF WINTH QdB AND HEIGHT (Y2-Y1). THEN



 $dV = (y_2 - y_1)t ad\theta, \quad \forall e_1 = \frac{1}{2}(y_1 + y_2) \quad \tilde{\epsilon}_{e_1} = \frac{1}{2}$ $Now ... \quad y_1 = \frac{h/2}{2a} + \frac{1}{2} \qquad \qquad y_2 = -\frac{2h/3}{2a} + \frac{1}{2}h$ $= \frac{h}{ba}(2+a) \qquad = \frac{h}{3a}(-2+2a)$

AND $2 = \Omega \cos \theta$ THEN $(4^r - 4^l) = \frac{10}{10}(-\Omega \cos \theta + 2\Omega) - \frac{10}{10}(\Omega \cos \theta + \Omega)$ $= \frac{10}{10}(1 - \cos \theta)$

NOW $(y_1+y_2) = \frac{h}{h}(a\cos\theta + a) + \frac{h}{h}(-a\cos\theta + 2a)$ $= \frac{h}{h}(s-\cos\theta)$ (continues)

5.145 CONTINUED

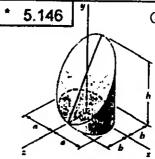
.. $dV = \frac{aht}{2} (1-\cos\theta)d\theta$, $\vec{\eta}_{EL} = \frac{h}{12} (5-\cos\theta)$, $\hat{\epsilon}_{EL} = a\cos\theta$ Then $V = 2\int_{0}^{\pi} \frac{aht}{2} (1-\cos\theta)d\theta = aht[\theta - \sin\theta]_{0}^{\pi}$ $= \pi aht$ And $|\vec{\eta}_{EL}dV| = 2\int_{12}^{\pi} \frac{h}{12} (5-\cos\theta)[\frac{aht}{2} (1-\cos\theta)d\theta]$ $= \frac{ah^{2}t}{12} \int_{0}^{\pi} (5-\cos\theta + \cos^{2}\theta)d\theta$ $= \frac{ah^{2}t}{12} \int_{0}^{\pi} (5-\cos\theta + \cos^{2}\theta)d\theta$ $= \frac{ah^{2}t}{12} \int_{0}^{\pi} (5-\cos\theta + \cos^{2}\theta)d\theta$ $= \frac{2h}{12} \pi ah^{2}t$ $= \frac{2h}{12} \pi ah^{2}t$ $= \frac{2h}{12} \pi ah^{2}t$ $= a^{2}ht[\sin\theta - \frac{aht}{2} - \frac{\sin 2\theta}{4}]_{0}^{\pi}$ $= -\frac{1}{2}\pi a^{2}ht$ Now. $\vec{\eta} V = |\vec{\eta}_{EL}dV| = \vec{\eta}_{EL}dV = \frac{1}{2}\pi ah^{2}t$

AND EV= | ZerdV: Z(TAht) = - Z TAZht

OR Z = - Za

* 5.146

* CIVEN: THE PORTION OF I
ELLIPTICAL CYLINDER

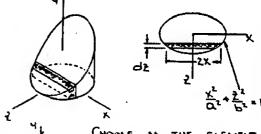


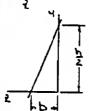
GIVEN: THE PORTION OF AN
ELLIPTICAL CYLINGER
SHOWN
1 FIND: LOCATION OF THE

FIND: LOCATION OF THE CENTROIS

FIRST NOTE THAT SYMMETRY IMPLIES







CHOOSE AS THE ELEMENT OF VOLUME A VERTICAL SLICE OF WINTH 2X, THICKNESS & AND HEIGHT 4. THEN

dV = 2xyd2, They

Now X = B (P2-35), gers Ed, gers E

(CONTINUED)

IMEN $A = \sum_{P} \left(S \frac{P}{P} \frac{(P_T - 5_5)}{P} \right) \left(\frac{SP}{P} (P - 5) \right) q5$

 $= \sigma \rho \rho \int_{-\Delta r}^{\Delta r} \frac{1}{2} (\rho \cos \theta) (\rho (r - \sin \theta)) \rho \cos \theta d\theta$ $= \sigma \rho \rho \int_{-\Delta r}^{\Delta r} \frac{1}{2} (\rho \cos \theta) (\rho (r - \sin \theta)) \rho \cos \theta d\theta$ $= \sigma \rho \rho \int_{-\Delta r}^{\Delta r} \frac{1}{2} (\rho \cos \theta) (\rho (r - \sin \theta)) \rho \cos \theta d\theta$ $= \sigma \rho \rho \rho \int_{-\Delta r}^{\Delta r} \frac{1}{2} (\rho \cos \theta) (\rho \cos \theta) \rho \cos \theta d\theta$



V= 270bh b (b-2)/(2 \$ (b-2)/20) 25(b-2)/d2/ THEN $\left\{ \frac{1}{A^{E}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{s}} \right\}_{\mu = 0}^{MS} \left\{ \frac{1}{P_{s}^{2} - 5_{s}} \frac{\partial p_{s}}{\partial r_{$

= \$\frac{1}{4} abh^2 \int \(\cos^2 \theta - 2 \sin \theta \cos^2 \theta \) d\theta + \sin^2 \theta \cos^2 \theta \) d\theta = \frac{1}{4} abh^2 \int \(\cos^2 \theta - 2 \sin \theta \cos^2 \theta \) d\theta + \sin^2 \theta \cos^2 \theta \cos^2 \theta \)

MOW SIN B = 2 (1- COS 2B) (05 B = 2 (1+ COS 2B)

so THAT SIN2θ COS2θ = \$(1- cos2θ)

THEN | THEN | THE dV = \$ abh | The (cos2θ - 2 sinθ cos2θ)

 $+ \frac{4}{4}\theta - \frac{4}{4}(\frac{5}{8} + \frac{8}{2iN49}) \Big]_{2}^{2}$ $= \frac{4}{3}\alpha P \mu_{2} \Big[(\frac{5}{8} + \frac{4}{2iN59}) + \frac{3}{2}\cos_{3}\theta + \frac{4}{3}\cos_{2}\theta \Big] + \frac{4}{3}\cos_{2}\theta \Big]$ $= \frac{4}{3}\alpha P \mu_{2} \Big[(\cos_{2}\theta - 5\sin\theta\cos\theta) \Big] + \frac{4}{3}\cos_{2}\theta \Big]$

 $A(20) \begin{cases} \frac{1}{2} \frac{1}$

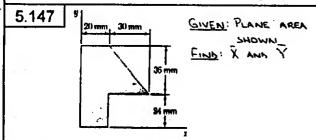
Using sing cos θ = $\frac{1}{4}(1-\cos^2\theta)$ from Above... $\frac{1}{2} \frac{1}{6} \frac{1}{6$

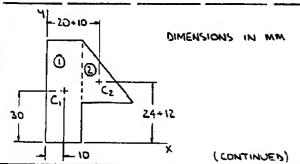
= ab2 / [- = co2 8 - 40+4(2+ SINAB)] NS

=- \(\bar{\text{P}}\) \(\pi \alpha \beta^2 \beta \)

NOW .. yV= SyEL dV: y (¿TRABH) = 32 TRABH व्य प्राहिष

MD 2V. JEEL dV: 2(2710bh)=- BTIQ bih Z=-4P

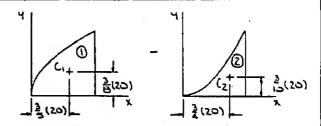




5.147 CONTINUED

	A, mm2	x,mm	4.mm	XA, mm3	9A. mm3	
1	20160 = 1200	9	30	12 000	36 000	
2	2-30-36-540	30	ى ش	16 200	19 440	
W	1740			28 200	55440	
		THEN	\bar{x}	£2 = A3	Α	
			፯	1740)=	18 100	
				or !	X=16.21 mm	
		AND	Ÿ	2 - A3	A	
1				(1740) = 5		
				DR	Y = 31.9 mm	4

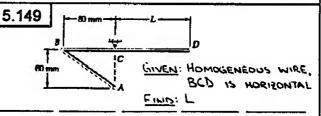
5.148 GIVEN: PLANE AREA $x = ky^2$ SHOWN FIND: X AND Y



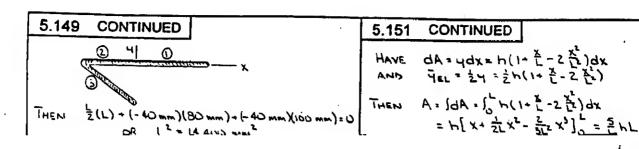
DIMENSIONS IN IN.										
	AINE	X.1N.	٦,١٨.	*A.In3	7A. 1N3					
٦.	3(50)(50)= 800/3	12	7.5	3200	2000					
2	- 3(20)(20)400/3	15	lo	-2000	-800					
Σ	400/3			1200	1200					
		THE	n Ī	ΣΑ - Σ:	ĀΑ					
	X (400/3) = 1200									
	OR X=9.00 III.									

<u>ΥΣΑ - Σ</u>ηΑ AND (400/3) = 1200 OR Y=9.00 IN.

NOTE: SYMMETRY IMPLIES X = Y WHICH IS CONFIRMED BY THE ABOVE SOLUTION.

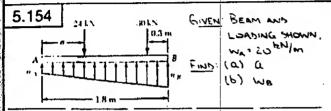


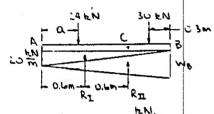
FIRST NOTE THAT FOR EQUILIBRIUM THE CENTER OF GRAVITY OF THE WIRE MUST LIE ON A VERTICAL LINE THROUGH (. FURTHER, BECAUSE THE WIRE IS HOMOGENEOUS, THE CENTER OF GRAVITY OF THE WIRE WILL COINCIDE WITH THE CENTROIS OF THE CORRESPONDING LINE. THUS. X = 0 (SEE SKETCH ON THE NEXT SO THAT EXL = O PAGE) (CONTINUES)





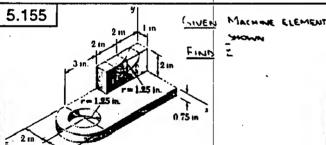
HAVE.. $R_1 = \frac{1}{2}(3.6m)(2200 \frac{N}{m}) = 3960 N$ $R_1 = (3.6m)(1200 \frac{N}{m}) = 4320 N$ $THEN.. <math>\xrightarrow{4} \Sigma F_x = 0$: $B_x = 0$ $\Rightarrow \Sigma M_B = 0$: $= (3.6m)A_{y} = (2.4m)(3960 N)$ = (1.8m)(4320 N) = 0 $\Rightarrow \alpha A_y = 480N$ $\Rightarrow A_y = 480N$



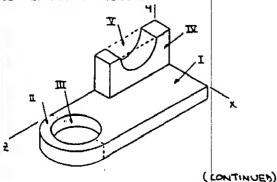


Have.. $R_{1} = \frac{1}{2}(1.8 \text{ m})(20 \frac{\text{keN}}{m}) = 18 \text{ keN}$ $R_{1} = \frac{1}{2}(1.8 \text{ m})(\text{Note } \frac{\text{keN}}{m}) \cdot 59 \text{ Note } \frac{\text{keN}}{m}$ (a) $\text{Fig.} M_{c} = 0$: $(1.2 - 2) \text{me} \cdot 24 \text{ keN} \cdot 36 \text{ keN} \cdot 30 \text{ keN$

عد ۵- س 315 m که ۵ - س 315 m که ۵ - س 315 m که ۱۵ س عد ۱۵ س اولاد اولاد که ۱۵ س اولاد که ۱۸ س اولاد که ای



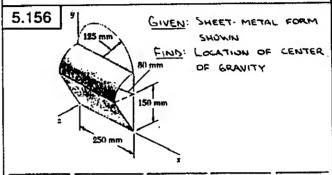
FIRST ASSUME THAT THE MACHINE ELEMENT IS HOMOGENEOUS SO THAT ITS CENTER OF GRAVITY WILL COINCIDE WITH THE CENTROIS OF THE CORRESPONDING VOLUME.



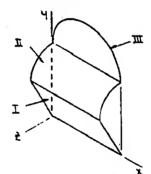
5.155 CONTINUED

1	V. 1113	Ž, IN.	EV. IN4
ī	(4)(0.15)(1) = 21	3.5	73.5
T	2(2) (0.75) = 4.7124	7+ 33 1 7.8488	36,987
\overline{m}	-77 (1.25) × (3.75) = -3.6816	1	-25,731
	(1)(2)(4) - 13	2	16
$\overline{\mathbf{x}}$	- = (1.25)2(1) =- 2.4544	2	- 4.9088
Σ	27,516		95.807

THAVE. = \$ [V. [2] : 12] = 95.807 IN



FIRST ASSUME THAT THE SHEET METAL IS
HOMOGENEOUS SO THAT THE CENTER OF GRAVITY
OF THE FORM WILL COINCINE WITH THE CENTROIS
OF THE CURRESPONDING AREA. NOW NOTE THAT
SYMMETRY IMPLIES



 $\vec{q}_{II} = 150 + \frac{71}{11}$ = 200.93 mm $\vec{c}_{II} = \frac{2 \cdot 930}{11}$ = 50.930 mm

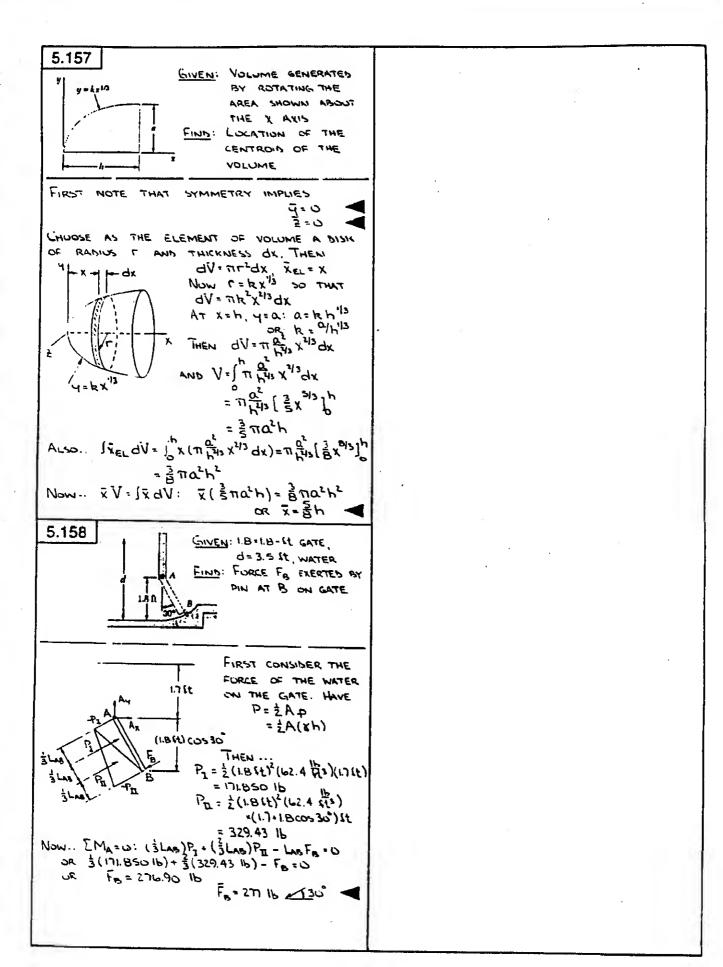
X = 125 mm

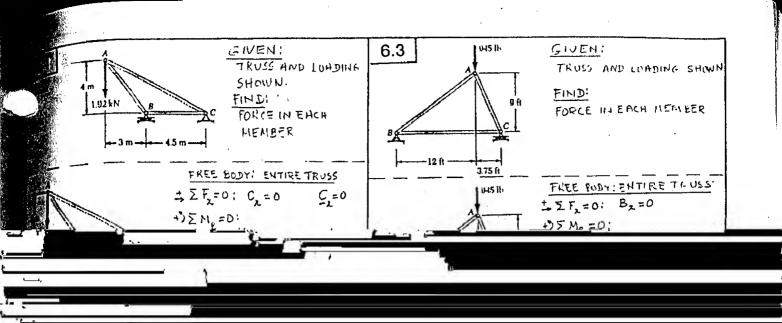
 $T_{III} = 230 + \frac{4 \times 125}{371}$ mm 20.685 =

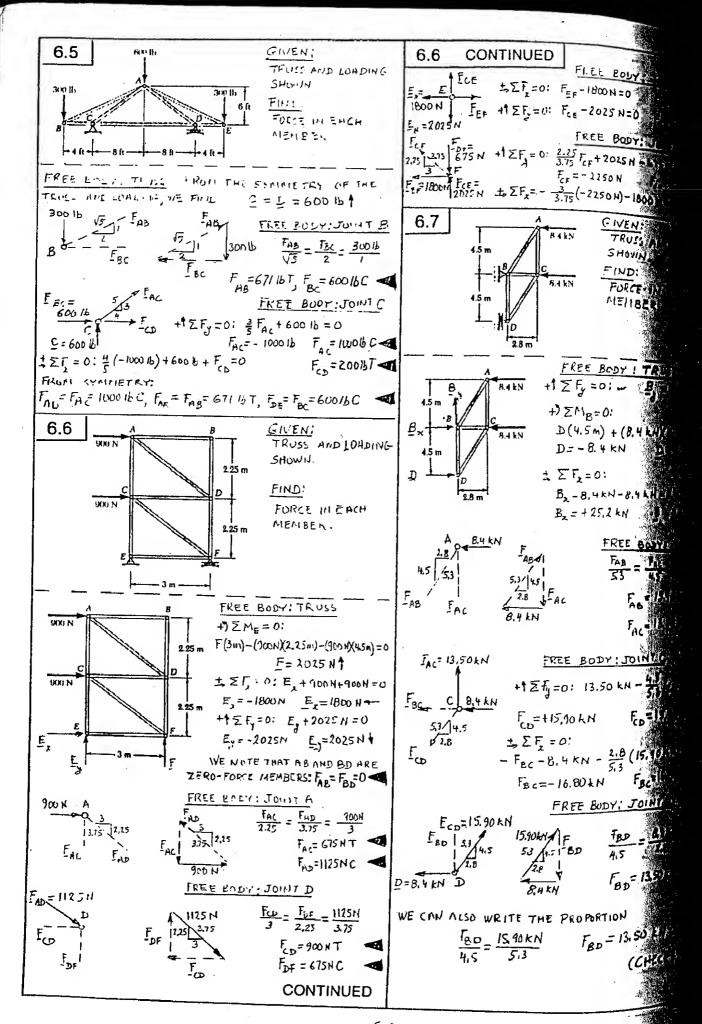
	A. mm2	4,00	2, mm	4A,mm3	2A, mm3
I	(250)(170)=42 500	75	40	3 187 500	1700 000
π	7(60)(250)=31416	200.93	50.930	6312400	1 600 000
77	7 (125)2 24 544	283.05	0	6 947 200	0_
Σ	98 460			16 447 100	3 300 000

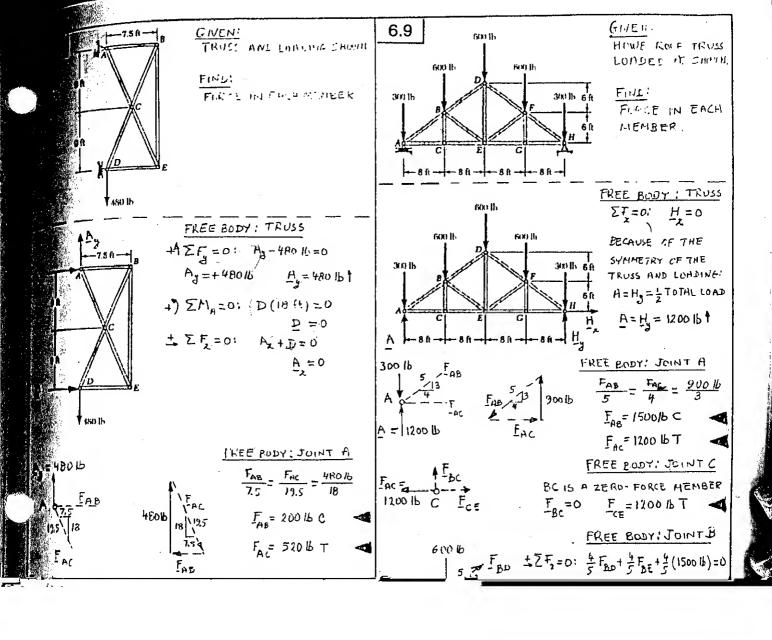
HAVE .. YEA = EGA: Y(98 460 mm²) = 16447 100 mm²
OR Y=1670 mm

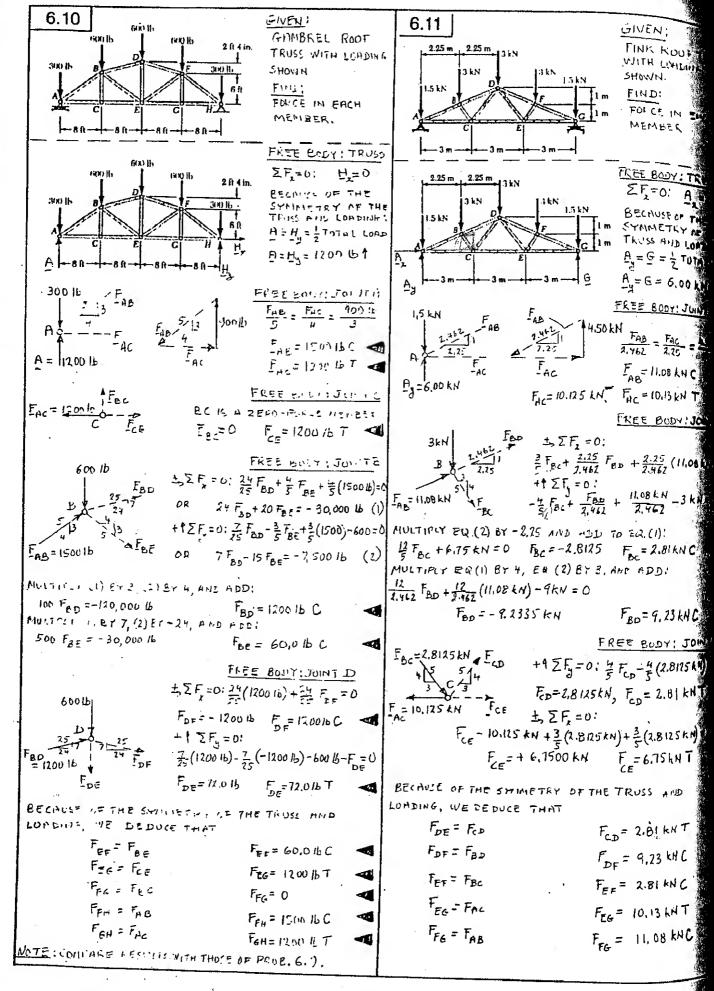
2ΣA=ΣZA: Z(98460 mm²)= 3.300=10 mm or Z=33,5 mm

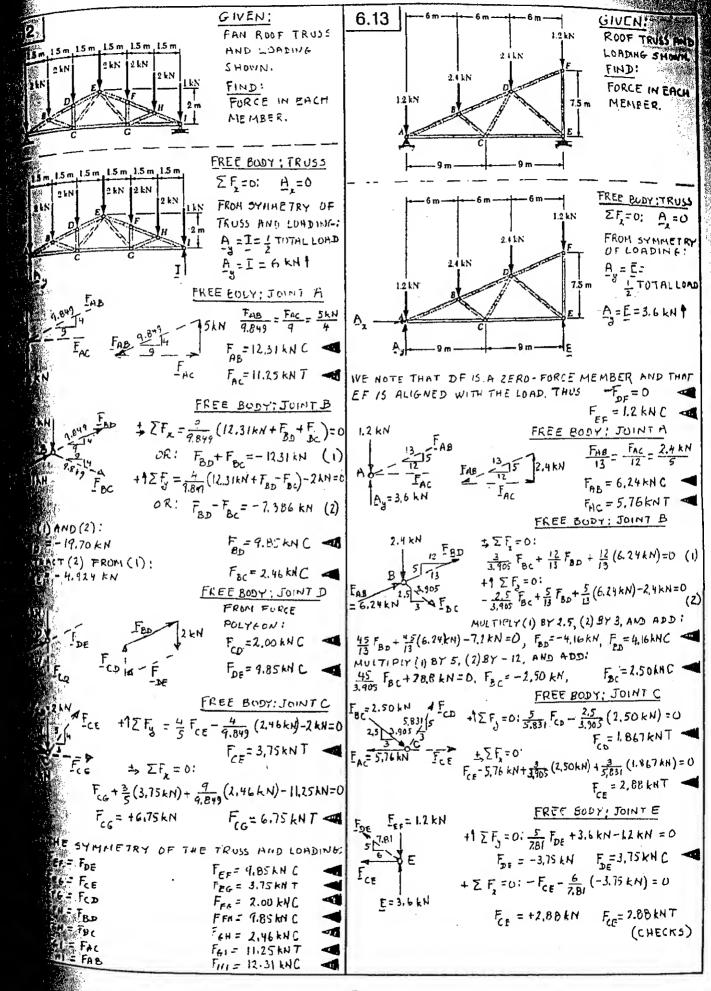


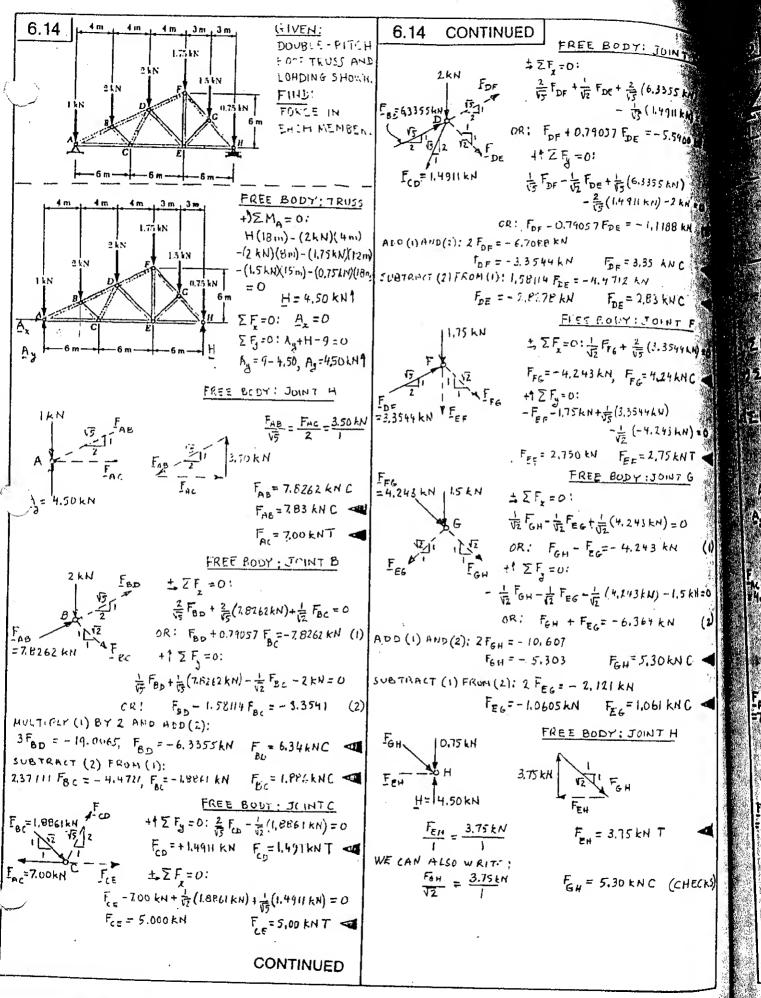


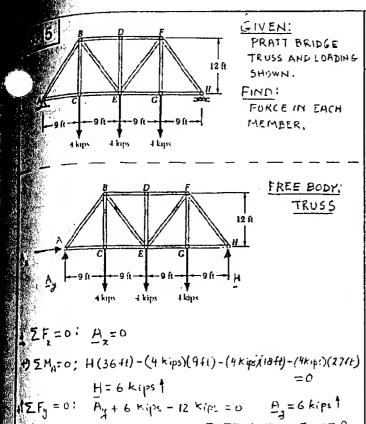


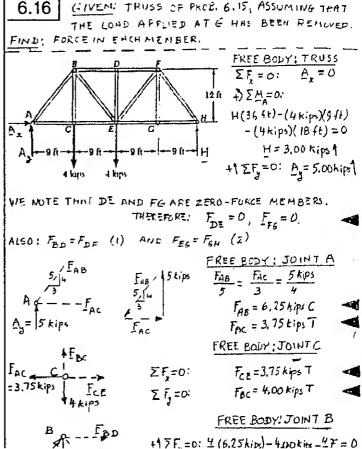


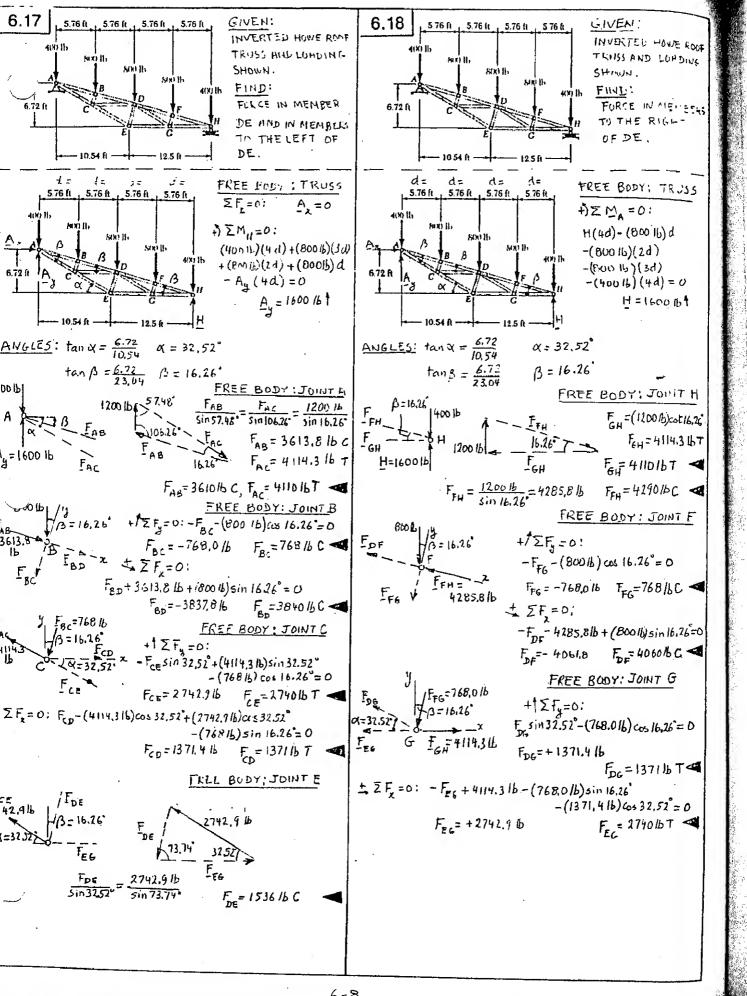












6.1

ALS

K

Α

¥2=

FR

2kr

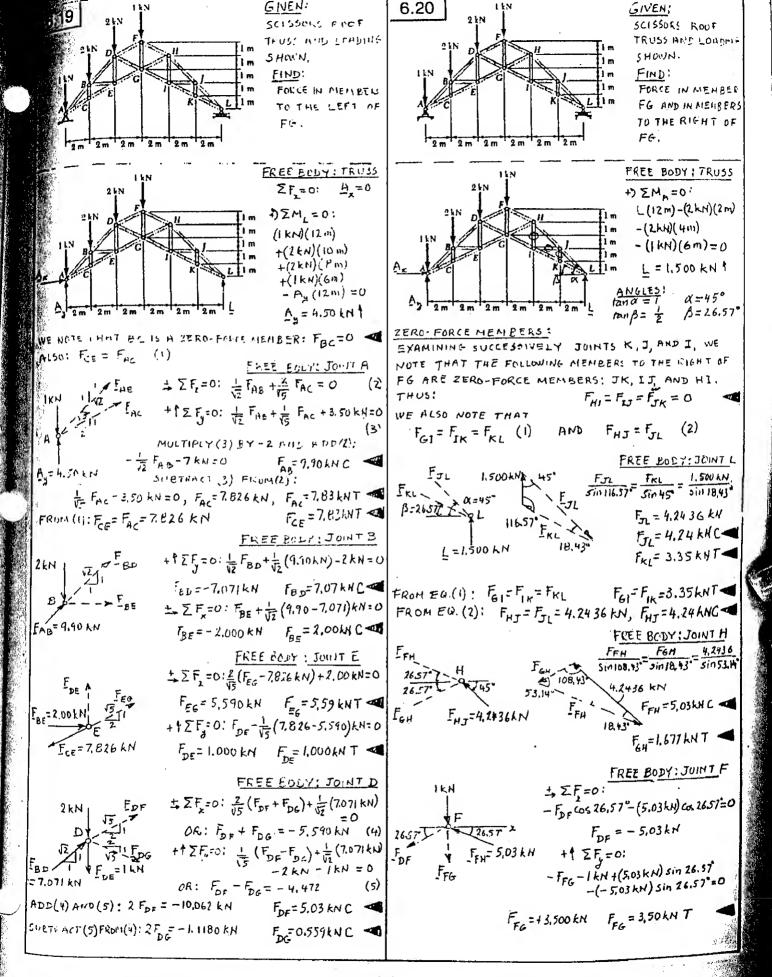
FAR

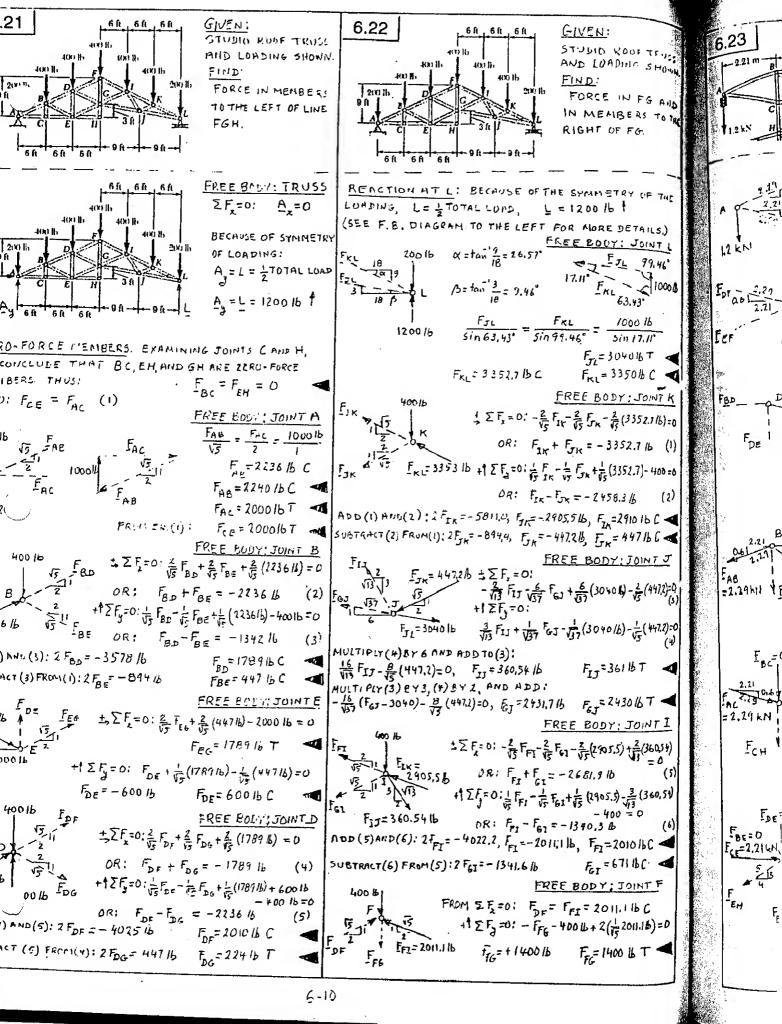
FBE-

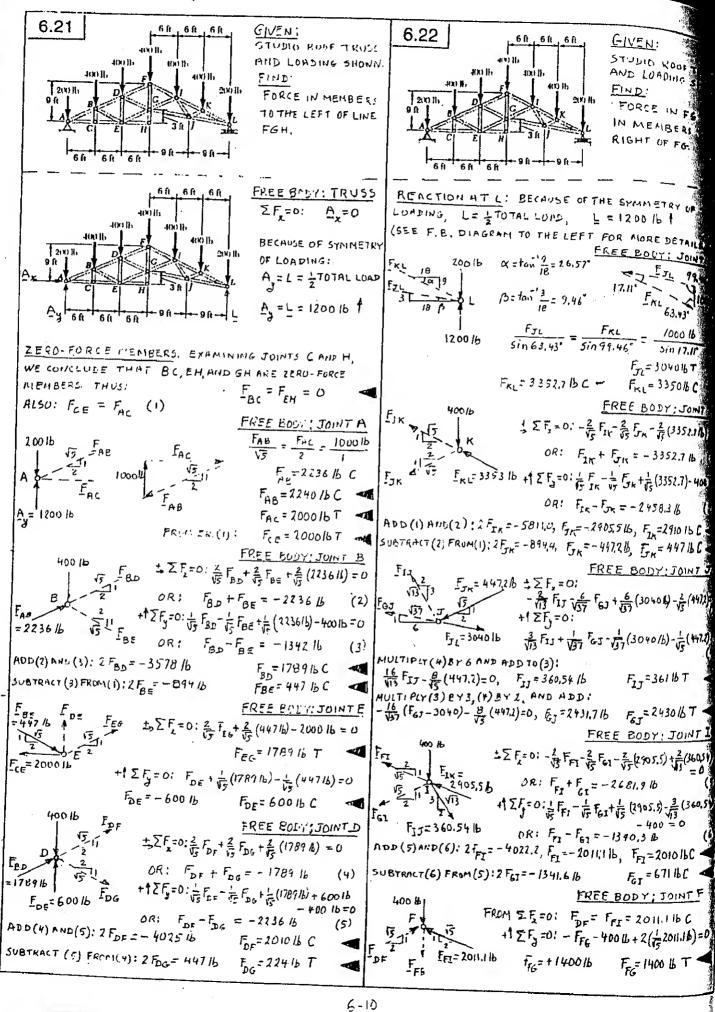
FBE

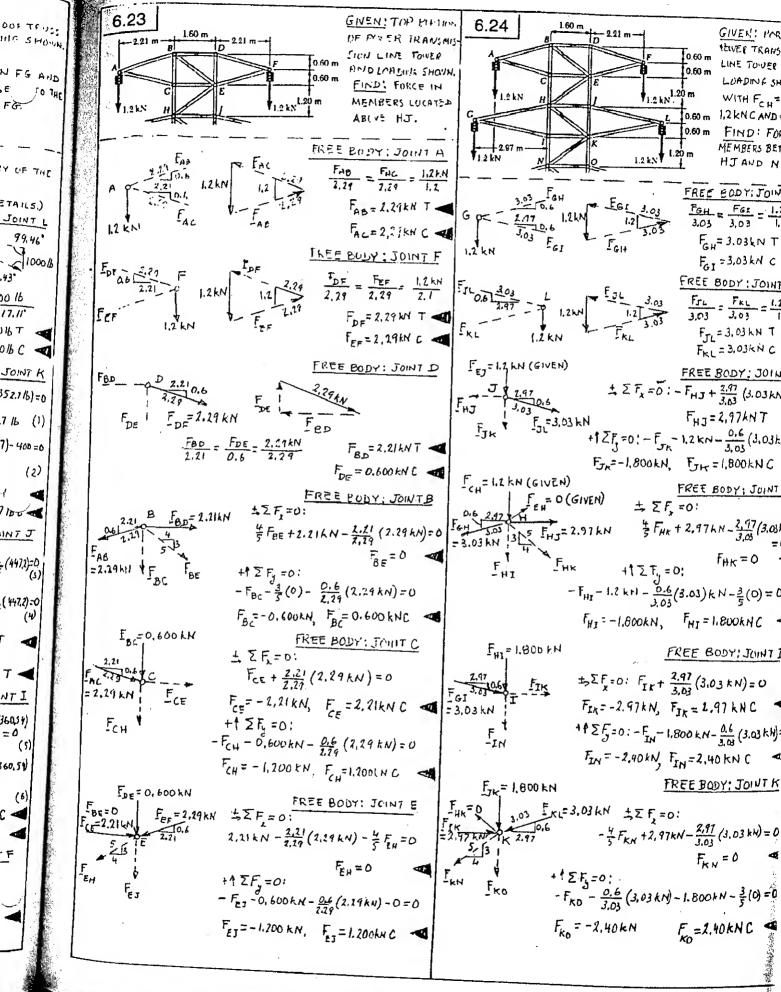
= 7.

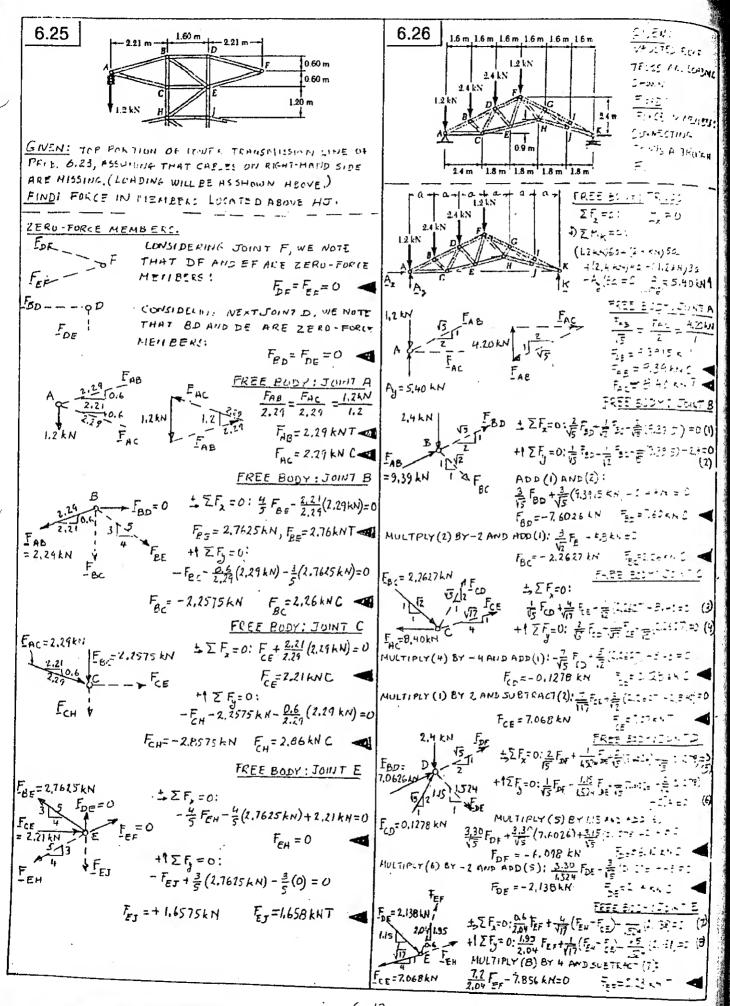
AD

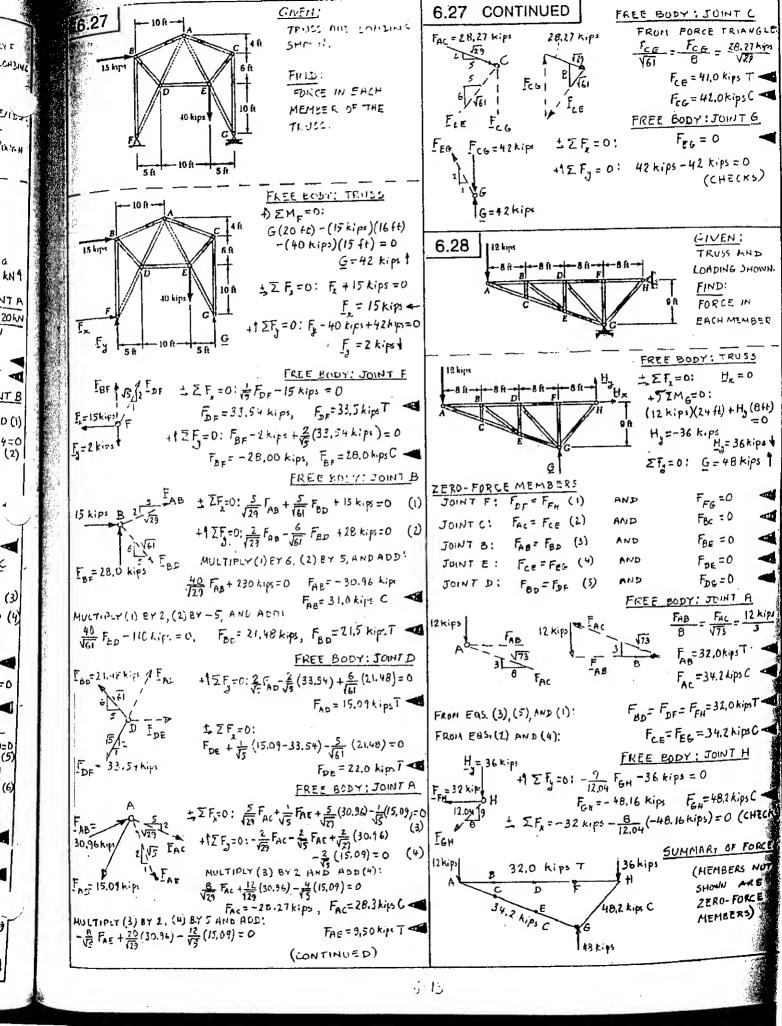










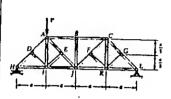


6.29 DETERMINE WHETHER THE TRAINING OF 14021. 6.31 a, 6.31 a, AND 6334 ARE BIMPLE

TRUSS OF PROL. 6.31a

STARTING WITH TURNIGLE ABO AUD ADDITIO TWO MERICENS AT A TIME, WE OBTHIN TOUTS D. E. G. F. AND H. RUT CHEART GO FITHTHER THUS, THIS TRUS 15 127 A SIMPLE TTIBS

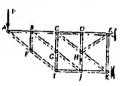
TRUSS OF PROF. 6.32 a



STARTING WITH TRIANGLE HDI AND ADDING THE THIEFE AT A TIME, HE CKTHIN SUCCES-SIVELY JOINTS A, E, J, MWI P, BUT CANT' I GO FURTHER. THUS, THIS TRUSS

IS NOT A SIMPLE TRUSS

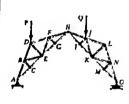
TRUSS OF PROB. 6,33 a



ST IRTING WITH TRIMINGLE EHK AND ADDING THE MEMBERS AT A TIME, WE OBTHIN SUCCES-SIVELY JOINTS D. J. C.G. I, B, F, AND A, THEY COMPLETING THE TRUSS. THEREFORE, THIS TRUE IS A SIMPLE TRUES

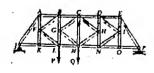
DETERMINE WHETHER THE TRUSPES OF 6.30 PROFLEMS 6.316, 6.326, AND 6.33 & ARE SIMPLE TRUSSES.

TRUSS OF PROB. 6.31 b. STARTING WITH TRIANGLE



ABC AND ADDING TWO MEASERS AT A TIME, WE OBTAIN SUCCES-SIVELY JOINTS E, D, F, G, AND H, PUT CANNOT EN TURTHER. THUS, THIS THE ISS IS NOT A SIMPLE TRUSS

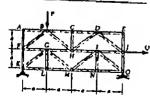
TRUSS OF PICE. 6.32 b.



STARTING WITH TRIANGLE CGH AND ADDING TWO HENBERS AT A TIME, WE OFTAIN SUCCES-SIVELY JOINTS B.L.F. A.K. J, THEN H, D, N, I, E, M, AND P THUS COMPLETING THE TRUSS.

THEREFORE, THIS TRUSS IS A SHIPLE TRUSS

TRUST OF TROP. 6.33 b.



STARTING WITH THINNELS GLM AND ADDING TWO HEMETES AT A TIME, WELLTHIN JOINS K AND+ BUT CHUINT CONTINUE, STANTING INSTEAD WITH TRIANCE BCH, WE SETAIN JOHNT D BUT CAMECT ONTINUE, THE THE TRUS IS HOT A SIMILE TRUSS

6.31

DETERMINE -HE ZERO-FORCE MEMBERS IN AF THE TRUSSES SHOWN FOR THE SIVEN LUNG

T RU 55(a) F.B. JOINT B: FB: JOINT C:

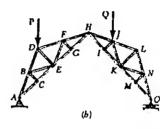
FB: JUNIJ: F₂₇=0 FB: JOINT I: F1,=0

Fr = 0

FB: JUINT N: THU = 0 FB: JOINT M: FLH=0

THE ZERO-PULCE MEMBERS, THEKEHIRE, AKE

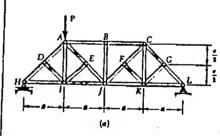
BC, CD, IJ, IL, LM, MN



TRU35(b) FB: JOINT C: FBC = 0 FB: JOINT B: $F_{BE} = 0$ FR: JOINT G: Fra=0 FB: JOINT F: $F_{EF}=0$ TB: JUNT E: F2E = 0 IB: Jan I: Fir=0 FB: JOINTM: FMN = 0 FB:JOINTN:

FKN=0 THE ZERO-FURCE MEMBERS, THEREFORE, ARE BC, BE, DE, EF, FG, IJ, KH, MK

DETERMINE THE ZERO-FORCE MEMBERS IN 6.32 EACH OF THE TRUSSES SHOWN FOR THE GIVEN LOADING

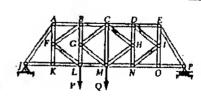


TRUSS (a) FB: JOINT B: F =0 FB: JOINT D: FDI = 0

ABIJOINTE: FEZ = 0 FB: JONTI: FAT =0

FB: JOINT F: FFK=0 FBIJOINTG: FGK=0 FBIJOINT K: FCK = 0

THE ZERO-FORCE MEMBERS, THEREFORE, ARE AI, BJ, Ck, DI, EI, FK, GK



TRU33 (P)

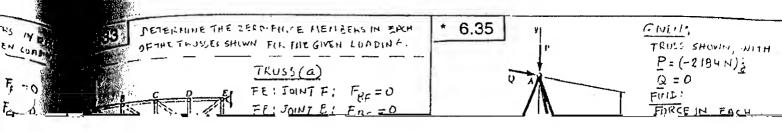
FB: JUINTK: FFK=0

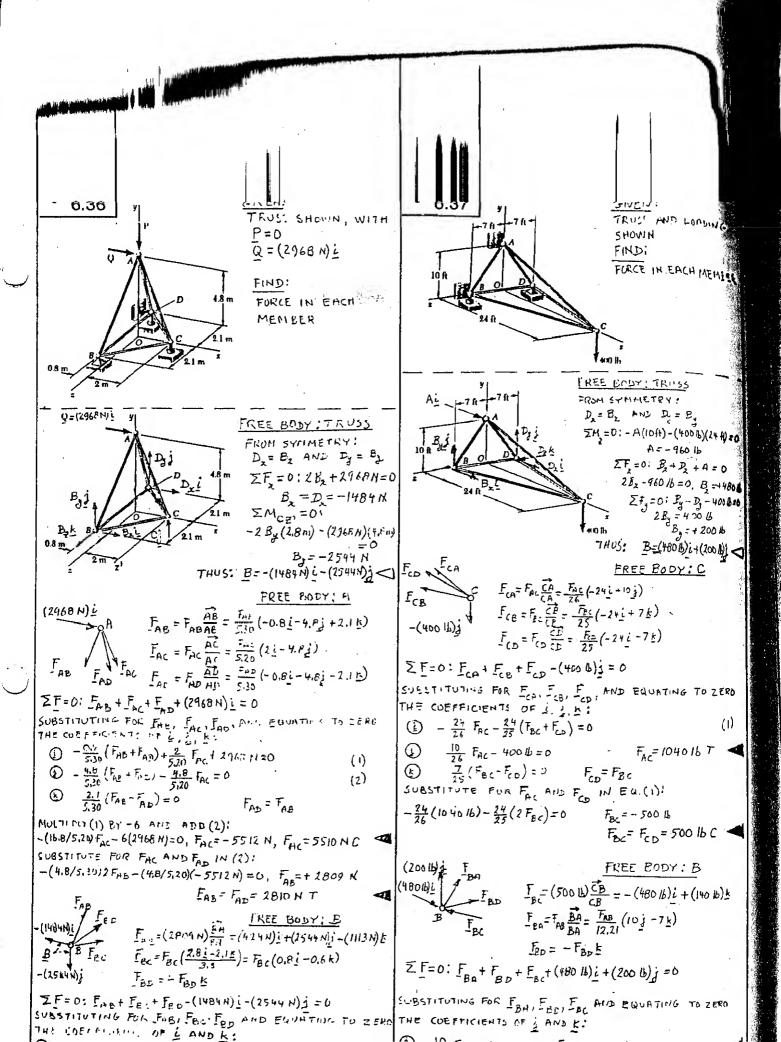
FB: JOINT O: FID=0

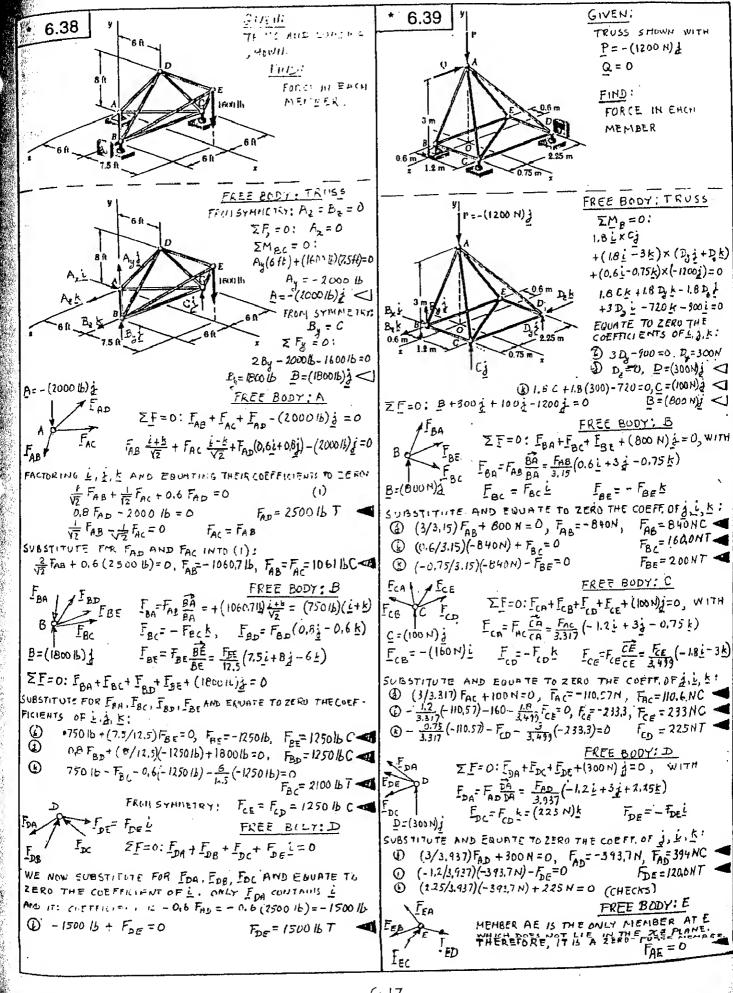
THE ZERD FORCE HENBERS, THEREFORE, ARE FK AND IO

ALL OTHER MEMBERS ARE EITHER IN TENSION OF CONFRESSION .

4

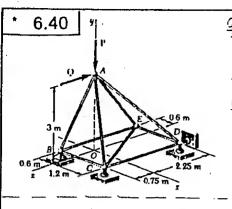






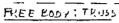
=0

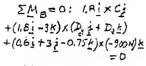
6.41



GIVEN :. TRUSS SHOWN WITH P=0 Q=(-9011)}

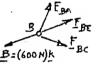
FOKE IN SHICH MEMPER





1.864+1.814 -1.81 +3Dy i +540; -2700 i = 0 EQUATE TO ZERO THE LOEFF. OFL, j, k: 3D4-1700=0 A=900H -1.81 +540=0 D=300H 1,8C+1,8A=0, C=-Dy=-900H

THIM: G=-(900N) ; D=1900N) ;+(300 N) K $\Sigma F = 0: B - 900j + 900j + 300k - 900k = 0$ B=(600N)k <



Q = (-900 11)k

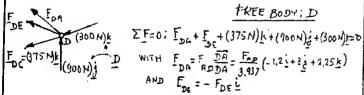
FPLI LODY: B SINCE B IS ALIGNED WITH MENBER BE:

FAB = F = D, F = 600 NT

ZF=0: F +F +F - (900N) j=0, WITH C=-(400H)

SUBSTITUTE AND EQUATE TO ZERO THE COEFT OF & . L , K:

- (3/3,317)FAC-900 N=0, FAE 9951 N.
- (1) 1.2 (995.1) 1.8 FCE = 0, FCE= 699.8N, FCE= 700NC
- (a) $-\frac{0.75}{3,217}(995.1) F_{CD} \frac{3}{3499}(-699.8) = 0$ F = 375NT



SUBSTITUTE AND ENGATE TO ZERO THE COEFF. OF & E. K.

- (3/3,937) FHE + 900N = 0, FHE = 1181,1 N, FAD = 1181NC
- (1.2/3.937)(-1181,1N)-FDE=0 FDE = 360 N T
- (2,25/3,937)(-1181,1H+375 N+300N=0 (CHECKS)



FREE BODY: E MENSER AE IS THE ONLY MEMBER AT E WHICH DOES NOT LIE IN THE XE PLANE, THEREFORE, IT IL A DERO-FORCE, MENLES.

FAE = 0

(275,16) 1 10.08 R

(240 Na k

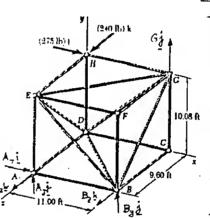
GIVEN.

TRUSS AND LEADING SHI (a) CHECK THUS THUS SIMPLE TRUSS, SOMPLETE CONSTRAINED - AND REACTE STATICALLY DETERMINAN (b) FIND:

FORCE IN ENCH OF THE SIX MEMBERS JOINED

(3) CHECK SIMPLE TRUSS, (1) START WITH TETRAHEDRON BEFG

- (2) ADD MEMBER. BD. ED, GD JOINING AT D.
- 3) ADD MEMBERS BA, DA, EA JOINING AT A.
- (4) ADD MEMBERS DH, EH, GH JOINING AT H. (5) ADD MENEERS BC, DC, &C JOINING AT C
- TRUSS HAS BEEN COMPLETED: IT IS A SIMPLE TRUSS



FREE BODY : TRUSS CHECK CONSTRAINTS AND REALTIONS.

SIX UNKNOWN REACTIOUS. OK - MUREOVER SUPPORTS AT A AND B CONSTRAIN TRUSS TO ROTA TE ABOUT AB AND SUPPLAT AT 6 PREVIOUS

SUCH A ROTATION . THUS

TRUSS IS COMPLETELY CONSTRAINED AND REACHNI

ARE STATICALLY DETERHANT

TETERMINATION OF RENCTIONS!

ZMA = 0: 11 ix (Ei+ Ek) + (11 i - 1,6 k) x 6j+ (10.08j - 9,6 k) x (275i + 240k) = 0 11 By 6-11 By 8+11 Gk+9.6 Gi-(10.08)(275)k+(10.08)(210)i-(9.6)(275)j=0 EQUATE TO ZERO THE COSTS. OF L. J. K.

- (9.6 G + (10.08)(240)=0 G=-25216 G=(-25216)1 11Bz-(9.6)(275) =0
- B = 240 16 11 6y + 11 (-252) - (10.08)(275) = 0, By = 504 B

B=(50416)j-(24016)k < EF=0: A+ (50416) i- (24016)k-(25216)j+(27516)i+(24016)k=0 A=-(27516)i-(25214)j

ZERD-FORCE MEMBERS

THE DETERMINATION OF THESE MEMBERS WILL FACILITATE

FB: C. NRITING ZF=0, ZF=0, ZF=0 YIELDS F =F=F=0

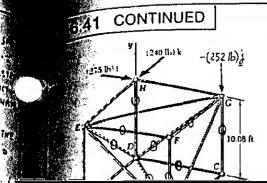
FB.F. WRITING ET = 0. ZT=0, ZT=0 YIELDS FBT=FET=FT=0

FB:A: SINCE A=0, WRITING ZF=0 YIELDS FAD=0 FB:H: WRITING EF = 0 VIELDS

FB:D: SINCE FAD FOD = TOH = 0, WE NEED CONSIDER ONLY WEMBERS DB, DE, AND DG.



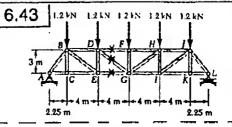
SINCE FOE IS THE ONLY FORCE NOT CONTAINED IN PLANE BOG, IT MUST BE ZERO. SIMILAR REASONINGS SHOW THAT THE OTHER TWO FBD=FD=FD=0 FORCES ARE ALSO ZERO (CONTINUED)



THE RESULTS PATAINED FOR THE REACTIONS AT THE SUPPORT! AND FIG THE ZERN-FORCE MEMPEL: ARE SHOWN ON THE ADJACENT FIGURE.

ZERO-FORCE

ZERO-FORCE MEMBERS ARE INTICATES BY A ZERO("O")

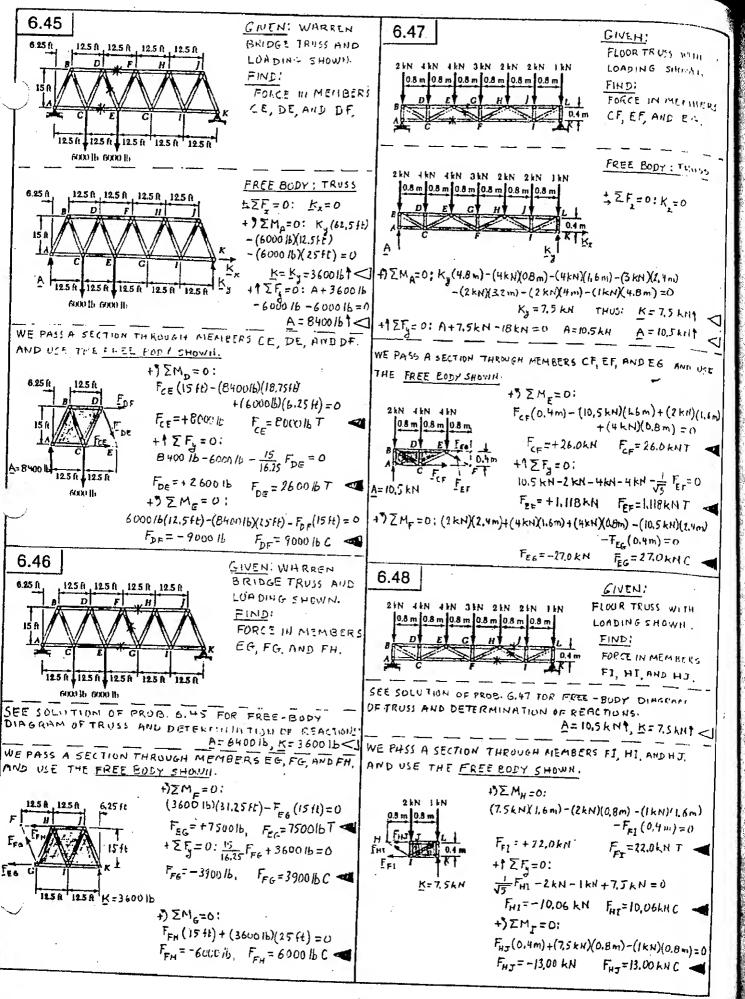


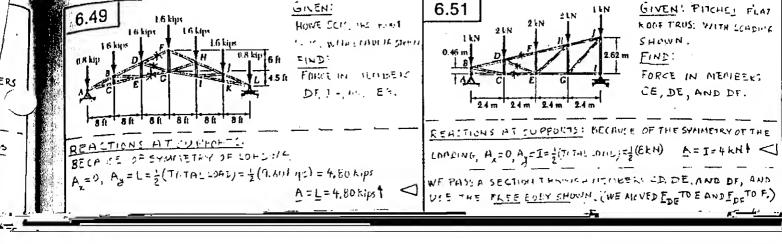
GIVEN' MANSARD
ROOF TRUSS AND
LOADING SHOWN.
FIND:
FORCE IN MEANETRS
DF, DG, AND E4.

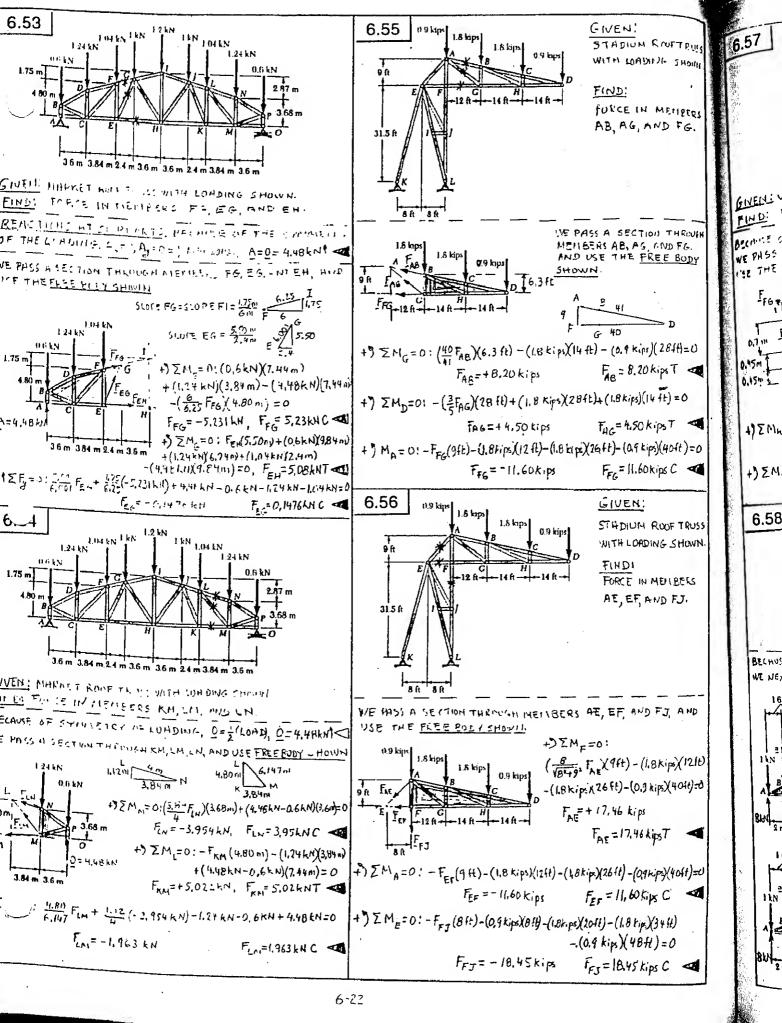
REACTIONS AT SUPPORTS

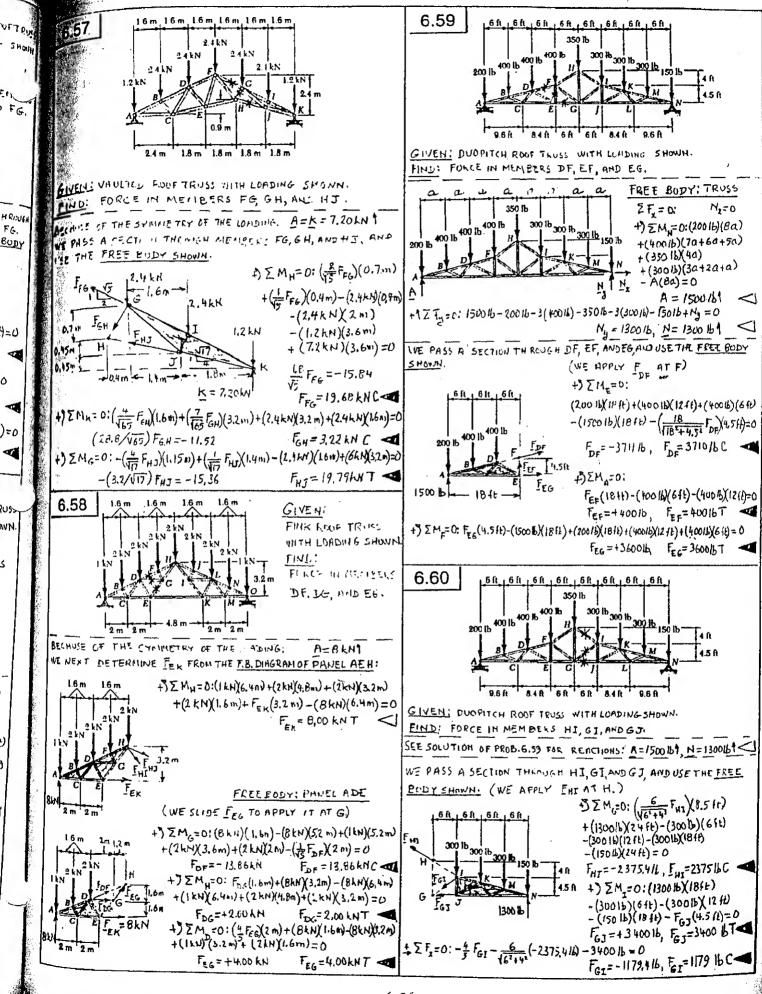
BECHUSE OF THE SYMMETRY OF THE TRUSS AND LOADING,

A=0, A= L= \frac{1}{2} (TOTHL LOAD) = \frac{1}{2} (6kN) A= L= 3kN 1







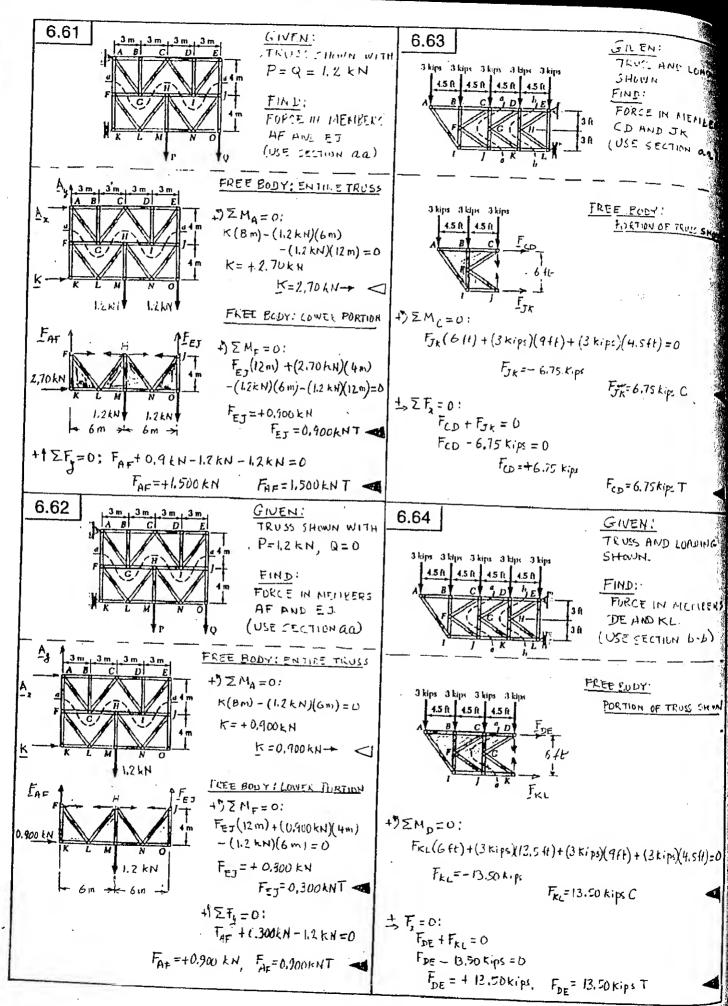


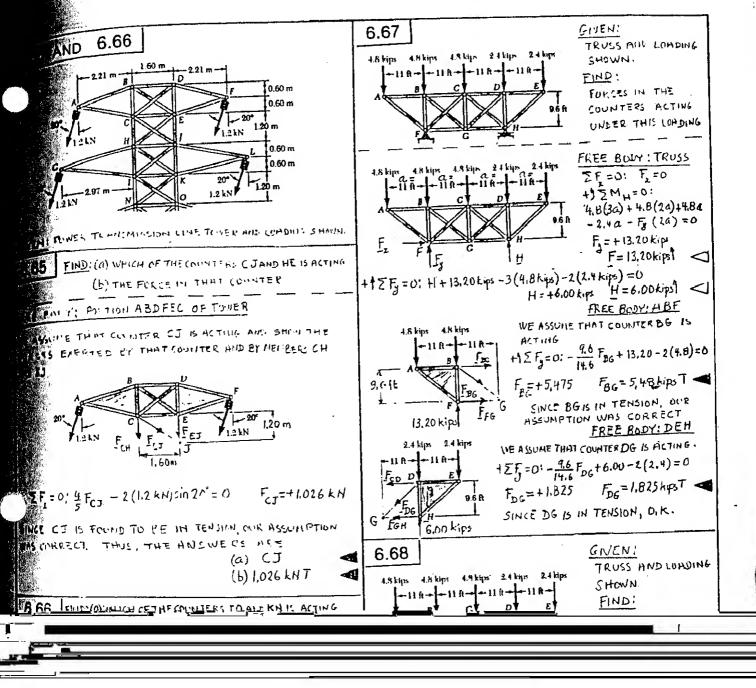
FG.

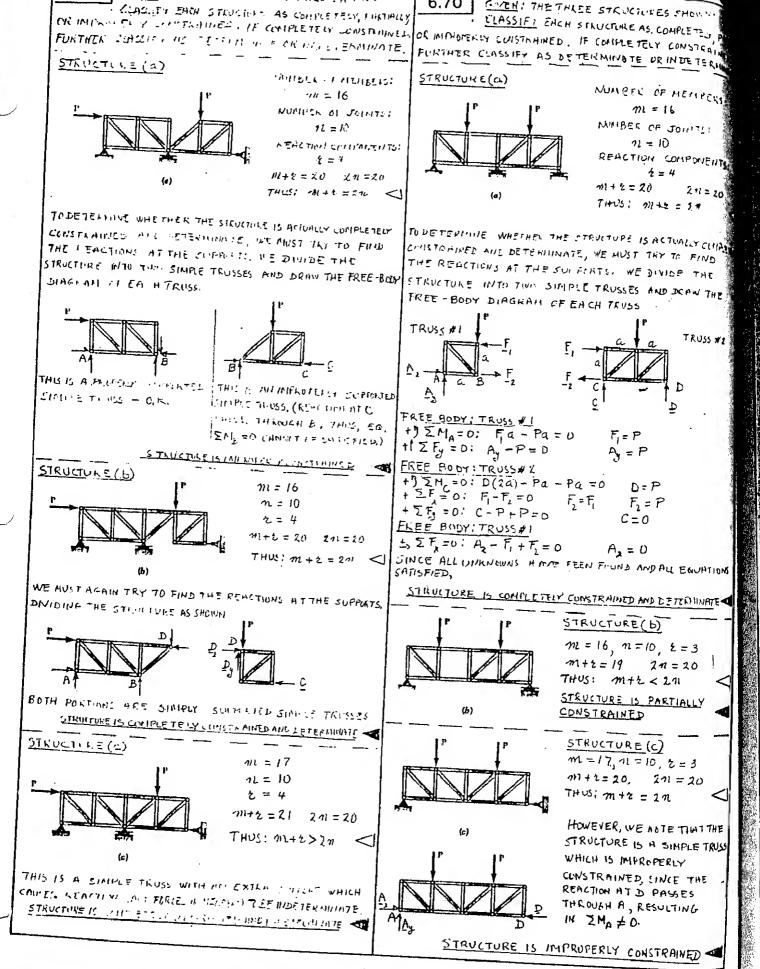
٥

NVA

٤







PARTIN ME D. HIND

∤T5: 20

the life

#2

4 E

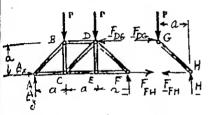
THE

FRUSS

SIVEN: THE THEEE "TE KINDER SHOWN. CLASS IF EACH STRUCTURE AS COMPLETICAL PARTIALLY. THE HEROPERLY TOUSTE HIVEE, IF CHIPLETE Y CONSTRAINED, FURTHER CLASSITY AS DETERMINATE NO INDETERMINATE.

STEUCTOF 5 (4) NUMBER OF MEMETICS 717 = 12 HUMBER OF JOINTS: n = 6REACTION COLUMNERITE! 2 = 4 111+2=16 2n=16 THUS: 11+6=27

TO DETERMINE WHE PITTE THE STUNTILE & ACTUALLY COMPLETELY CONSTINUED AND DETERMINATE, WE MUST TRY TO FIND THE RENCTIONS AT THE SUPPLICTS. INTE PASS A SECTION AND OBTAIN THE SIMPLE TRUST ABODEF INDIRUSER GH.

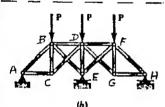


FREE BIDY GH 1) ZM = 0: Pa - FDG a = 0 FDG = P ZF,=0: FFH=FG=P ZF = 0: H= P

FREE BODY: TRUCE ABODE F 15 F, = 0: A, + F = - F = 0 A, + P-P=0 +9 2MA=0! F(31)+Fa-Pa-P1=0 +1 ITy =0: Ay - P-P+3 P=0

SINCE ALL ONKHOURS HAVE FEED FRANCE AND ALL SOURTIONS

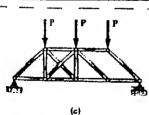
STRUCTURE IS CUMPLETELY CONSTRAINED AND DETERMINATE



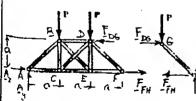
STRUCTURE (b) つい= 13 : カ= 8 , と= 4 71+2=17 21=16 THU: M+2>211

MULEOVER, WE NOTE THAT STRUCTURE IS A SINFLE TRUSS (TOLLOW LETTERING TO CONSTRUCT)

STRUCTURE IS CONFETELY CONSTANIED AND INDETERMINATE



STRUCTURE (c) n1 = 13, n=8, 2=3 n1+6=16 211=16 THUS: 1711+2 = 21 \triangleleft WE PASS A SECTION AND C'BTAIN THE TWO FREE BODIES SHOUN.



FREE EUDY: FG WE RECALL FROM PARTICO FDG= FN = H=7

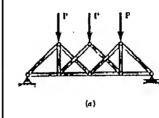
FREE BODY: ABLDET 25HA = Figa - Pa-P(20) = Pa - 3Fa = 2Pa #0 THIS ENUMBRICH EQUITION IS NOT SATISFIED THEREFOR STRUCTURE IS IMPROPERLY CONTRAINED

6.72

CIVEN: THE THREE STRUCTURES SHOUN BLASSIFT EHCH STRUCTURE AS COMPLETELY.

PARTIALITY OR INTERIORERY CONTRAINED, IF LOTIFIED TILLY CONSTRAINED, FURTHER CLASSIFY AS DETERMINATE OK INSETERMINATE

STRULTURE (a)



NUMBER OF HEILBERS! 111= 12 NUMBER OF JOINTS: 12=8 REACTION CLASSONEINTS! r = 3 211:16 m+6 = 15 THUS: 111+6 < 21

STRUCTURE IS PART HELY CONSTRAINED

STRUCTURE (b)

1 = 13, 11 = 82=3 211=16 111+2= 16 THU: 11-12=22

TO VERIFY THAT THE STRUCTURE IS ACTUALLY COMPLETELY CONSTRAINED AND DETERMINATE, WE OBSERVE THAT IT IS A SIMPLE TRUSS (FOLLOW LETTERNIG TO CHECK TAIS) AND THAT IT IS SIMPLY SUPPORTED BY A PIN-AND-BRACKET AND A ROLLER. THUS!

STRUCTURE IS COMPLETELY CONSTRAINED AND DETERMINATE.

STRUCTUPE (C)

m = 13, n=8 2=4 111七二17 211=16 THUS: M+2>21 STRUCTURE IS COMPLETELY

CONSTRAINED AND INDETERMINATE

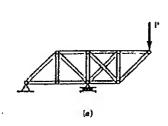
THIS RESULT CAN BE VERITIED BY OBSERVING THIS THE STRUCTURE IS A SIMPLE TRUSS (FOLLOW LETTERING TO CHELK THIS), THEREFIXE KIGID. AND THAT ITS SUPPLEKTS INVOLUE 4 UNKNOWNS.

6.73

GIVEN: THE THESE STENCTURES SHOWN CLASSIFY EACH STRUCTURE AS CONTRACTOR

PARTIALLY, AL IMPROPERLY CONSTLAINED. IF CONFICERLY CONSTRAINED, FORTAGE CLASSIFY AS DETERMINISTE OR IMPETERMINISTE.

STRUCTURE (a)



NUMBER OF HEMBERS: ML = 14

NUMBER OF JOINTS!

REACTION COMPONENTS:

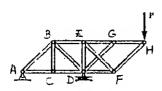
m+t=17 2n=16

TAUS: 111+2722

STRUCTURE IS COMPLETELY COUSTRAINED AND INDETERMINATE

THIS RESULT CAN BE VERITIED BY OBSERVING THAT THE STRUCTURE IS AN OVERRIGID TRUSS (ONE EXTRA MEMBER).

STRUCTURE(b)



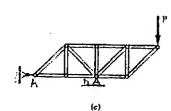
m=13, m=8

か+2=16 21=16 THIL: 111+2=211

WE OBSERVE THAT THE STRUCTURE IS A SIMPLETRUSS (FOLY)W LETTERING TO CHECK THIS) AND THAT IT IS DIMPLY SUPPORTED BY A PIN AID-BRACKET AND A ROLLER, THUS:

STRUCTURE IS COMPLETELY CONSTRAINED AND DETERMINATE

STRUCTURE (4)



m = 13, n = 8

71112=16 211=16

7HOS: 11+2=212

WE OBSERVE THAT THE STRUCTURE IS A SIMPLE TRUSS, BUT THAT IT IS IMPROPERLY CONSTRAINED, SINCE THE REACTION AT A PASSES THRUSH THE SUPPORT D THE EQUATION EM =0, THEREFORE, IS NOT SATISFIED.

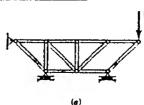
THUS: STRUCTURE IS IMPROPERLY CONSTRAINED

6.74

CLASSIFY EACH STRUCTURES SHOW

CONTINUEN, OR IMPROPERTY CONSTRAINED. IF COMPLETED CONTINUED FORTHER CLASSIFY AS DETERMINED OF INTRETERMINATE.

STRUCTURE (a)



NUMBER OF MEMBERS: THE 12 NUMBER OF JOINTS: THE B

REACTION CONTENTS
2=4

711+2=16

711-16

THUS: MI+2=21

TO VEKIF, WHETHER OF INT THE STRUCTURE IS CONFICTION OF CONSTRAINED AND DETER THE PLANE PASS A SECTION AND CONSIDER THE FREE BODIES ABODEF (A SIMPLE TRUSS) AND

A B C E FEW FEW H

FREE GODY: GH + 7 ZMH=0: FRA-P FF6 = P

\$2 F=0: FEH-FEC

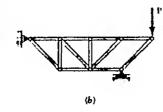
+ \$ 2 Fg = 0; H - P=0 H=7

FREE RODY: TRUSS ABONEF +) $ZM_{A}=0$: $Ca-F_{EH}a=0$ $C=F_{FH}=P$ +> $ZF_{A}=0$: $A_{2}+F_{FG}-F_{EH}=0$ $A_{3}=0$ +> $ZF_{3}=0$: $A_{3}+C=0$ $A_{3}=-C=-P$

SINCE ALL UNKNOWNS HAVE REEN FOUND AND ALL EQUATIONS

STRUCTURE IS CONFLETELY CONSTUAINED AND DETERMINATE

STRUCTURE (b)



111 = 12, 11 = B 2 = 3

22=16

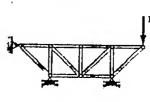
THUS: m+2<211

111+2=15

STRUCTURE IS PARTIALLY

STRUCTURE IS PARTIALLY
CONSTRAINED

STRUCTURE (C)



M1=13 , n=6 セ=4

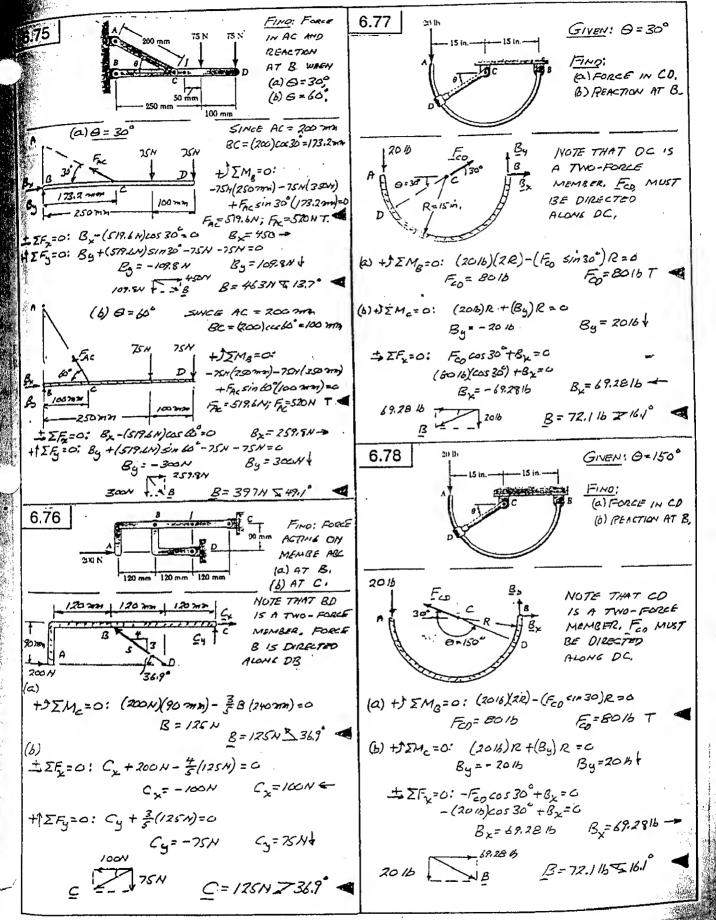
 $n+2=17 \qquad 2n=16$

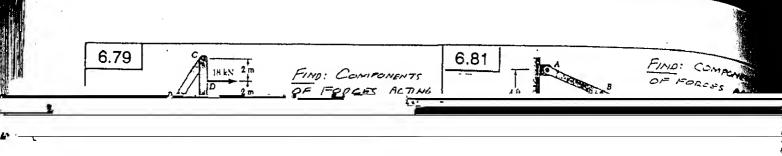
THUS: 11+2 > 272

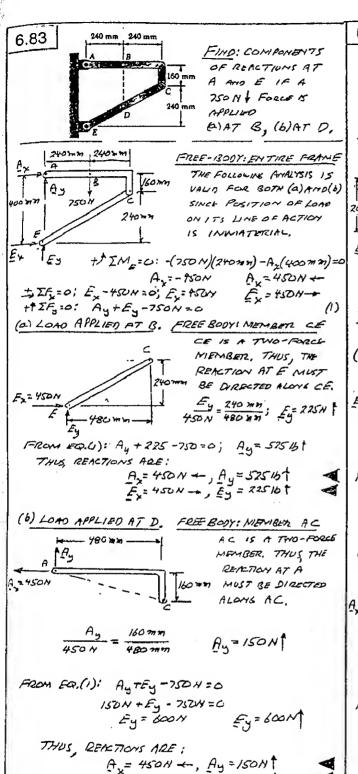
(c)

WE DESERVE THAT THE STRUCTURE IS A SIMPLE TRUSS AND THAT ITS SUPPORTS INVOLVE 4 UNKNOWNS (INSTEAD OF 3 FOR A SIMPLY SUPPORTED TRUSS), THUS

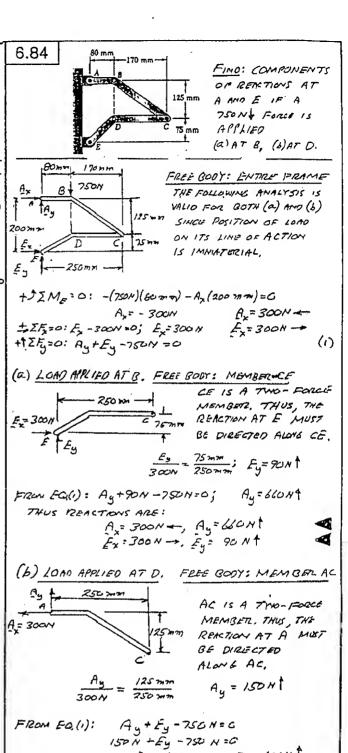
STRUCTURE IS CONTREETELY CONFIRMINED AND INDETERMINITE





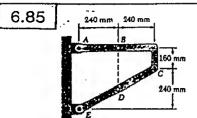


Ex= 450 N->, Ey = 6001

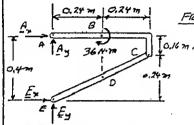


Ey= GOON Ey= GOON ?

THUS, 12 EACTIONS ARE: A = 300N-, Ay= 150Nt Ex= 300N -> , Ey= 600N+



FIND: COMPONENTS
OF REACTIONS AT
A MY E IF A
36 N. 2 COUPLE
IS APPLIED
(a) AT B, (b) AT D.



FREE BOOY: ENTIRE FRAME
THE FOLLOWING

O.16 m. AHALYSIS IS YAUD

FOR BOTH (A) AND (b)

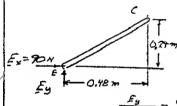
SINCE THE POINT OF

APPLICATION OF THE

CURE IS IMMATERIAL.

 $+ \int I M e^{-Qt} - 36 N \cdot m - A_{\chi}(Q + m) = 0$ $A_{\chi} = -90N \qquad A_{\chi} = 90N + 1$ $+ \int I F_{\chi} = 0; \quad -90 + F_{\chi} = Q$ $E_{\chi} = 90N \qquad E_{\chi} = 9CN - 3$ $+ \int I I F_{\chi} = 0; \quad A_{\chi} + E_{\chi} = 0 \qquad (1)$

(a) COUPLE APPLIED AT B. FREEBODY: MEMBER CE



AC IS A TWO-FORCE
NIEMBER, THUS, THE
REACTION AT E MUST
BE DIRECTED
ALONG EC.

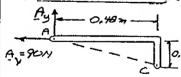
FROM £0(1): Ay + 45N =0
Ay = -45N

Ay = 45N +

THUS, REACTIONS ARE

Ax= 90N-, Ay= 45N+ Ex= 90N-, Ey = 457+

(b) COUPLE APPLIED AT D. FREE BODY: MEMBER AC



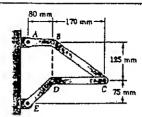
AC IS A TWO-FORES
MEMBER, THUS, THE
REACTION AT A
MUST BE DIRECTED
ALONS AC.

FROM EQ(): Ay+Ey=0
30N +Ey=0

Ey = 30N

THUS, REACTIONS ARE:

Ax= 90N +, Ay= 30N+ Ex= 90N ->, Ey = 30N+ 6.86



FIND: COMPONENTS OF REACTIONS AT A AND E IF A 36 N.M) COUPLE IS APPLIED (a) AT B, (6)AT D.

AY A 26H-M CARE BOOY: ENIRE FRAME

THE FOLLOWING

ANALYSIS IS VALID

FOR BOTH (a) AND (b)

SINCE THE POINT OF

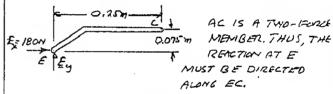
APPLICATION OF THE

EY

COUPLE IS IMMATERIAL,

 $+ \int \Sigma M_{g} = 0$: $-36N \cdot m - A_{\chi}(0.2m) = 0$ $A_{\chi} = -180N$ $+ \int \Sigma F_{\chi} = 0$: $-180N + F_{\chi} = 0$ $F_{\chi} = 180N$ $+ \int \Sigma F_{\chi} = 0$: $A_{\chi} + F_{\chi} = 0$ (1)

(a) COUPLE APPLIED AT B. FREE BODY: MEMBER CE



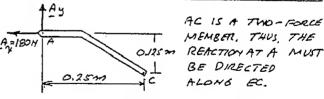
$$\frac{E_g}{180N} = \frac{0.075m}{0.25m} \qquad E_g = 54N^{\dagger}$$

FROM EQ.(1): Ay + 54 N=0
Ay = -54N
Ay = 5

THUS, REACTIONS ARE

Ax= 180N-, Ax=54N+
Ex=180N-, Ey=54N+

(b) CCUPLE APPLIED AT D. FREE BODY: MEMBER AL

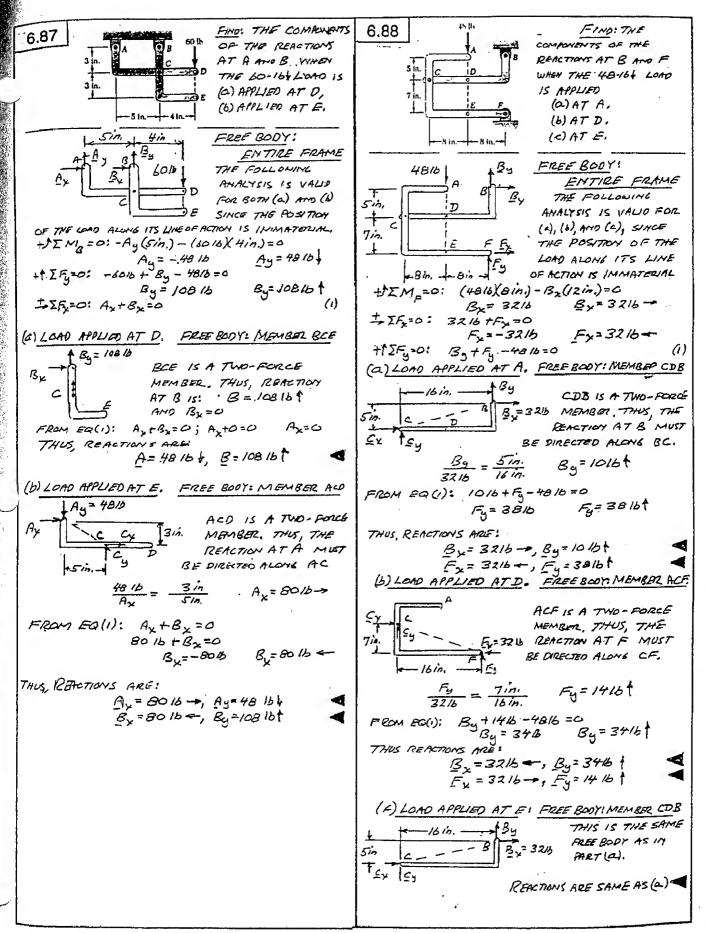


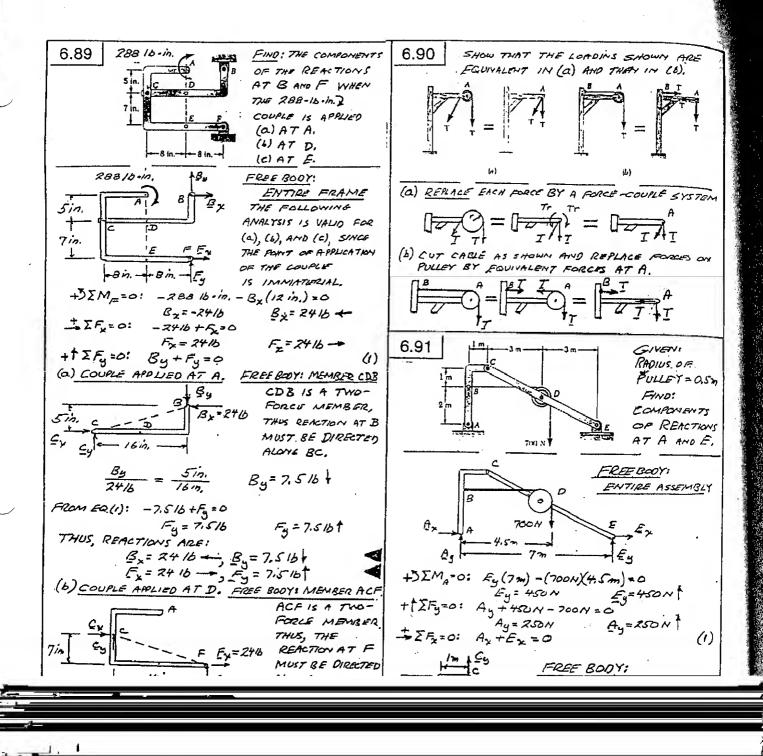
 $\frac{A_{y}}{180N} = \frac{0.125m}{0.25m} \qquad A_{y} = 90N^{\frac{1}{3}}$

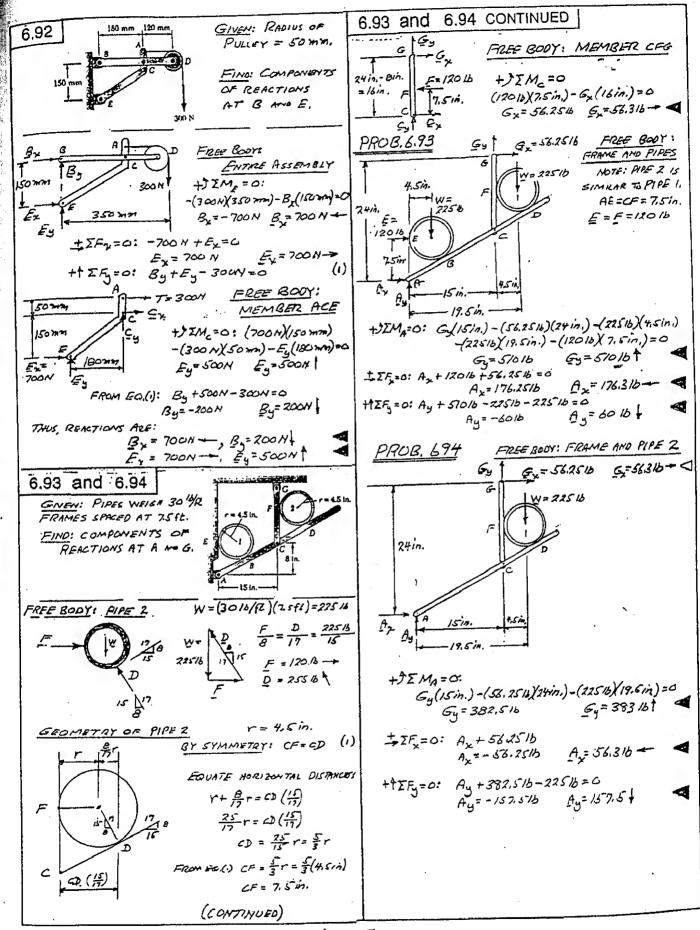
From Ea,(1): Ay+Ey=6
90N +Ey=0
Ey=-90N

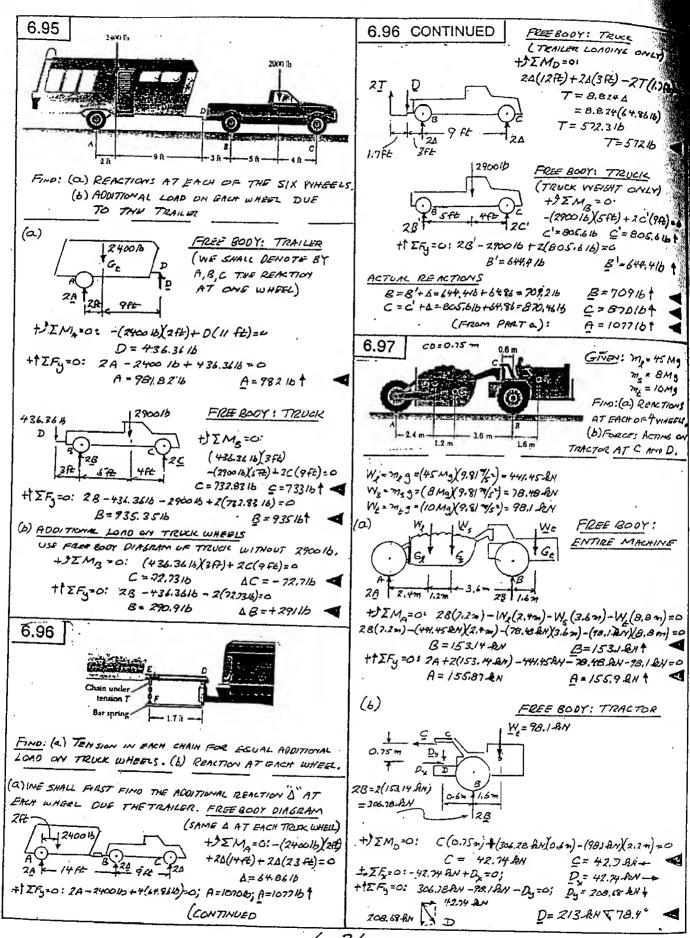
THUS, REACTIONS ARE

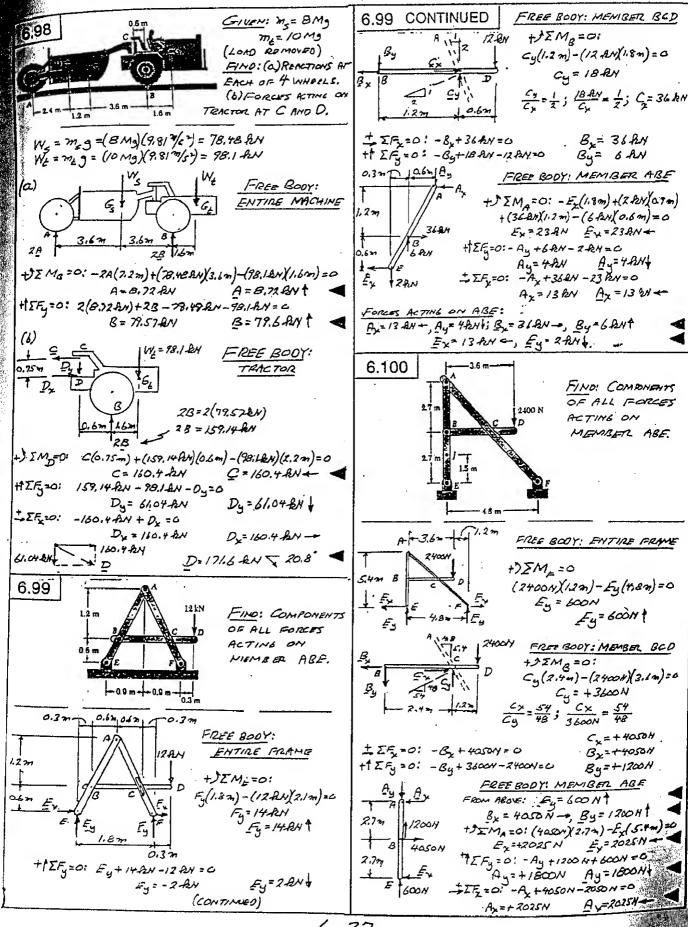
Ex= 180N->, Ey=90N+

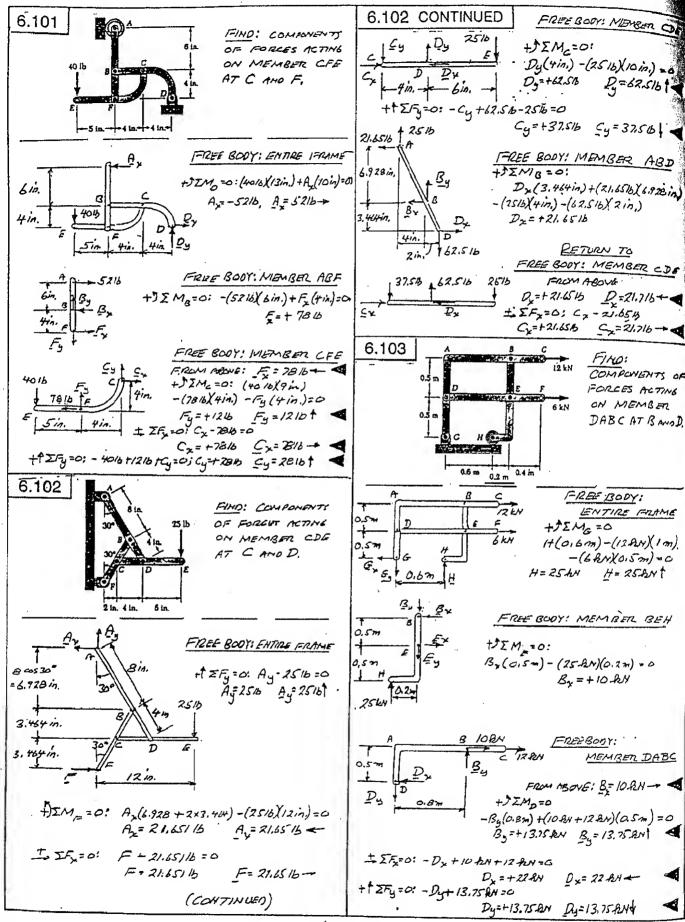


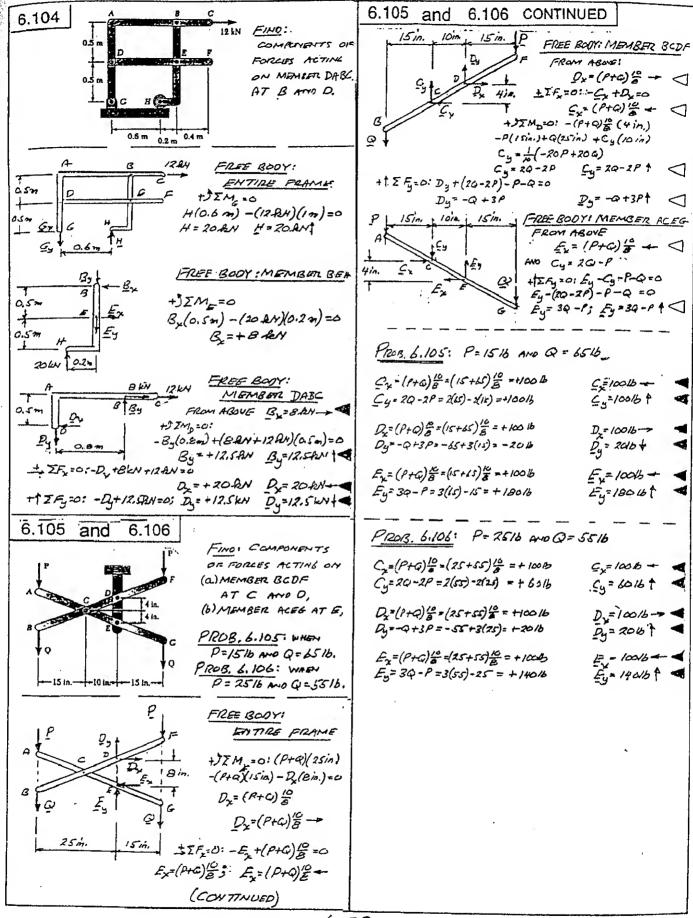


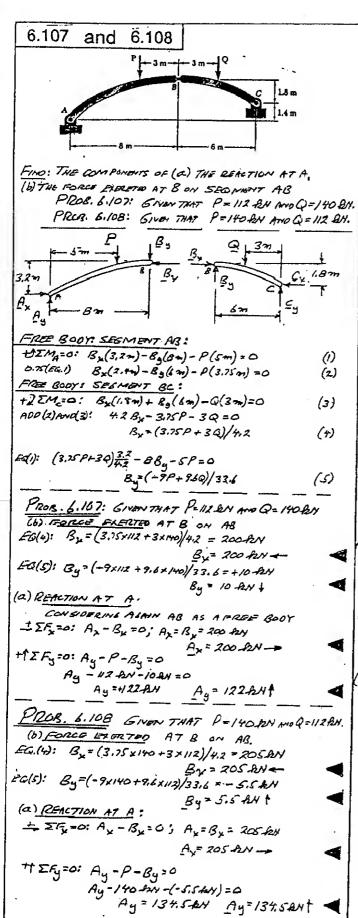


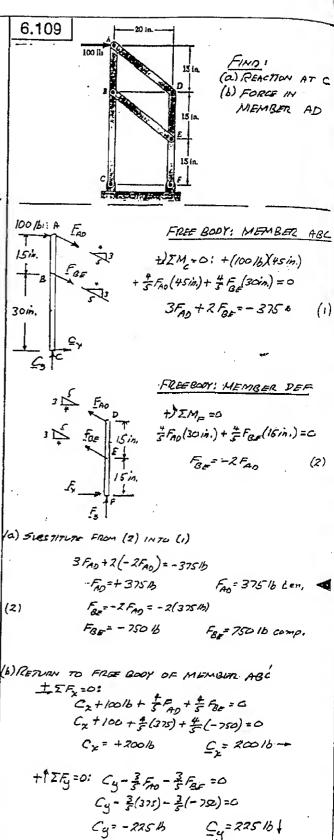






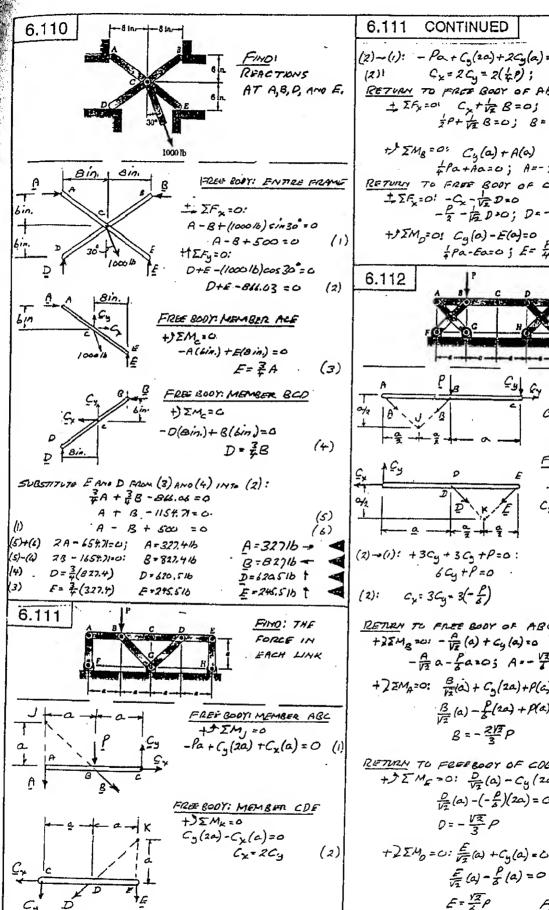




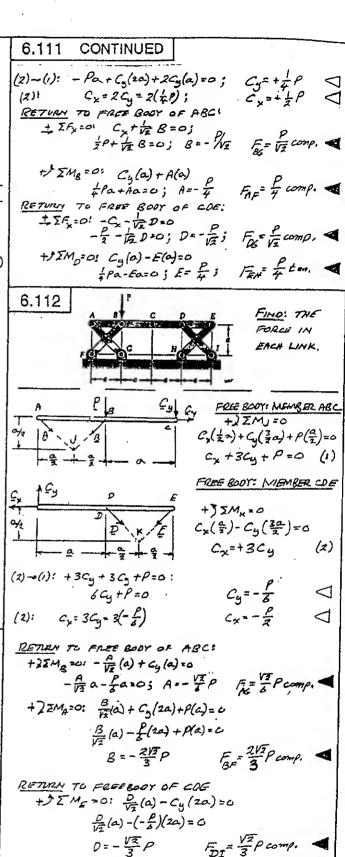


20013

C=30116 V 48.4°



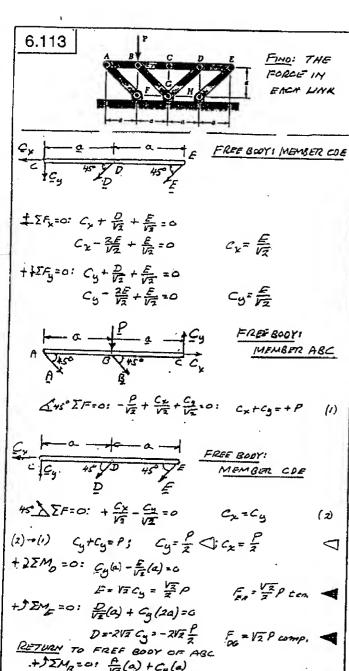
1)



E(a) - f(a) =0

 $E = \frac{\sqrt{2}}{6}\rho$

FEH TP ton.



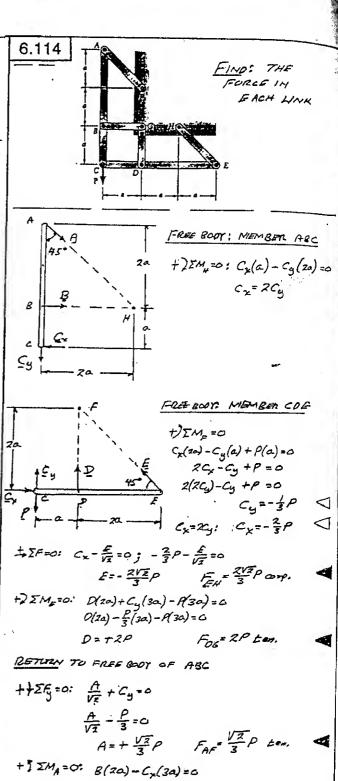
+) \(\frac{A}{V_2}(a) + C_y(a)

+) $\sum M_{=0}$: $\frac{B}{\sqrt{2}}a + Pa - Cy(2a) = C$

B=V2(P- = 2)=0

A=VZ Cy = VZP FAF ZP ton.

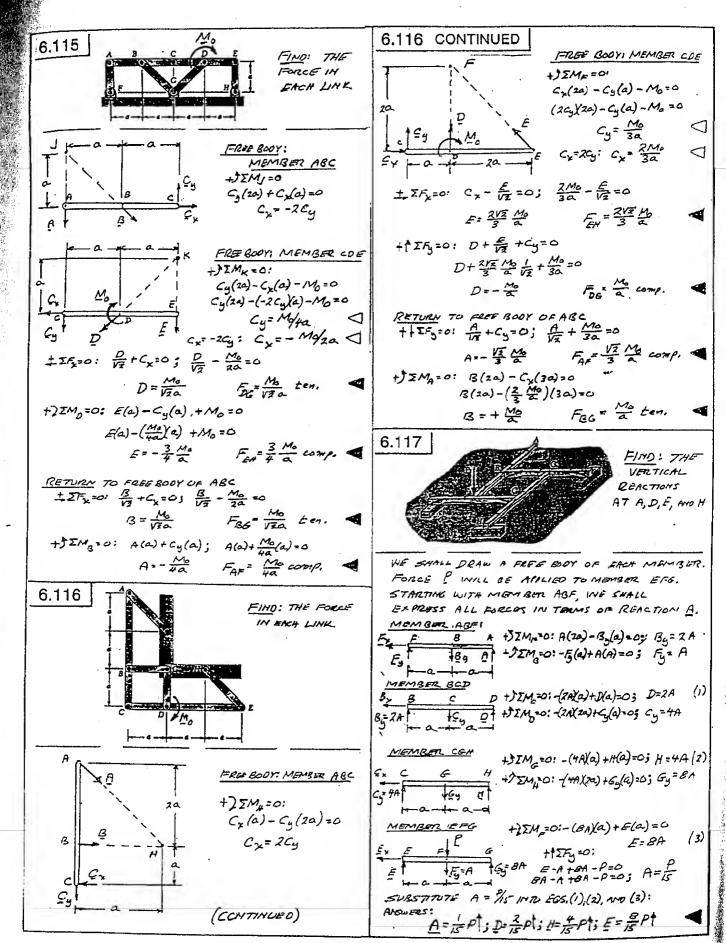
F36=0

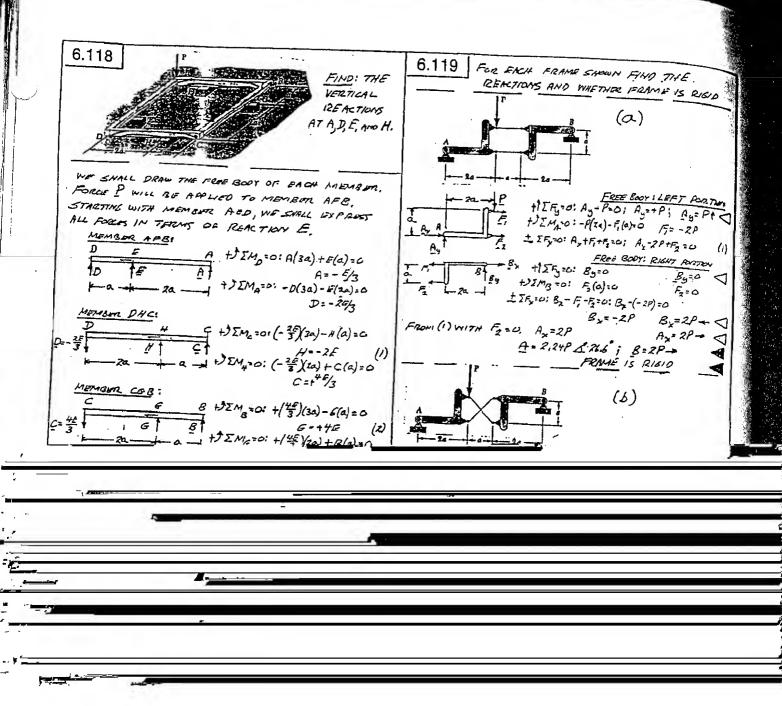


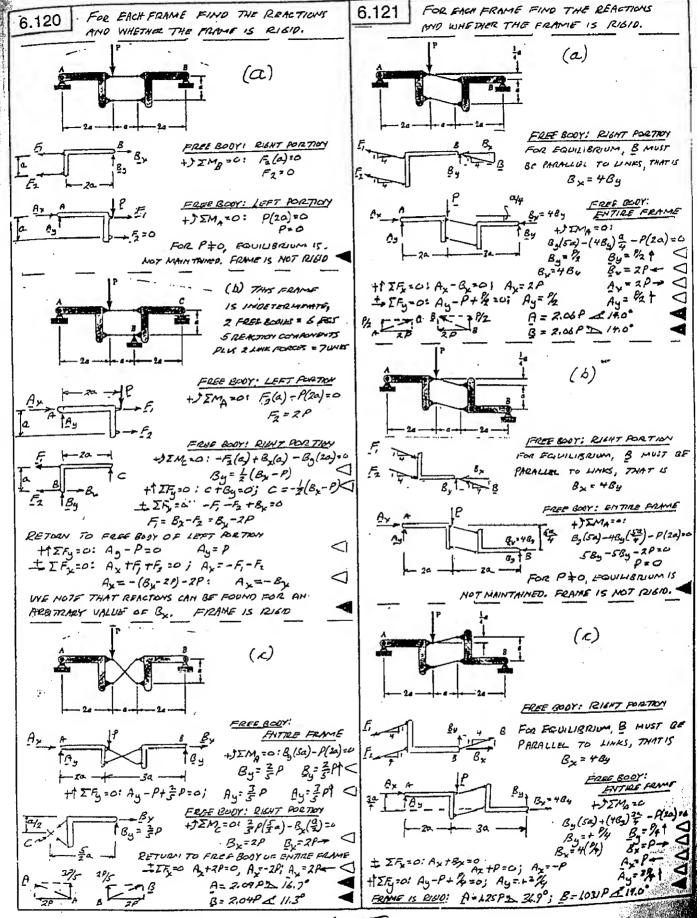
B(2a) + = P(3a) =0

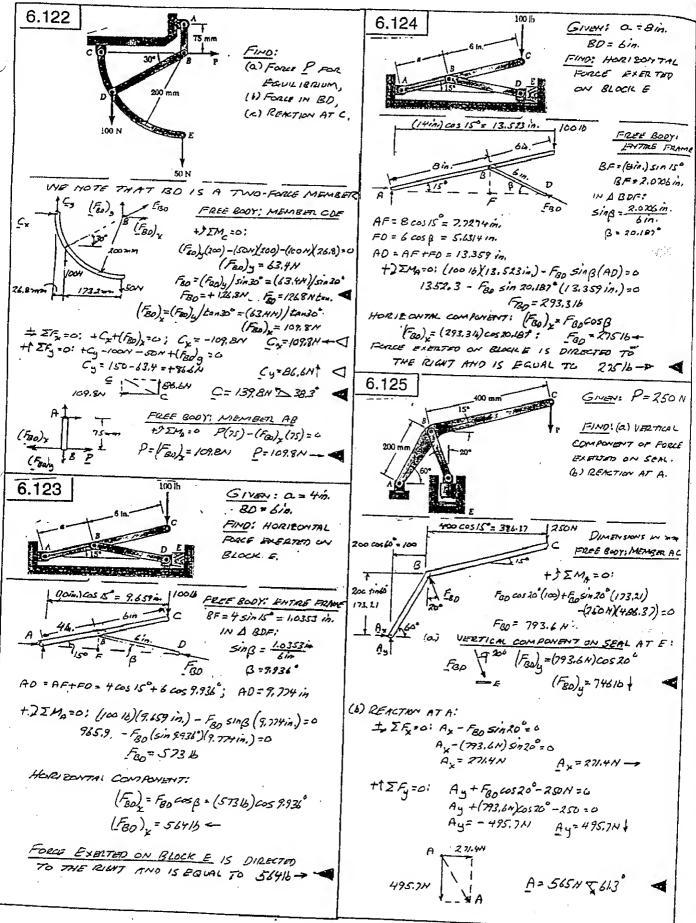
B = - P

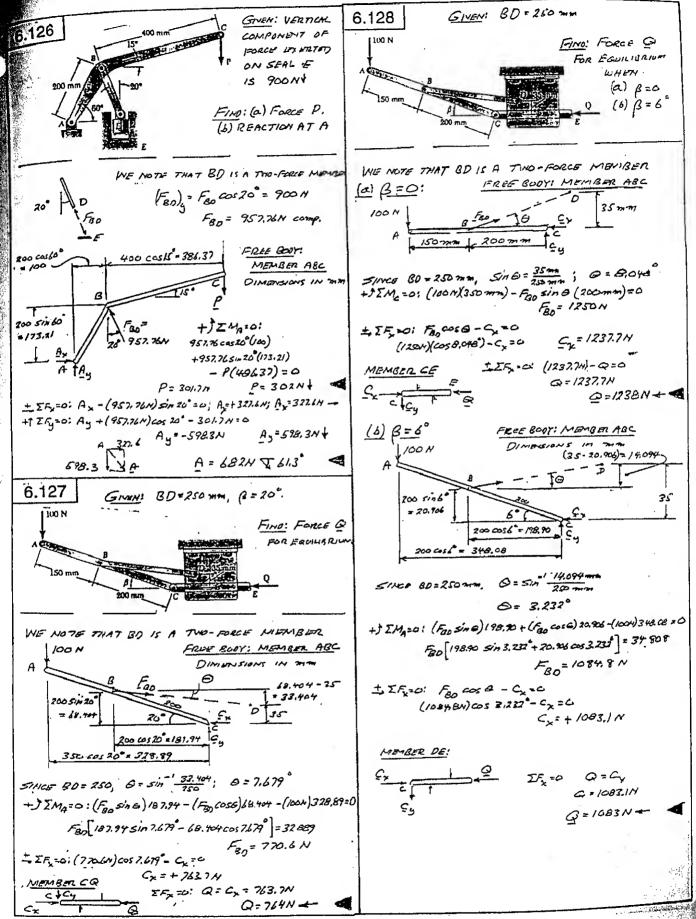
F86 = P comp.

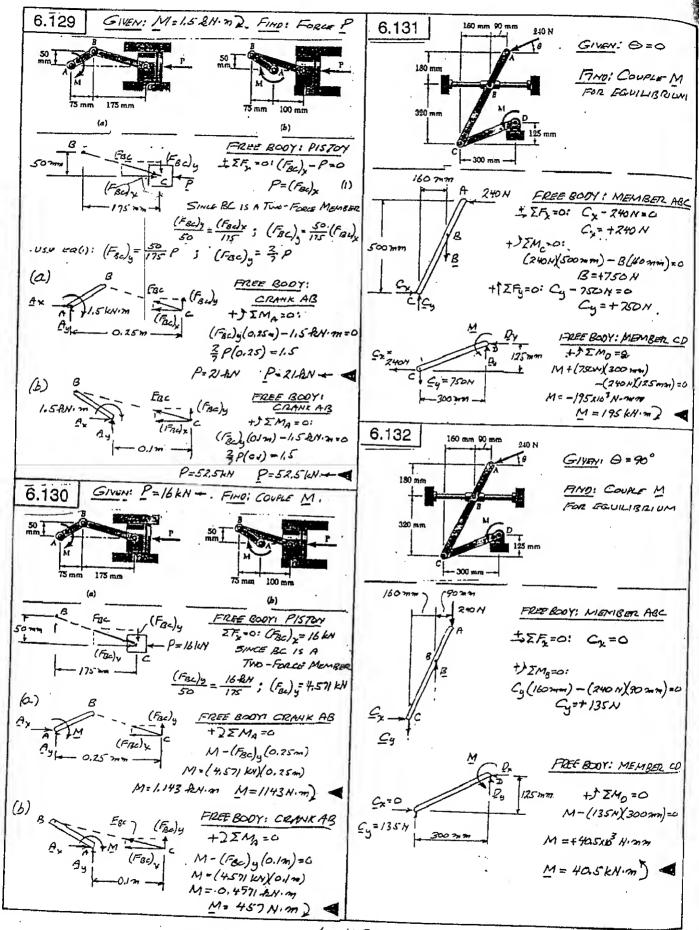


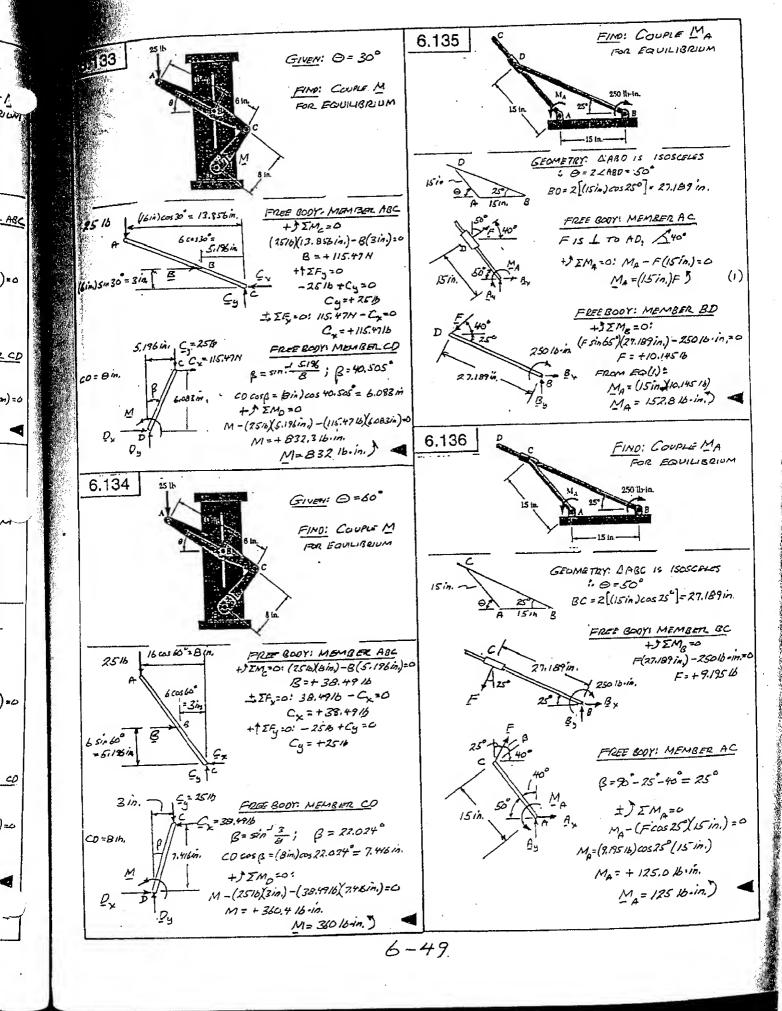


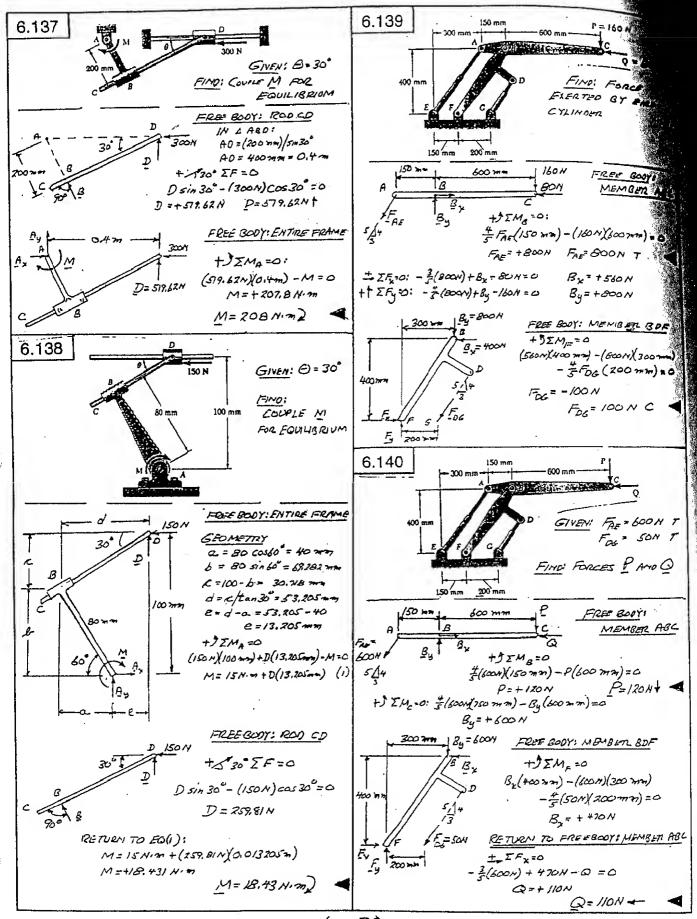


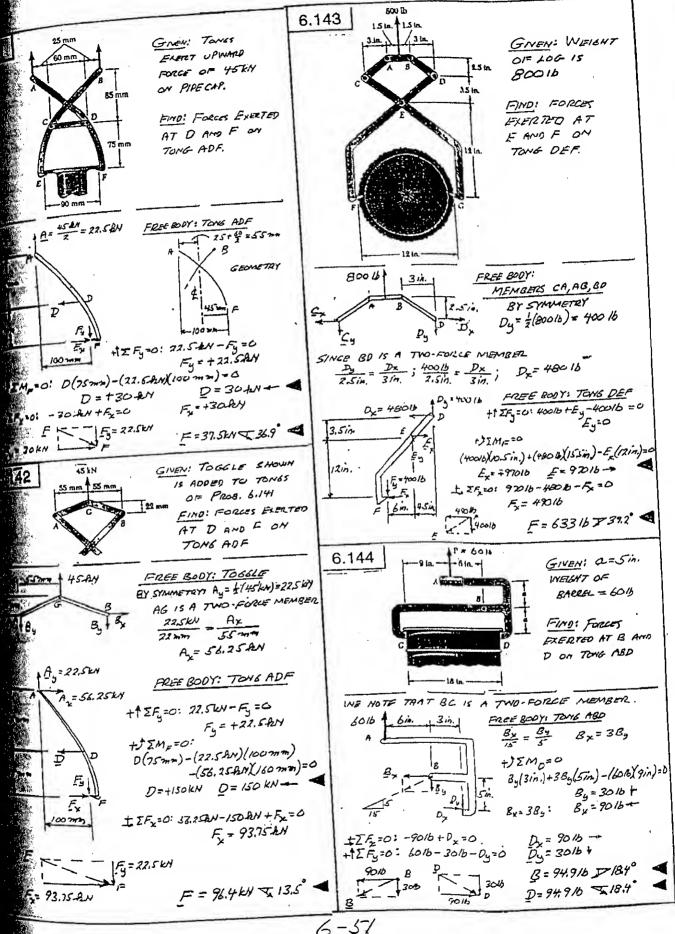


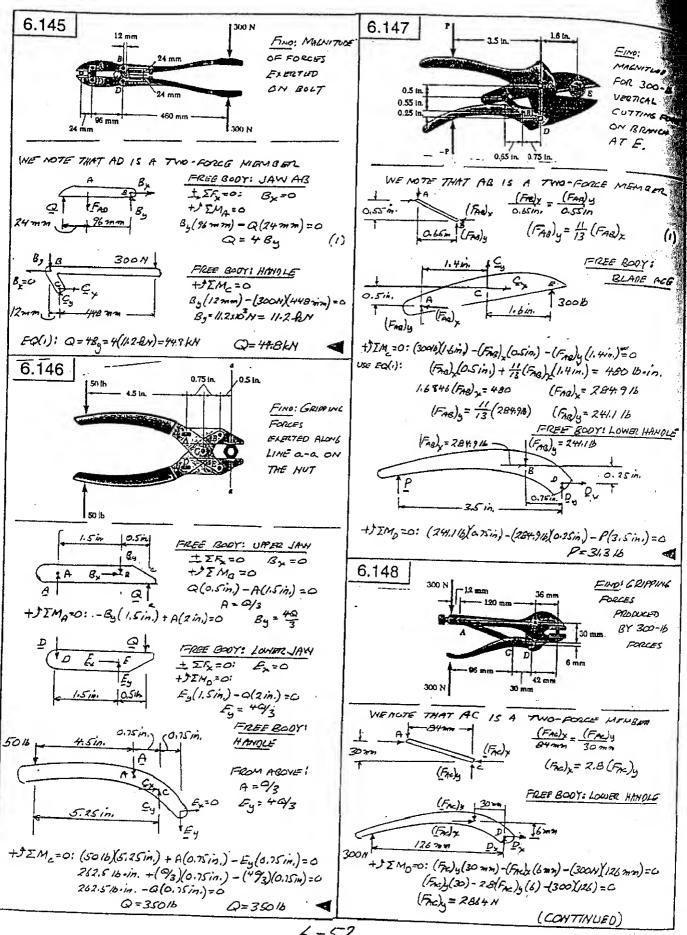


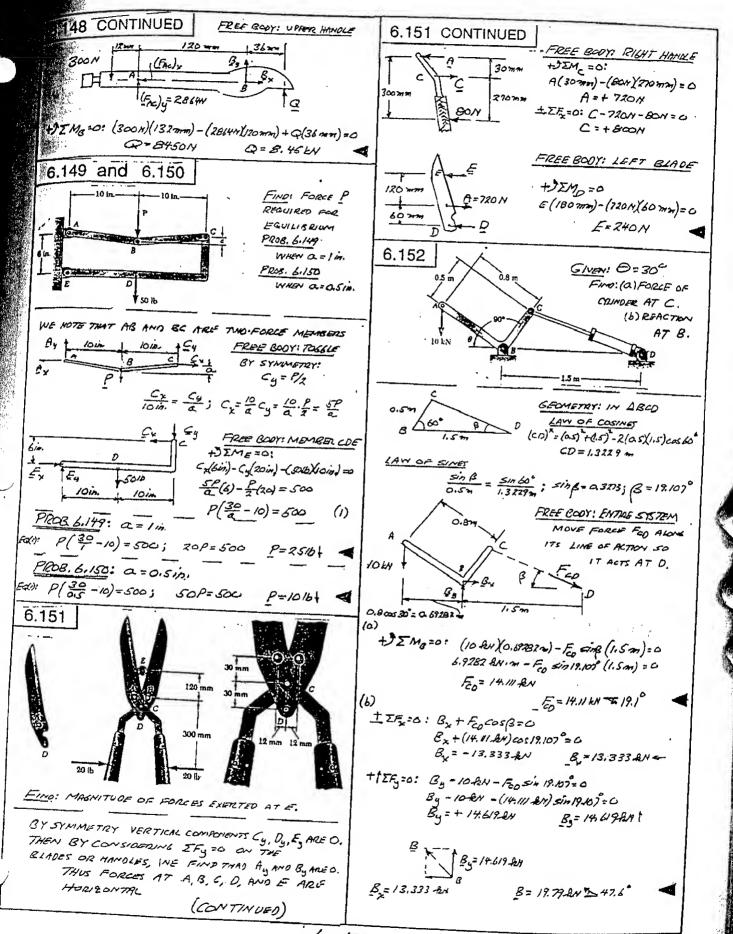


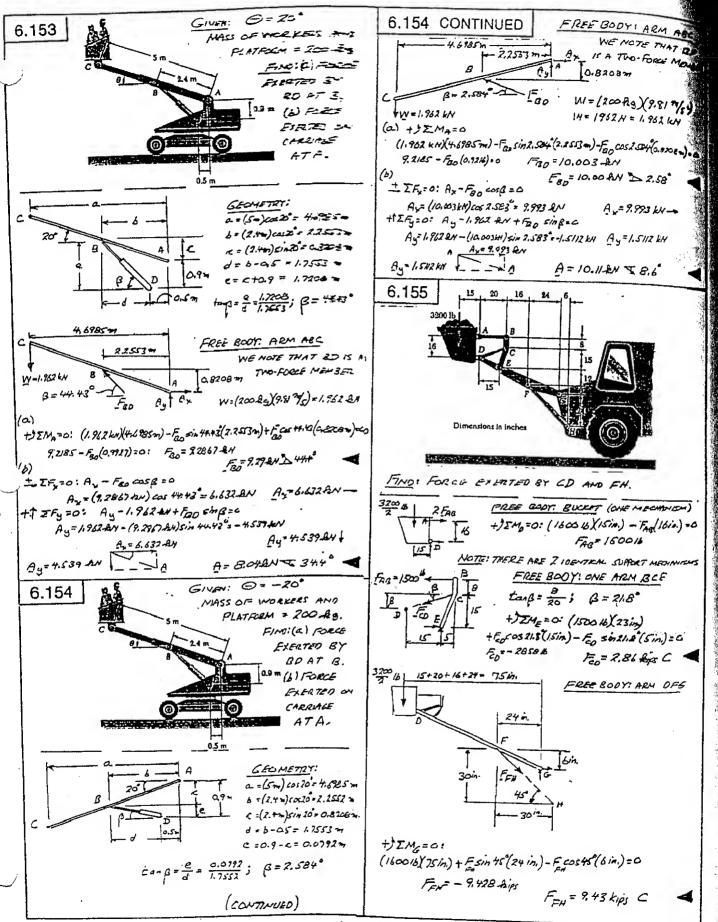


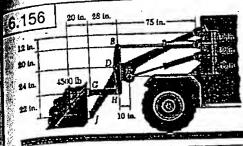




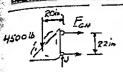




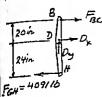




Fino: FORCE EXERTED BY CALCYLMOFR BC (b) CYLINDER EF



FREE BOOK BUCKET +JEMJ = 0: (4500 16)(20in.)-Fel (27in.)=0 FAN = 4091 16

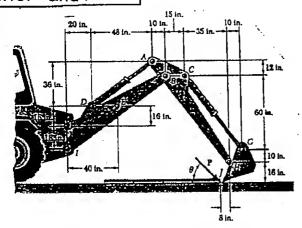


FREE BOOY: ARM BOH + 1 E Mo=0. -4409116 (2+in.) - FBC (20in.)=0 FBC=-490916 FBC=4.91 Kip C €

FREE BOOY: ENTIRE MECHANISM (The ARMS AND CYLHOLDS AFJE) 20+28+75=123 + ZFEF 4500 lb NOTE: TWO ARMS THUS 2 FEE

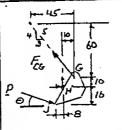
tong = 18in.; B = 15.48 +) IMA=ci (450016)(123 in) + FBC(12in) + 2FEF COSB (24in)=6 (450016)(23in) - (49094)(12in.) +2 FEECOS 15.48 (24in.)=0 FEF = 10:69 kips C FEF= -10,69016

and 6.158 6.157



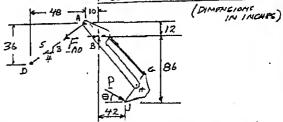
GIVEN: P= 2 lips FIND : FORCE PYENTYD BY EACH CYLINDER PROB. 6.157 WHEN @=45° PROB. 6.158 WHEN G=0

6.157 and 6.158 CONTINUED



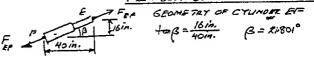
FREE BODY: BUCKET + TIMH = 0 (DIMENSIONS IN INCHES) #Fc6(10)+ 3Fc6(10) + Pcos 0(16) + Psin 0(8) = 0 F= - P(16 cos 0 + 8 sin 6) (1)

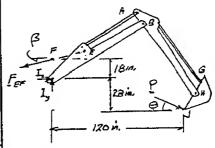
FREE BOOT ARM ABH AND BUCKET



+) IM8 = 0: 4 Fro(12)+ 3 Fro(10) + Prose(06) - Psin 0(42) = 0 FAD = - P (86 cos 6 - 42 sin 6) (2)

EFF BOOY: BUCKET MY ARMS IEB+ABI+





FEE COSB (18in) + PCES (28in) - PSin O(120 in) = 0

$$\frac{P(120 \sin \theta - 28 \cos \theta)}{\cos 218^{\circ}(10)} = \frac{P}{16.7124} (120 \sin \theta - 28 \cos \theta) (2)$$

PROB. 6.157 P= 2 Rips, 0=45°

FO(1): For = - 2 (16 cos45 + 851 45") = -2.42 Kipt

FOG = 2.42 leps C FOG = 7.56 (66 cos 45 - 42 si 45) = -3.99 kps FAD= -3.99 Kips C

EG(3): FEF= 2 (120 50, 45°- 280545) = +7.79 KM

F== 7.79 Kg T

PROB. 6.158 P= Z. R. P. O = 0

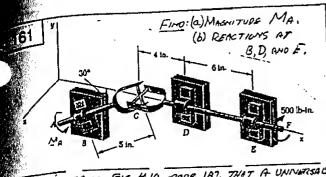
ECO(1): FC6 = - 2 (16 cos 0 + 8 sin 0) = - 2.29 - E/AS Fe6 = 2.29-Pip C

Ed(2): FAO = - 2 (860050 - 42510) = -11.03 Paper

FAD = 11.03 Leips C

FC(3): FEF = 16.7126 (120 500 - 28 cas 6) = - 3.35 Dups

FEF = 3.35 Rps C



ROCAL FROM FIS. 4.10, page 187, THAT A UNIVERSAL DINT EXETS ON MEMBERS IT CONNECTS A FORCE OF HENOWN DIRECTION AND A COUPLE ABOUT AN AMIS THE CROSS DIECE.

1-4in - 6in - FREE BOOY: SHAFT DF · chit GL Doit 13 F . L 1E. 13 - (500 16.m) (M. 45

Mc = 577.35 16 in IM=0: Mc cas 30 - 50016.11.20

FREE BODY; SHAFT BC WE USE HERE X, 4, & MITH Z' ALONG BC الارور وري وروي - الم

IM=0 -M, i'-(51.3516.in)i'+(-5i-)i'x(8,5+8,1)=0 FOUNTE COEFFICIENTS OF UNIT VECTORS TO ZETOS

(1) MA -577.3564=0 'M = 577.75 'MA=577.3516.m.

MA = 577 Bin. 4 Br=0 7

8=0 V-8=0 By=0 3

IF=0' B+C=0, SINCE B=0,

RETURN TO FREE BODY OF CHAFT DE

(NOTE THAT C=0 MO M= 577.3516.in. (577.25 16-10.)(cas 30 1 + sin 28 3) - (500 16-10) + (6in)4x(Ex (+Ey)+Ex)=0 (500/bin) & + (288, 18/bin) j - (500 10 in)

+ (6 in) Ey & - (6 in.) E & = 0 ESLATE COEFFICIENTS OF UNIT VECTORS TO BEDD!

E = 48.16 258.58 16.in, - (6in,)E=0

(1) E3 =0

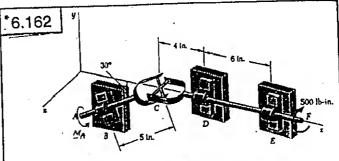
IF=0: C+D+E=0 0+0, 1+0, &+ Exi + (48.116) &= 6

(1) Ex=0

(1) Dy 20

3 De +48.16=0 Da= -48.1 16

REACTIONS ARE: D=-(48.116)-E (48.118) &



GIVENI ROTATE SHAFT WITH CROSSPIECE ATTACHED TO SHAFT OF IS VERTICAL, THEN

FIND: A) MAGNITUDE MA. (&) RENCTIONS AT B.D. AND E. FREE BODY SHAFT DF

1-4in - 6in -D2 4 Czk

M=500 16.in. IMx = 0; Mc-500 10.in, =0 FREE BODY: SHAFT BC -Me=-(500 10.in.)L WE USE HEADE 7, 4, 2 WITH IL ALONG BC Mail

WE RESOLVE - (SOO 16.10.) L INTO COMPONENTS ALONG 2' AND y' AXES: -M= - (500 10 in) (cos30 i + sin30 j') IM=0: Mal' - (50016.10.) (cos30 L'+ sin30 5) + (Sin) L' x (By 3' + B2 2) = 0

Mai' - (433 16.16) L' - (250 16.16) j' + (5/10) By & - (6/10) Be j'=0 EQUATE TO ZERU COEFFICIENTS OF UNIT VECTORS:

MA = 433 16.10. () MA-43316.101=0

B2=-5016 (3) - 250 16-in. - (Sin.) 8=0

Bu, =0 B = - (5016) & REACTION AT B:

IF=0: B-C=0 C== (SD16) & - (5016) B. - C = 0

RETURN TO FREE BOOY OF SHAFT DE:

IMD=0: (61) ix(Ex + Ex + Ex + Ex + - (4in) ix (-5016)-- (500/b.in.) + (500/b.in.) = 0

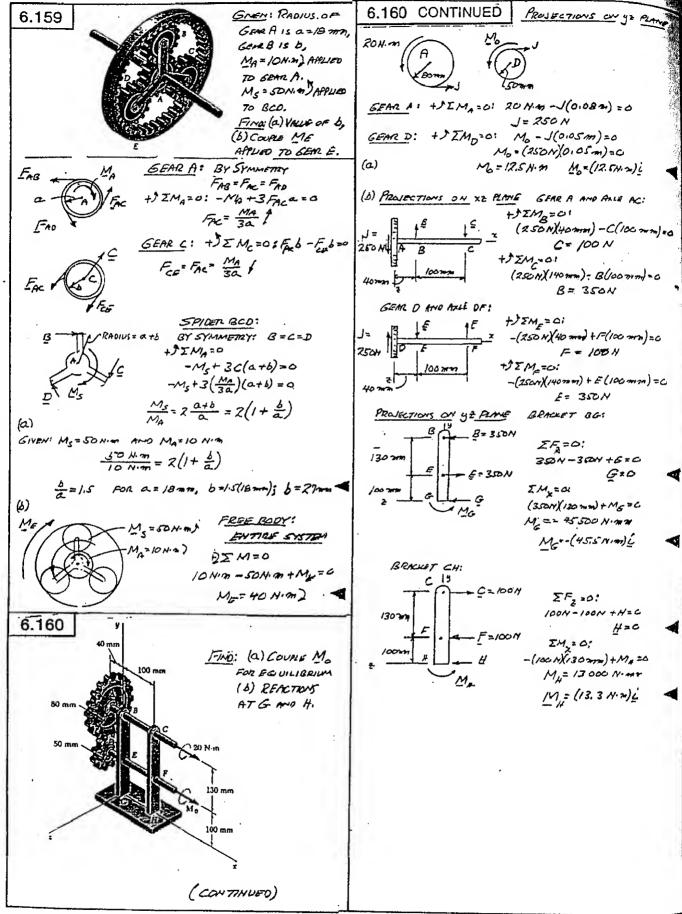
(bin) Eg & - (bin) Ez j - (200 16.in) j = 0

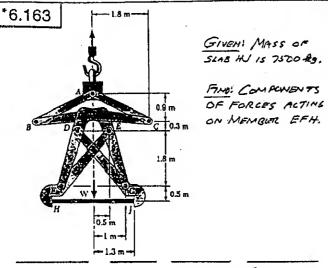
1 -Kin)E2-200 10-in =0 E2=-33,316

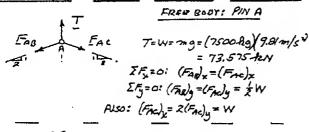
EF+0: C+D+E=0 -(5016) \$ + Dy 1+ De & + Ext - (33.316) \$ =0

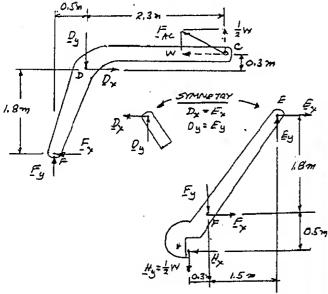
> (-5016 - 33.316 + D2=0 Dz=83,36

B= -(5016)& REACTIONS ARE: D= (83,316) & E = -(33,316) A









FIREE BOOY: MEMBER COE +) [Mn=0: W(0,3) + 1/x w(2.3) - Fx(1.8) - Fx (0.5m)=0 OR: 1.8 Fx + 0.5 Fx = 1.45 W (i)

Dx - Fx - W=0; OR Ex-Fx = W (z)

+ 1 2Fg=0: Fg-Dy+ 1 W=0; OR Fy-Fg= 1 W (3) FREE BODY: MEMBER EFH

+) \(\times M_{1} = 0: \F_{2}(1.8) + F_{3}(1.5) - H_{2}(2.3) + \frac{1}{2}W(1.6m) = 0 OR 1.8Fx +1.5Fy = 2.3Hy -0.9W (4)

(5) I Sty=0: Ex+Fy-Hy=0 OR Fy+Fy=Hy

(CONTINUED)

* 6.163 CONTINUED

2/2=H2-W SUBTERT (2) FROM(5): 3.4Fx = 5.25W - 2.3Hx SUB TRACT (4) FROM 3x(1): A00(7) 70 23x(4); 1. 8.2E = 2.95W Fy = 0.35976 W

SUBSTITUTE 1=ROM (B) INTO (1):

(13)(0,35976W) + 05Fg = 1.45W 0.5/= 1.45W-0.64758W = 0.80244W Fy = 1.6049 W

SUBSTITUTE FROM (B) INTO (2):

Ex= 1.3597644 Ex-0,359XW=W;

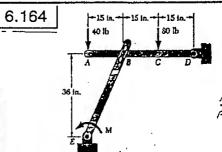
SUBSTITUTE FROM (9) IN TO (3):

Ey = 2.1049W Ey-1.6049W = +W

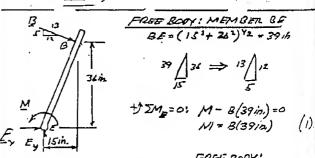
FROM (5): H=E+F=1.359XW+0.359XW=1.71952W RECALL THAT:

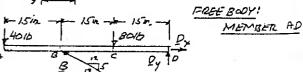
SINCE ALL EXPRESSIONS OBTHINED ARE POSITIVE, ALL FORCES ARE DIRECTED AS CHOWN ON THE FREE-BODY DINGRAPMS.

SUBSTITUTE W= 73.575-RN:



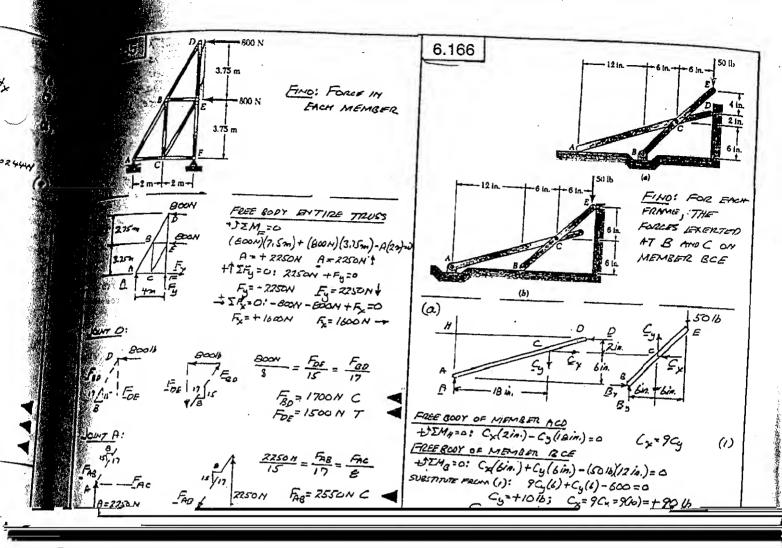
FINO: COUPLE M FOR EQUILIBRIUM

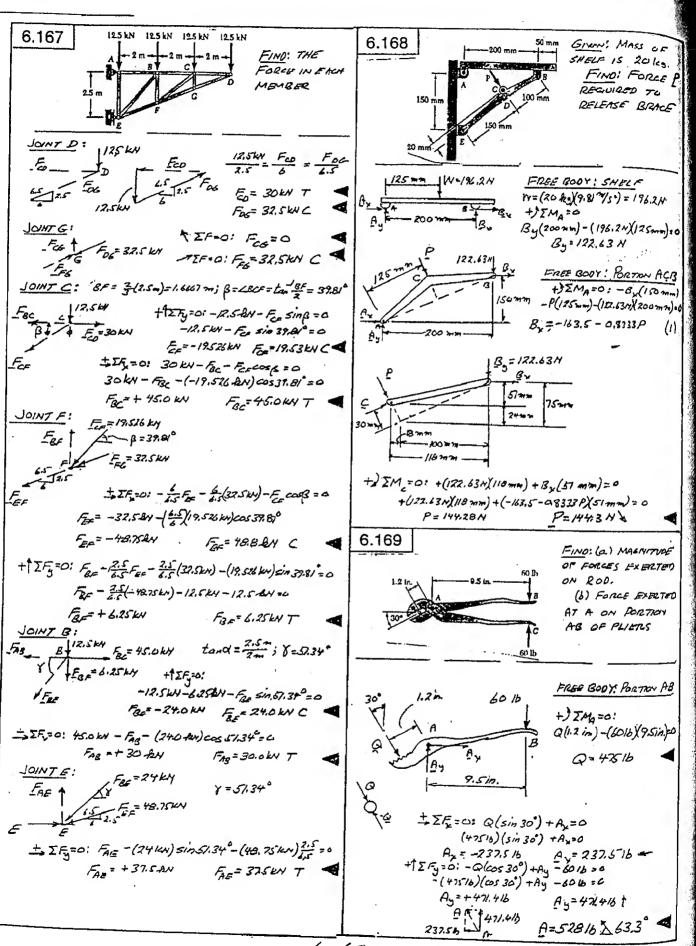




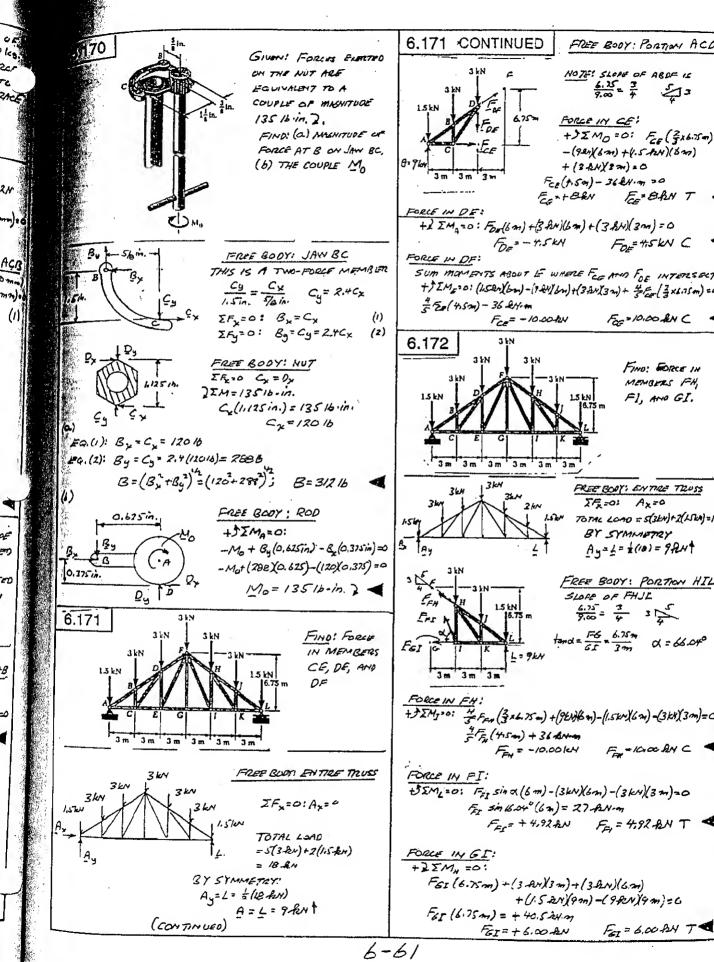
+) IMD=0: (4016)(45in.)+(6016)(15in.)- = (30in.)=0 B = 26016

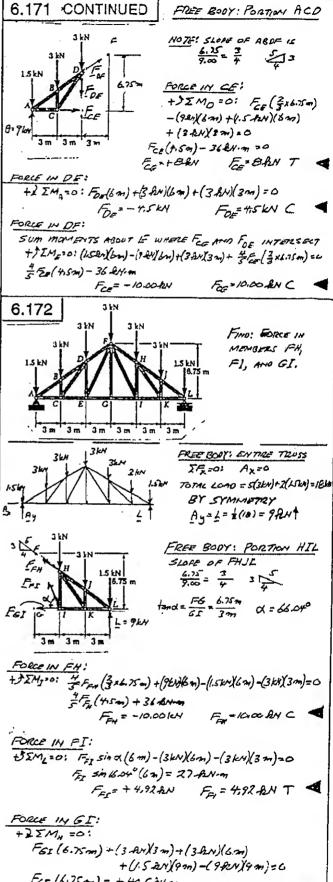
EG(1) M= B(38in.) = (2601) (39in.) = 10,14016-171. M = 10. 14 - Rip . in.)

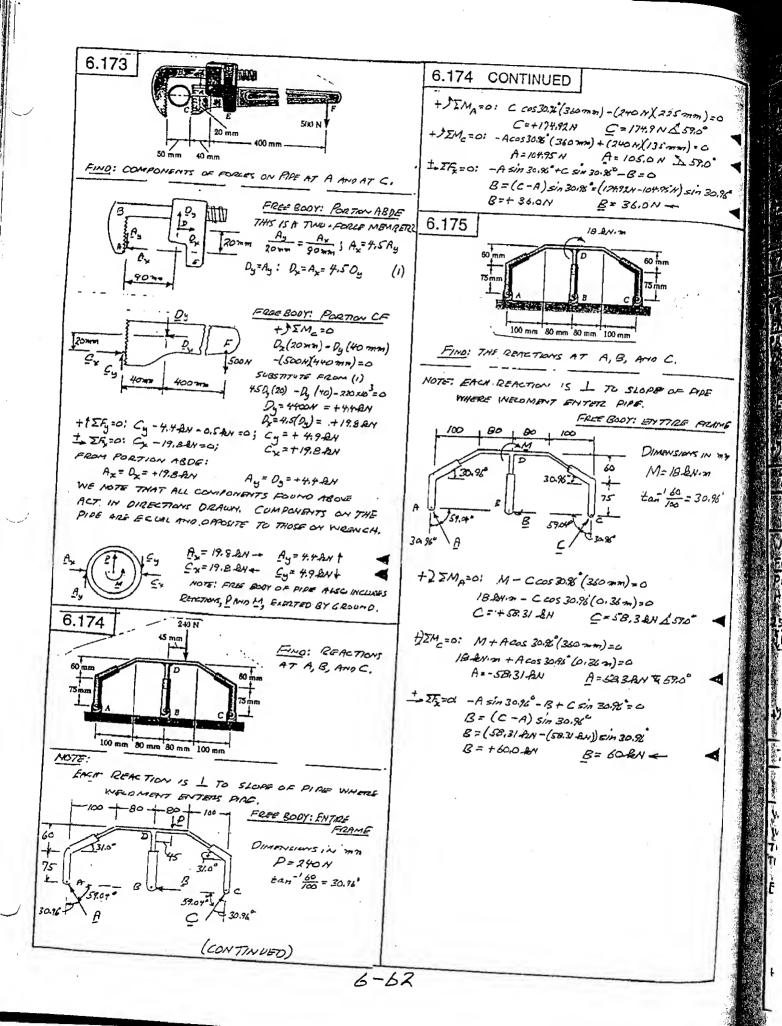


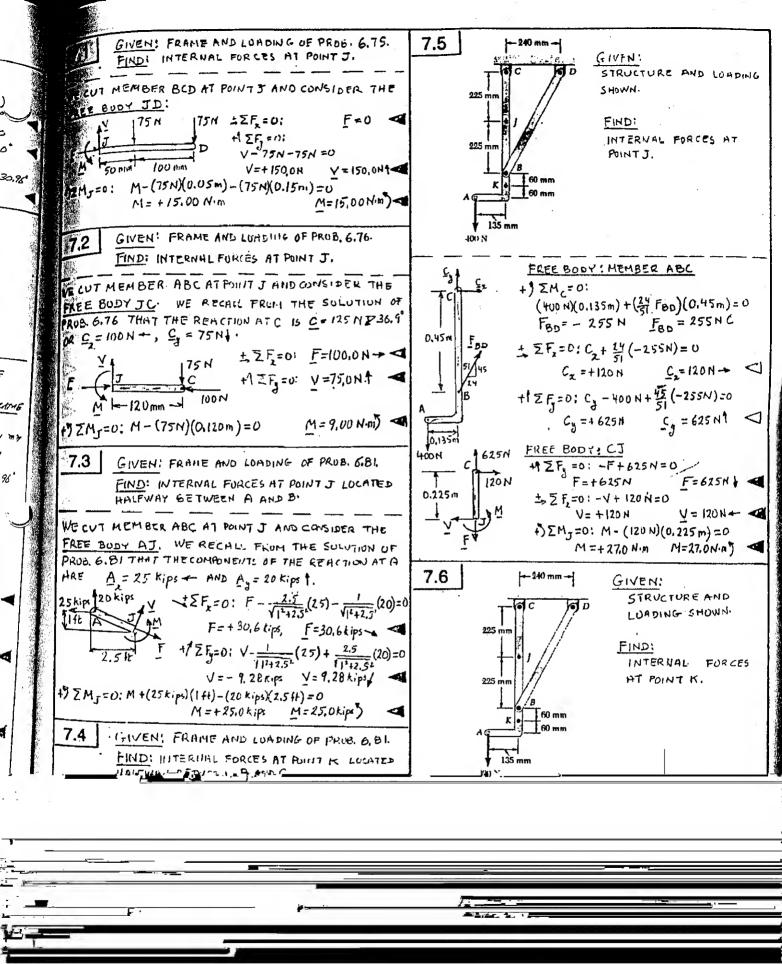


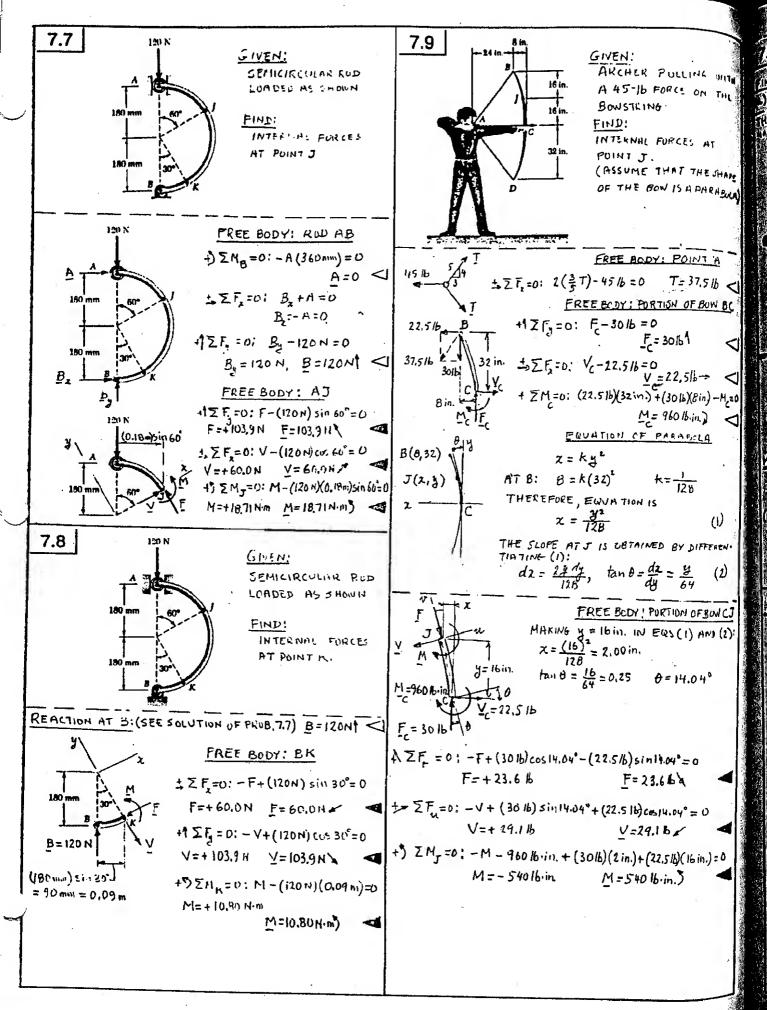
6-60

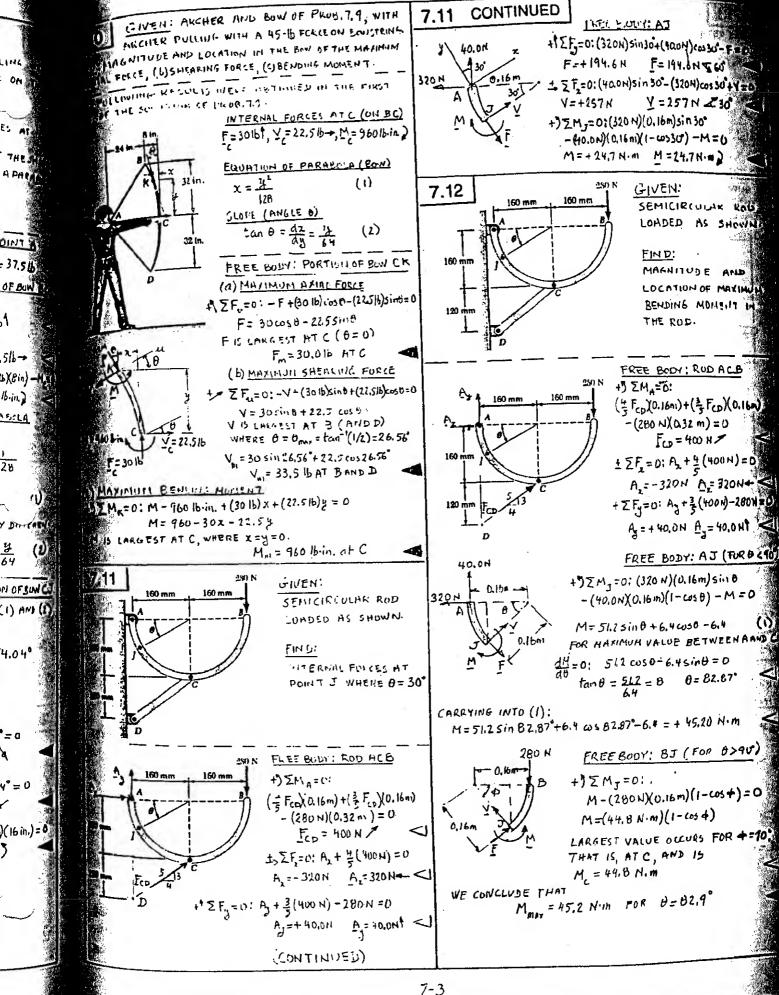












TIME

37.516

516-

b)(8in) -

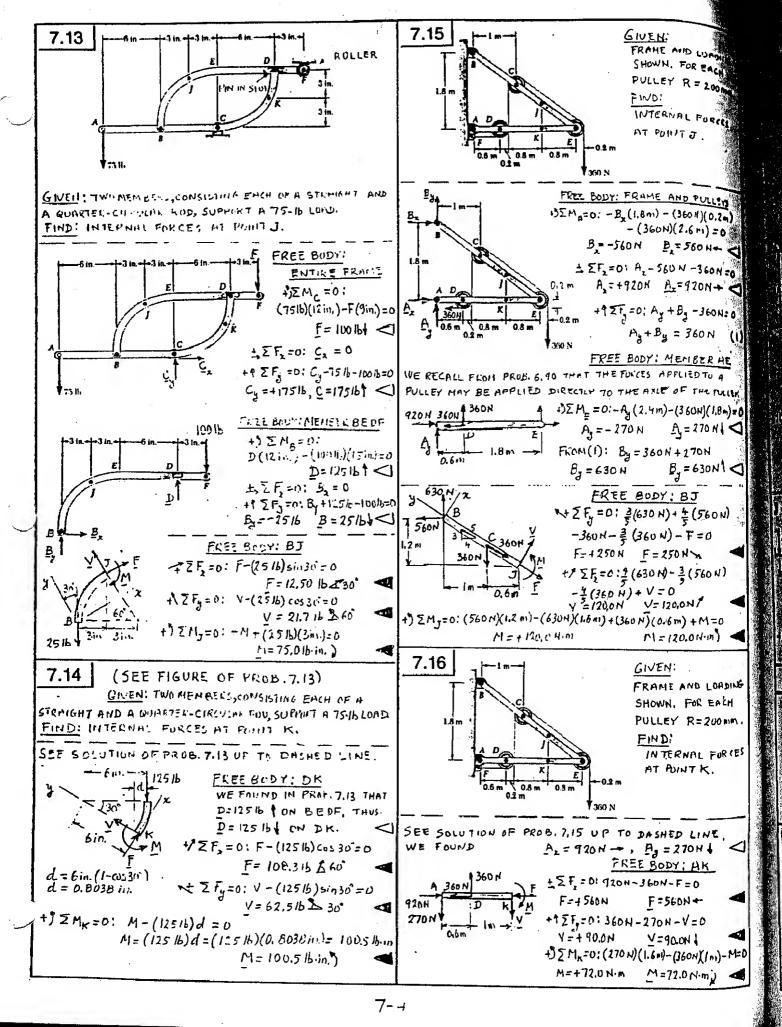
1bin.

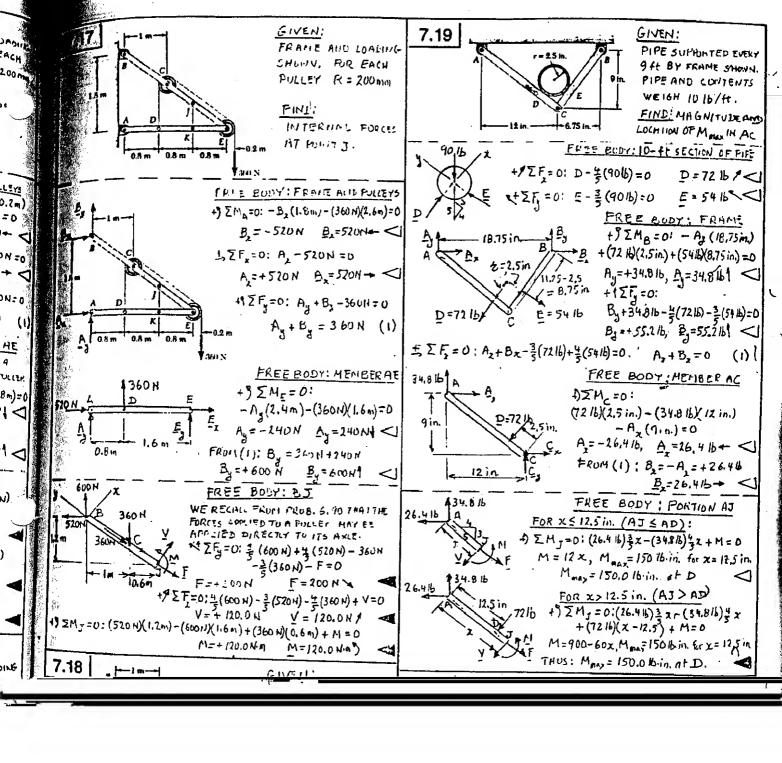
PICLA

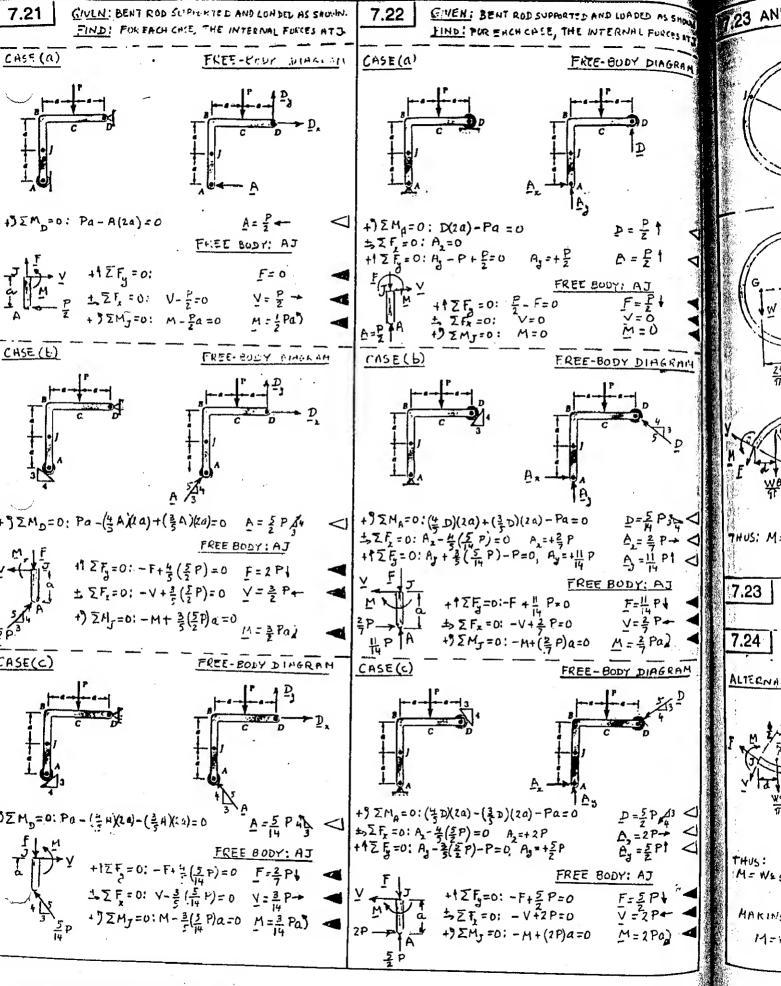
28

64

4.040

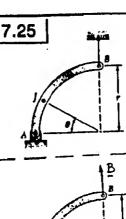






11=1

AND 7.24 GIVEN: SEMICIR CULAR RUD OF WEIGHT W AND UNIFORM CROSS SECTION SUPPURTED AS SHOWN. BENDING MUNENT AT J WHEN 0=60° (PROB. 7.23) 0=150 (PROB. 7.24) FREE BODY: ROD +) $\sum M_{A} = 0$: $W(\frac{2t}{11}) - B(2c) = 0$ 1Σ[=0; *-A=0 A=#-+ = Ex = 0: Ay - W = 0 Ay = WT FREE BUSY: TURTION BJ RAN + 3 2 Mz = 0: $M - \frac{W}{\pi} 2(1 - \cos \theta) - \frac{W\theta}{\pi} d = 0$ M = # + (1-cost)+ Wod BUT d= 2 sin 8 - 2 sin ; = $t \sin \theta - \frac{t}{\theta} 2 \sin^2 \theta$ = $t \sin \theta - \frac{2}{4} (1 - \cos \theta)$ '¿(1-ωsθ)+ ₩z θsinθ-₩z (1-ω0) (1) M= WE & Sint 1 MAKING 0 = 60 = # IN Ea: (1): M=0,289WE) M= W2 Isin 60 = WE sin 60 MAKING 8=150" = 5H IN EQ.(1): M= 0.417Wz) M= Wt 51 sin 150 = 5 W2 RAM ALTERNATIVE SOLUTION TO FROB. 7.24: 3 D PREE BODY: AJ +7 ZN 7=0: -M+W2sind-W2(1-cost)-Wd d=0 M= Wesind - W2 (1-ws 4) - Wod BUT d=もsin中·元sin号 ニセラシャーセスランデ = tsind - = (1-1054) M= WESING - # & (1-cost) - #2 + sinp+ # (1-cost) $\Lambda = 1 \vee \left(1 - \frac{\phi}{\pi}\right) \sin \phi$ MAKINE # = 180°-150° = 30° = 7/6 IN EQ. (2)1 11-Wz(1-2)sin30 = 3Wz M=0.417WE) (ON HJ)



GIVEN:

CHARTER CIRCULAR ROD OF

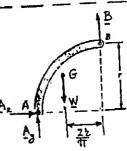
WEIGHT W AND UNIFORM CROSS

SECTION SUPPORTED AS SHAUN

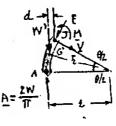
FIND:

BENDING MOMENT AT J WHEK

0 = 30°.



FREE BODY: ROD $\pm \sum F_{k} = 0$: $A_{k} = 0$ $\pm \sum F_{k} = 0$: $A_{k} = 0$ $\pm \sum M_{B} = 0$: $W(\frac{2t}{n}) - A_{b} = 0$ $A_{b} = \frac{2W}{\pi}$ $A = \frac{2W}{\pi}$



PREE BUDY: PORTION AJ +) $\Sigma M_J = 0$: $M + W'd - \frac{2W}{T} + (1 - \cos \theta) = 0$ $M = \frac{2W}{TT} + (1 - \cos \theta) - W'd$ (1) BUT $W' = W \frac{\theta}{T/2} = \frac{2W\theta}{T}$ (2) AND $d = \frac{2}{3} \cos \frac{\theta}{2} - t \cos \theta$ $= \frac{2}{3} \sin \frac{\theta}{2} \cos \frac{\theta}{2} - t \cos \theta$ $= \frac{2}{3} \sin \frac{\theta}{2} \cos \frac{\theta}{2} - t \cos \theta$

(3)

 $d = 2\left(\frac{\sin\theta}{\theta} - \cos\theta\right)$ 5UBSTITUTING FROM (2) AND (3) (NTO (1); $M = \frac{2W}{\Pi}2\left(1-\cos\theta\right) - \frac{2W}{\Pi}\theta + \left(\frac{\sin\theta}{\theta} - \cos\theta\right)$ $M = \frac{2W}{\Pi}2\left(1-\cos\theta - \sin\theta + \theta\cos\theta\right)$ $MAKING B = 30 = \frac{1}{\Pi}IN EQ (+);$

M = 2W2 [1-6530 + 16 6530]
M = 0.0557 WE)

THE SOLUTIONS OF PROBS. 7.26 AND 7.27 ARE GIVEN ON THE NEXT PAGE

7.28 GIVEN: ROD OF PROB. 7.25.

FIND: MAGNITUDE AND LOCATION OF MAXIMUM
BENDING MUNIENT.

WE RECHLL EU. (4) OF PROB. 7.25:

M = 2W2 (1-cost-sint + 0cost) (4)

 $\frac{dH}{d\theta} = \frac{2We}{17} \left(\sinh - \cos \theta + \cos \theta - \theta \sin \theta \right)$

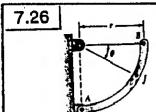
SETTING $\frac{dM}{d\theta} = 0$: $\sin\theta (1-\theta) = 0$

THE ROOTS OF THIS ENUNTION FOR 0 S & T HRE

0=0 AND 0=1 RAD=57.3°

FOR $\theta = 0$, M = 0. FOR $\theta = 1$ RAD = 57.3°, $E\omega(4)$ YIELD $M = \frac{2Wt}{f!}(1 - \cos 57.3° - \sin 57.3° + 1 \times \cos 57.3°)$ $= \frac{2Wt}{f!}(1 - \sin 57.3°) = 0.1009 \text{ W}$

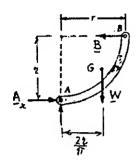
THUS: May = 0.1009 W2 for B = 57.3°



GIVEN:
QUARTER CIRCULAR RUD OF
WEIGHT W AND UNIFORM CROSS
SECTION SUPPORTED AT SHOWN.
FIND:
BENDING MOMENT AT J WHEN

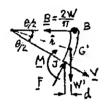
FREE BODY: RUD

0 = 30"



+)
$$\Sigma M_A = 0$$
:
 $Bt - W(\frac{2t}{\pi}) = 0$
 $B = \frac{2W}{\pi}$

FREE BODY: PORTION BJ



$$\frac{2W}{\pi} z \sin \theta - W'd - M = 0$$

$$M = \frac{2W}{\pi} z \sin \theta - W'd \qquad (1)$$

BUT W'= W
$$\frac{\theta}{\pi/2} = \frac{2W\theta}{\pi}$$
 (2)

AND
$$d = \frac{2}{2}\cos{\frac{\theta}{2}} - 2\cos{\theta}$$

$$= 2\frac{\sin{\theta/2}}{\theta/2}\cos{\frac{\theta}{2}} - 2\cos{\theta}$$

$$= 2\frac{\sin{\theta/2}\cos{\frac{\theta}{2}} - 2\cos{\theta}}{2\cos{\theta/2}} - 2\cos{\theta}$$

$$= 2\frac{(\sin{\theta/2}\cos{\theta/2} - 2\cos{\theta})}{2\cos{\theta/2}}$$
(3)

SUBSTITUTING FROM (2) AND (3) INTO (1):

$$M = \frac{2W}{\Pi} 2 \sin \theta - \frac{2W\theta}{\pi} 2 \left(\frac{\sin \theta}{\theta} - \cos \theta \right)$$

$$M = \frac{2W^{2}}{\Pi} \theta \cos \theta \qquad (4)$$

MAKINE 0 = 30 = 7 IN ER, (4):

$$M = \frac{2Wt}{\pi} (\frac{m}{6}) \cos 30^\circ = \frac{Wt}{3} \cos 30^\circ \quad \underline{M} = 0.289 \ Wt_{ij}$$

7.27 GIVEN: ROD OF PAUB. 7. 26.

FIND: MAGNITUDE AND LOCATION OF MAYINUM BENDING MOMENT.

WE RECALL EU. (4) OF PRUB. 7.26 ;

$$M = \frac{2W^2}{\Pi}\theta \cos\theta \tag{4}$$

 $\frac{dH}{dh} = 0:$

$$cos\theta - \theta sin\theta = 0$$

 $tan\theta = \frac{1}{4}$

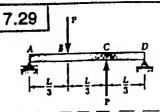
Solving By successive APPROXIMATIONS: $\theta = 49.293^{\circ} = 0.86033$ RAD

SUBSTITUTING INTO EQ.(4)

M = 2W1 (0.86033 RAD) COS 49.293 = 0.3572 W1

THUS: Mmax = 0.357 WE for 0= 49.3°

THE SOLUTION OF PROB. 7.28 IS GIVEN ON THE PRECEDING PAGE



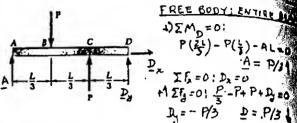
GIVEN:

BEHMAND LOADING

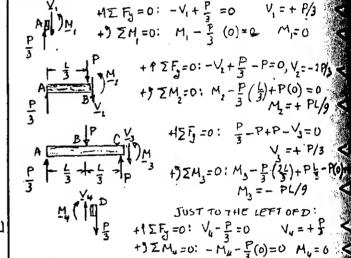
(a) DRAW VAND M DILL

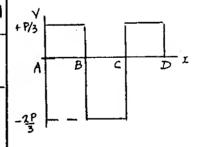
(b) DETERMINE IVI

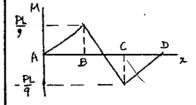
IMIANY.

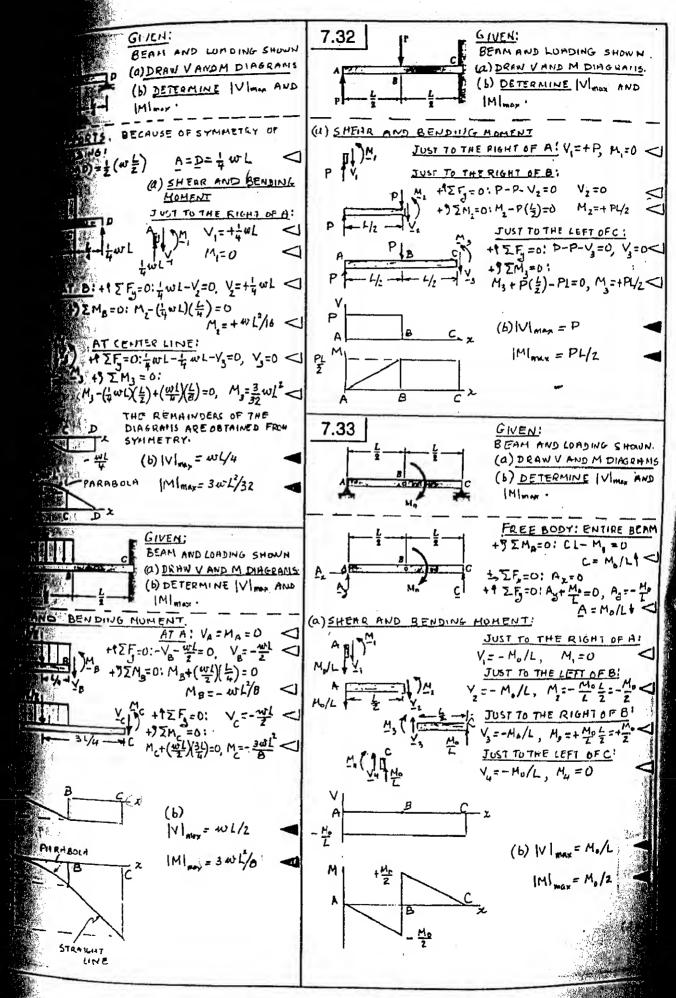


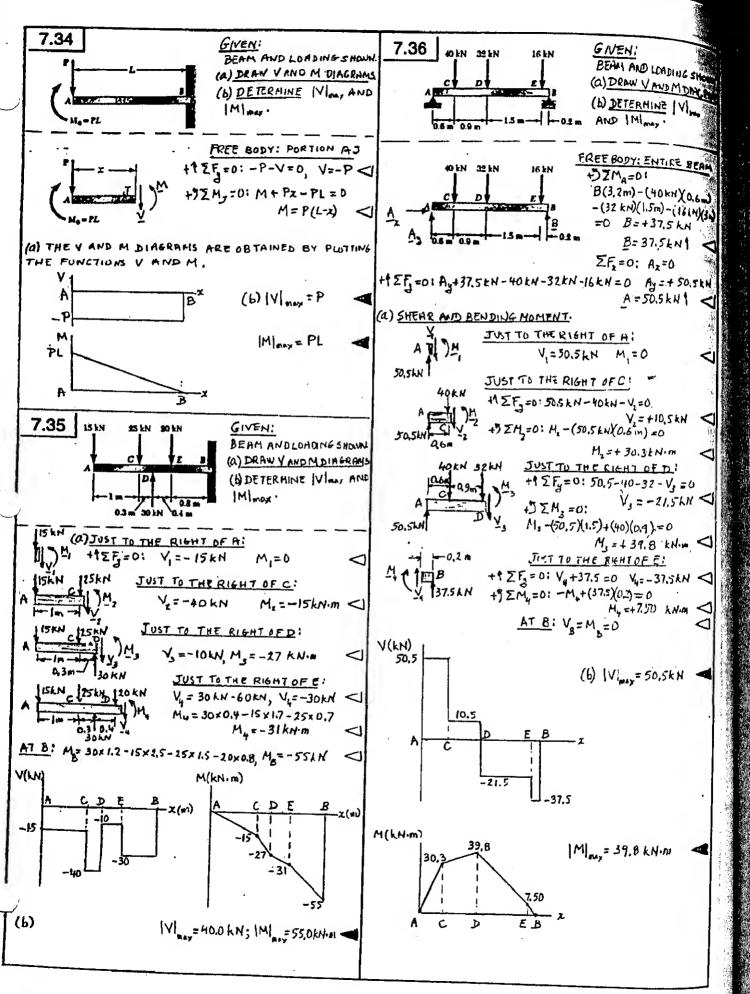
CONCENTENTED LUMBS, THE SHEAR DIAGRAM IS MAN HORIZONIAL STRAIGHT-LINE STEMENTS AND THE BAN JIMES IS MADE OF OBLIQUE STRAIGHT-LINE SEGMENTS. WE SAME DETERMINE V AND M JUST TO THE RIGHT OF A. B, AND C

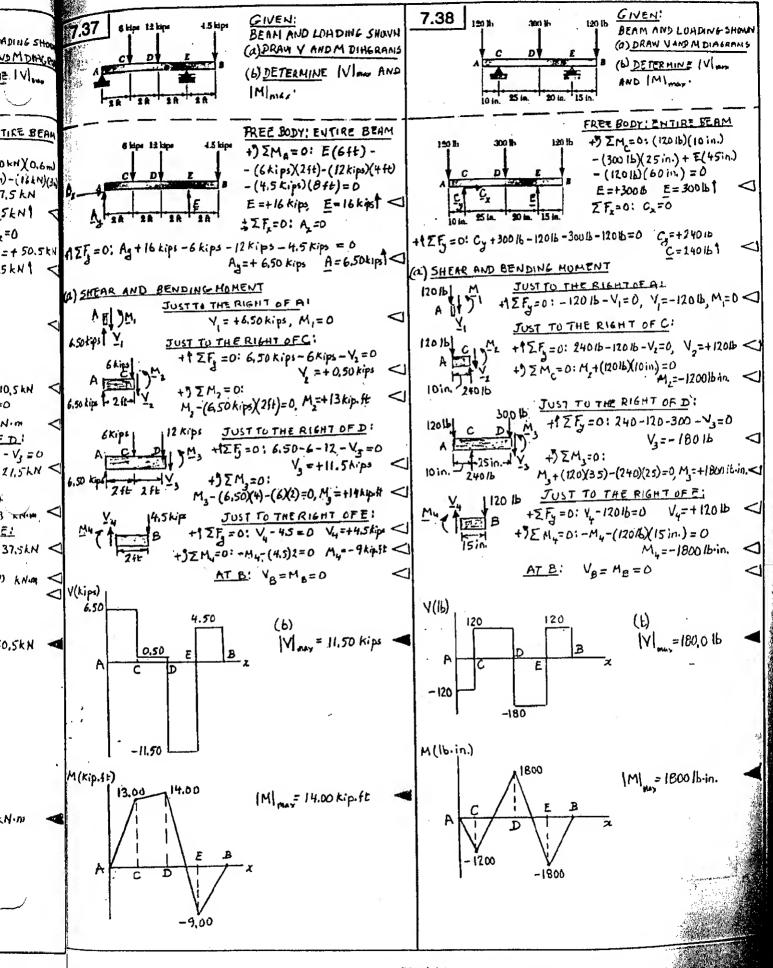


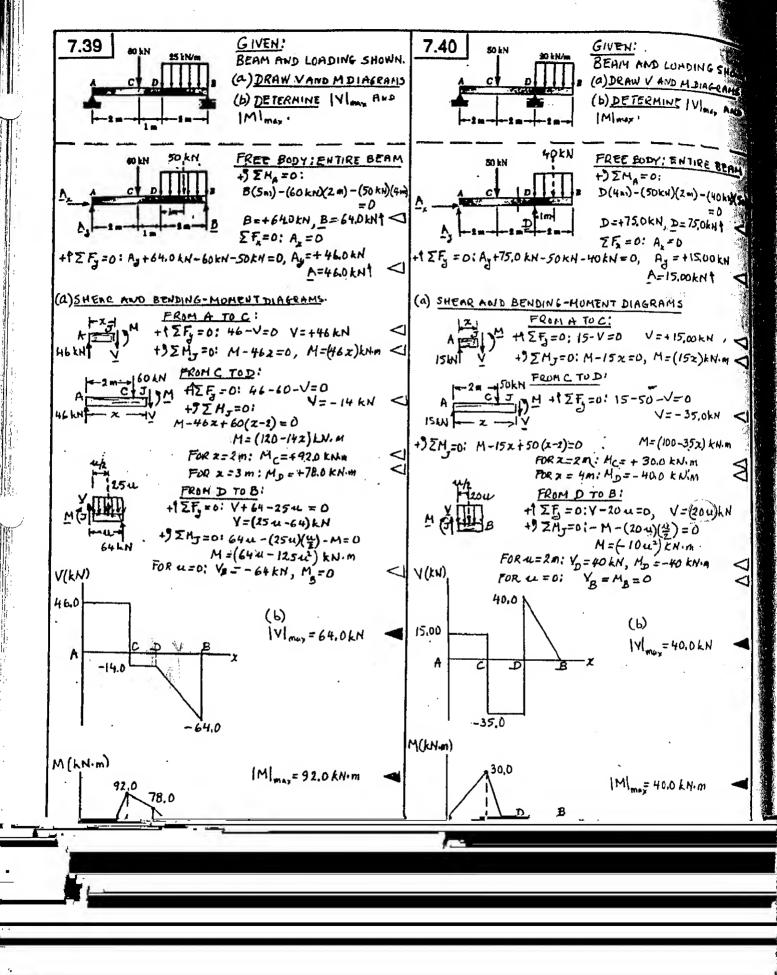


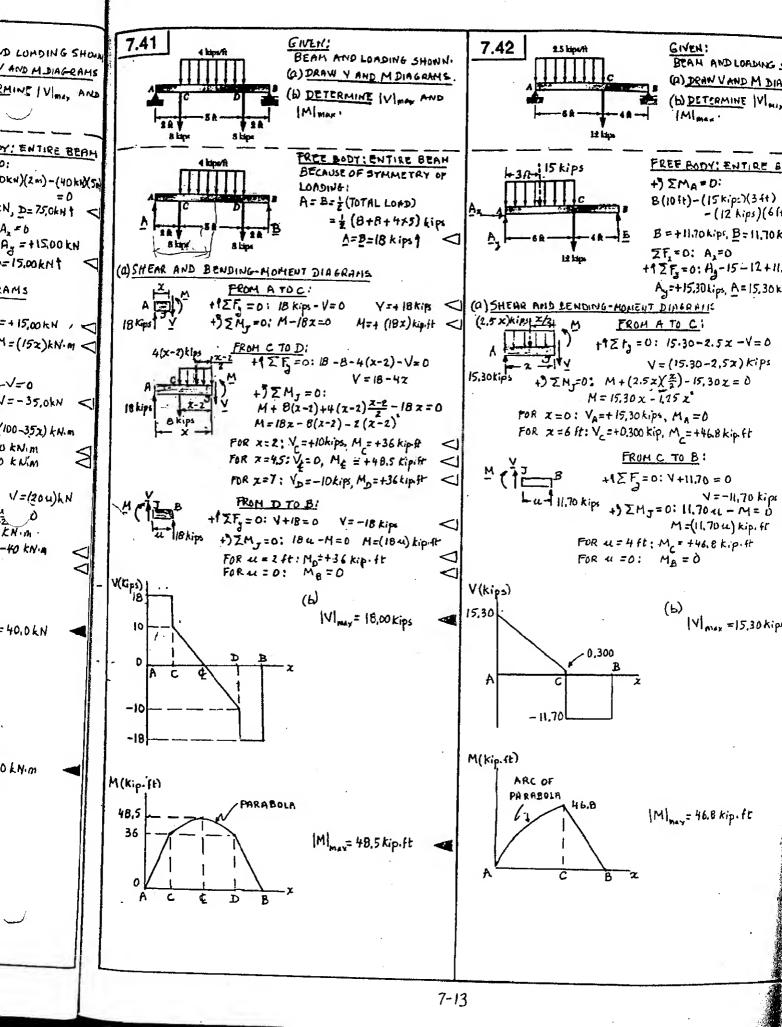


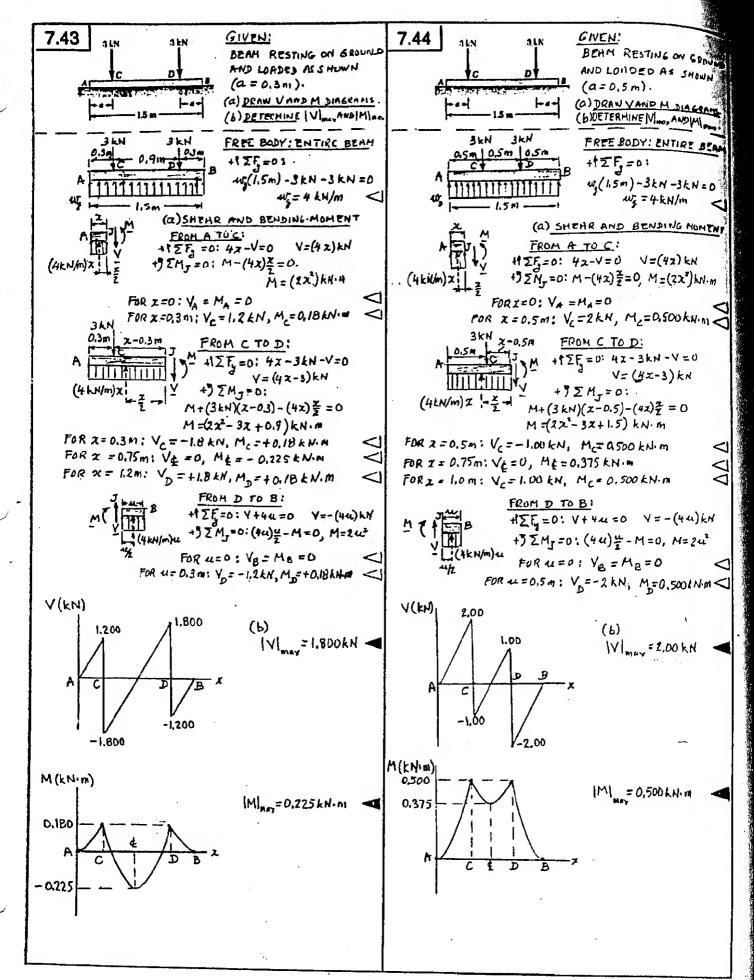


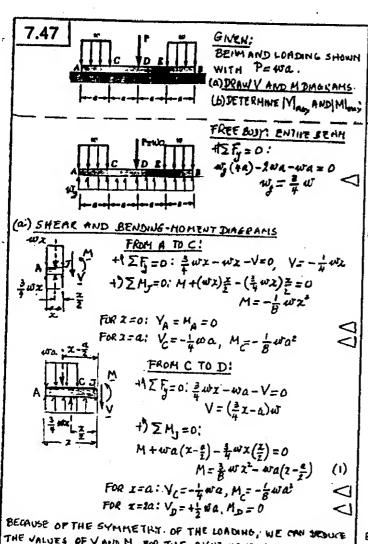




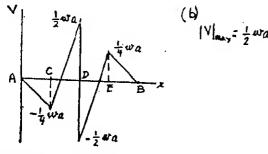




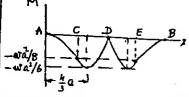




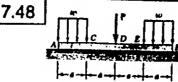
THE VALUES OF VAND M FOR THE RIGHT-HAND HALF OF THE BEAM FROM THE VALUES OBTAINED FOR ITS LEFT-HAND HALF.



TO FIND IM MAY, WE DIPPERENTIATE ED. (1) AND SET di =0: dy = 3 = x - wo = 0, x = 3 a, M = 3 w (4 a) - wo (4 - 1) = - wa IMmx=1wa2

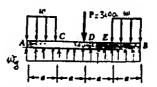


B.H. DIAGRAH CONSISTS OF FOUR DISTINCT ARCE OF PARABOLA.



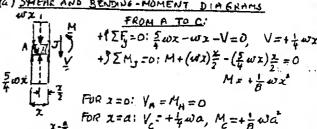
GIVEN: BEAM AND LONDING 3 WITH PE 3 wa. (0) DRAY VAND H DIRERA

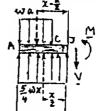
(b) DETERMINE |V| MA AND !



FREE BODY: ENTIRE +12 Fx =0: 4 (44) -2 Wa - 3 W

(a) SHEAR AND BENDING - HOMENT DIAGRAMS





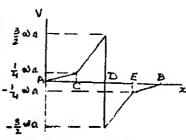
FROM C TO DI +1 IF, =0: \(\int \war = 0 \) +3 2H, = 01 M+ wa(x-4)- = 0x(3)=0 M=== wx -wa(z-a)

(P)

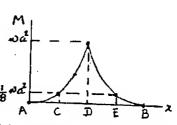
MIMAY = wa

FOR x = a: $V_c = +\frac{1}{4}\omega a$, $M_c = +\frac{1}{8}\omega a^2$ FUR z = 1a: Vo=+3 wa, Mo=+ wai

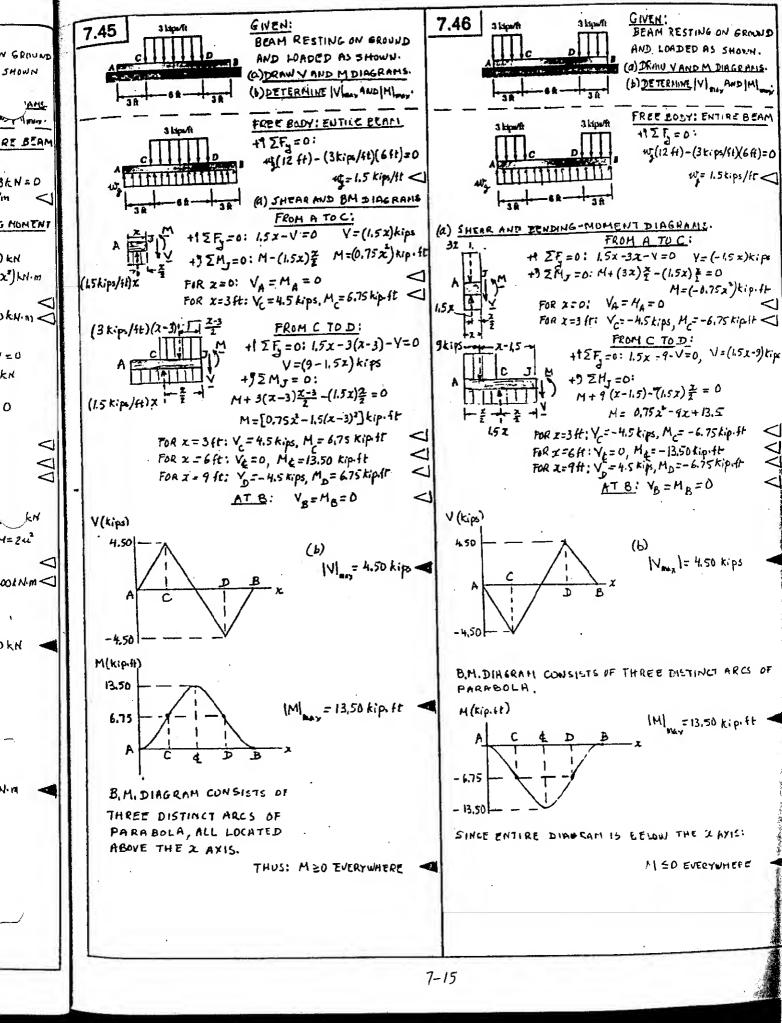
BECAUSE OF THE SYMPLETRY OF THE LOADING, WE CAN DEWA THE VALUES OF VANDM FOR THE RIGHT-MAND HALF OF THE EEAN FROM THE VALUES SPIAINED FOR ITS LEFT-HAND HALF.

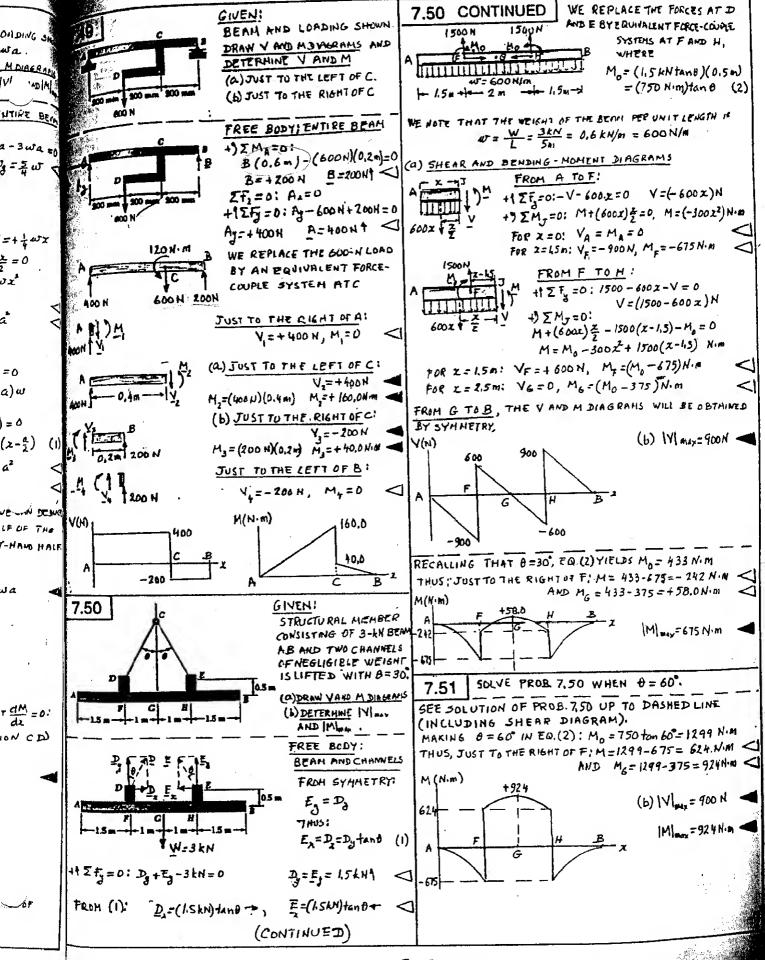


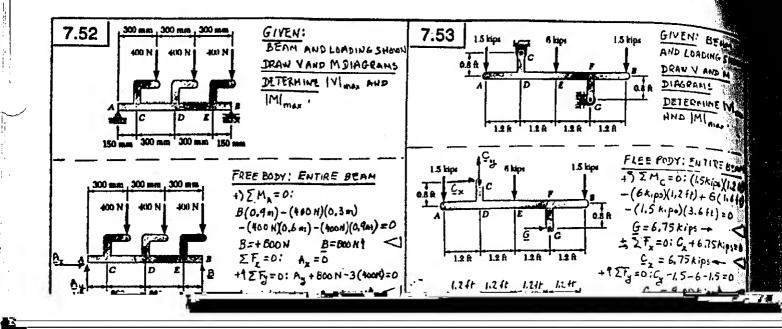
TO FIND IM MAK, WE DIFFERENTIATE EU. (1) AND SET AN =0: AT = 5 WI - WA = 0, X = \$ A < A (OUTSIDE PORTION CD) THE HAX. VALUE OF M OCCURS AT D:

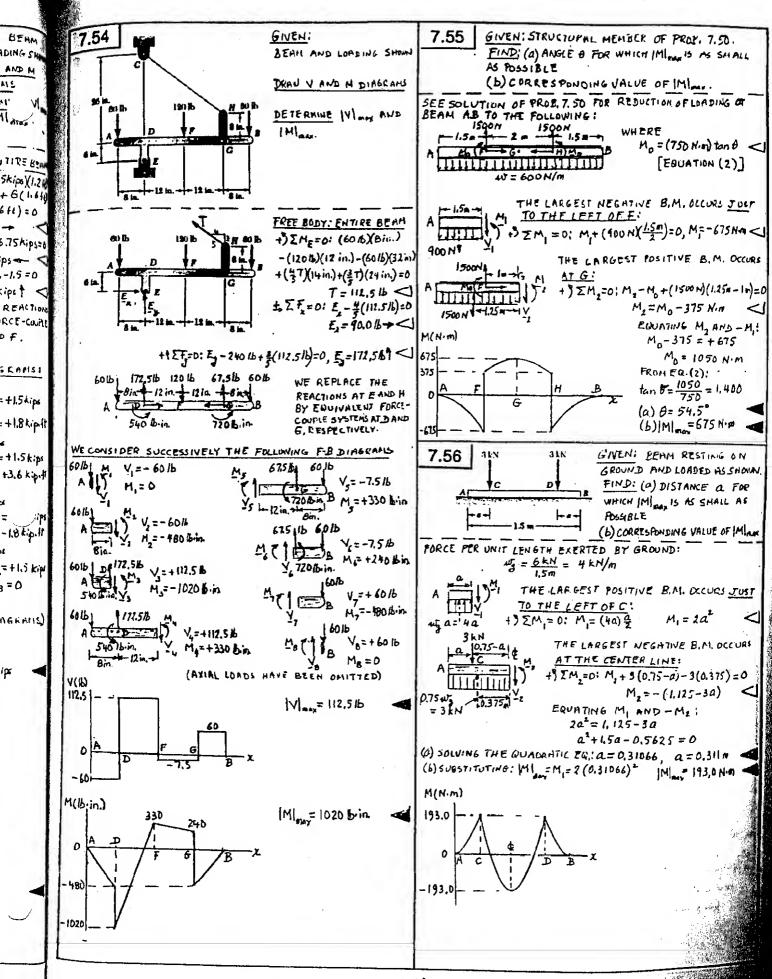


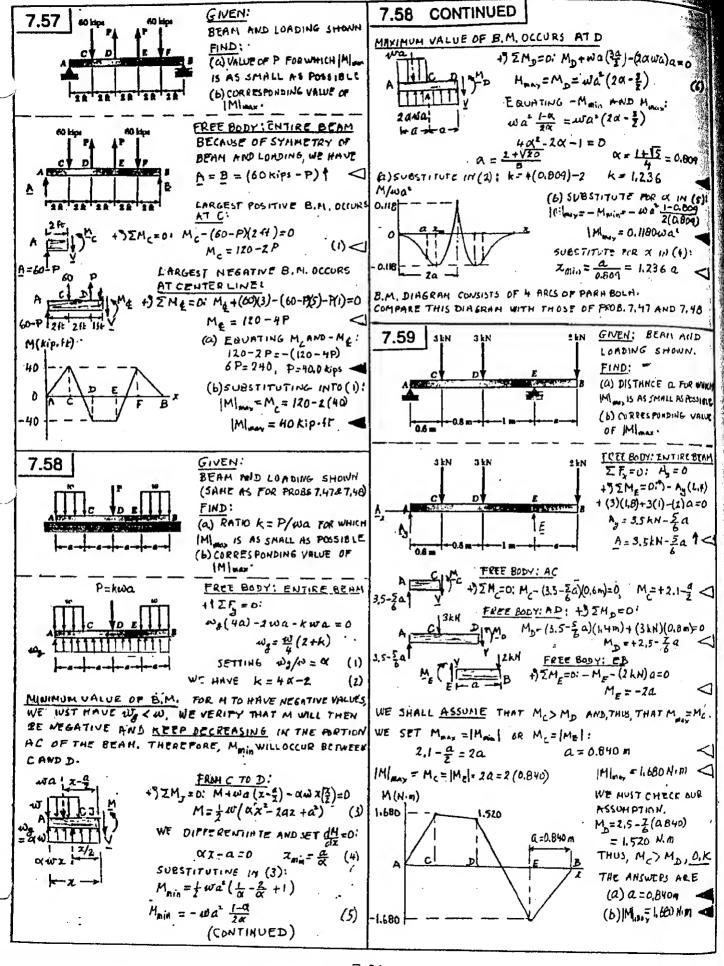
B.M. DIAGRAM CONSISTS OF FOUR DISTINCT ARCS OF PARA BOLA.

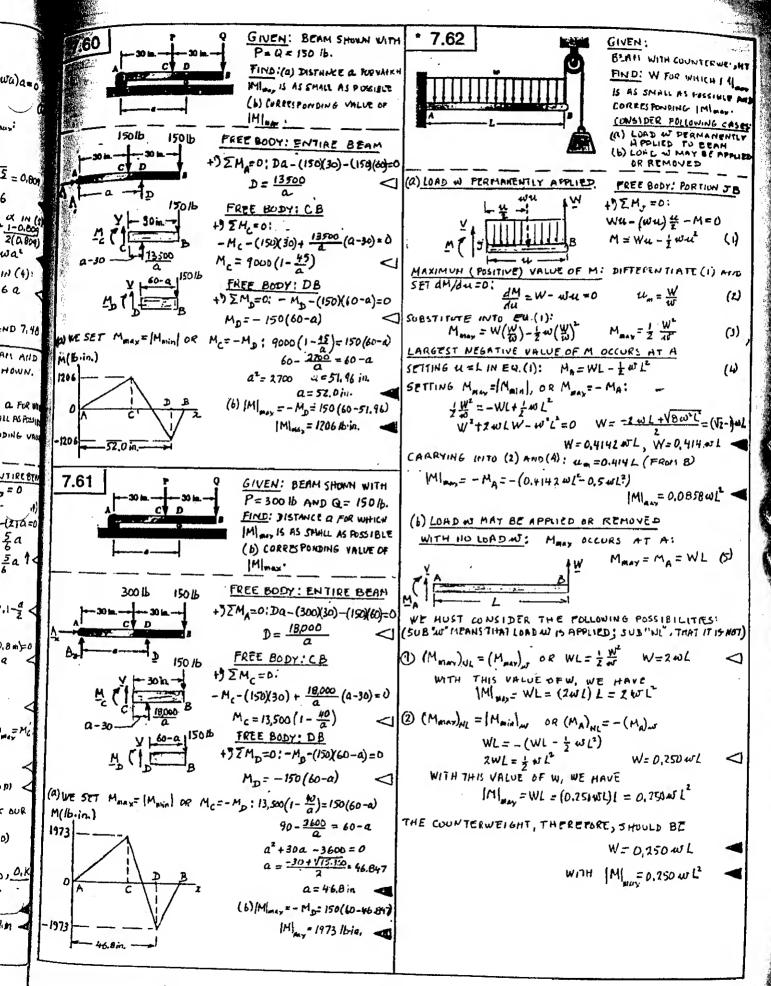


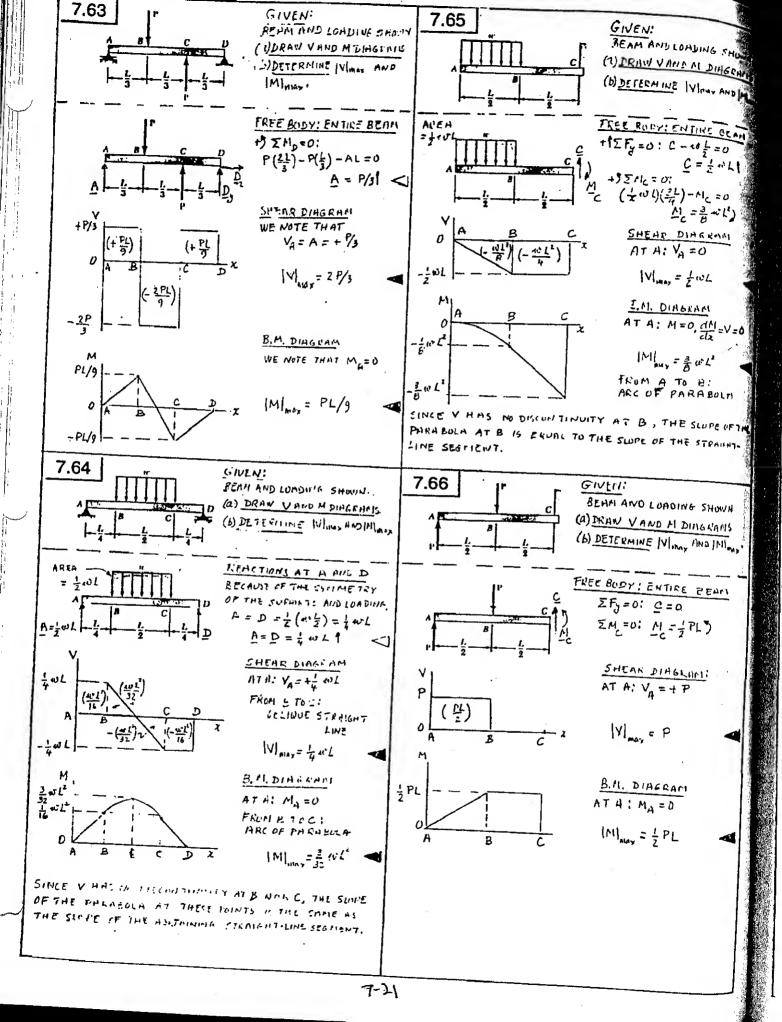


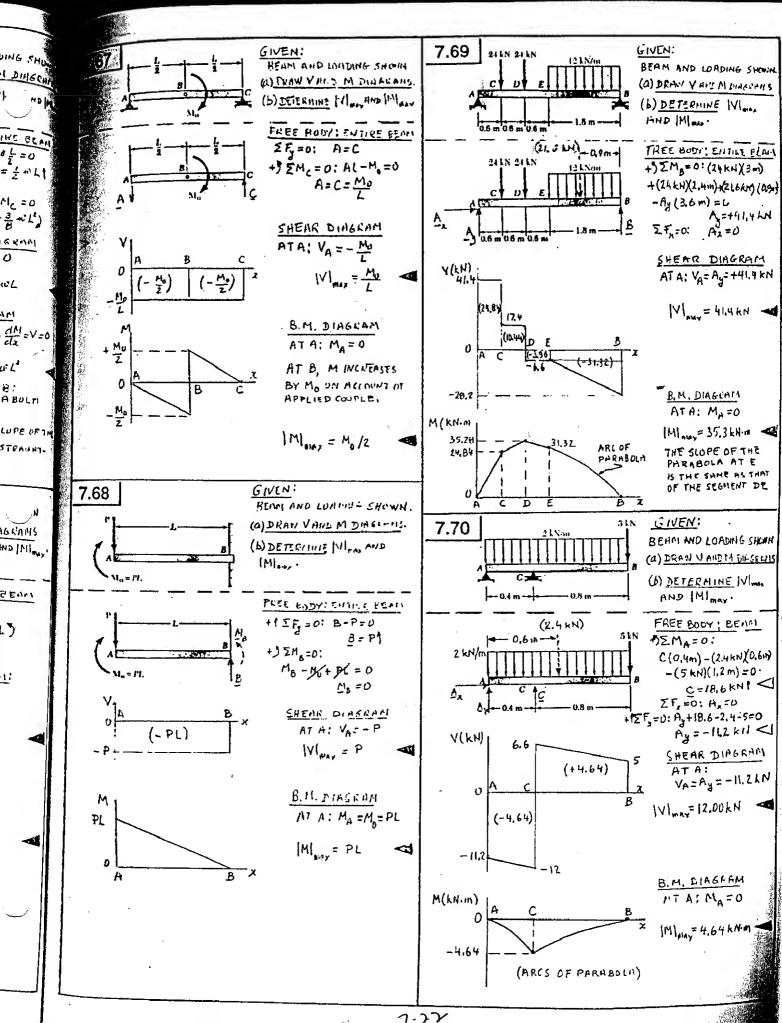


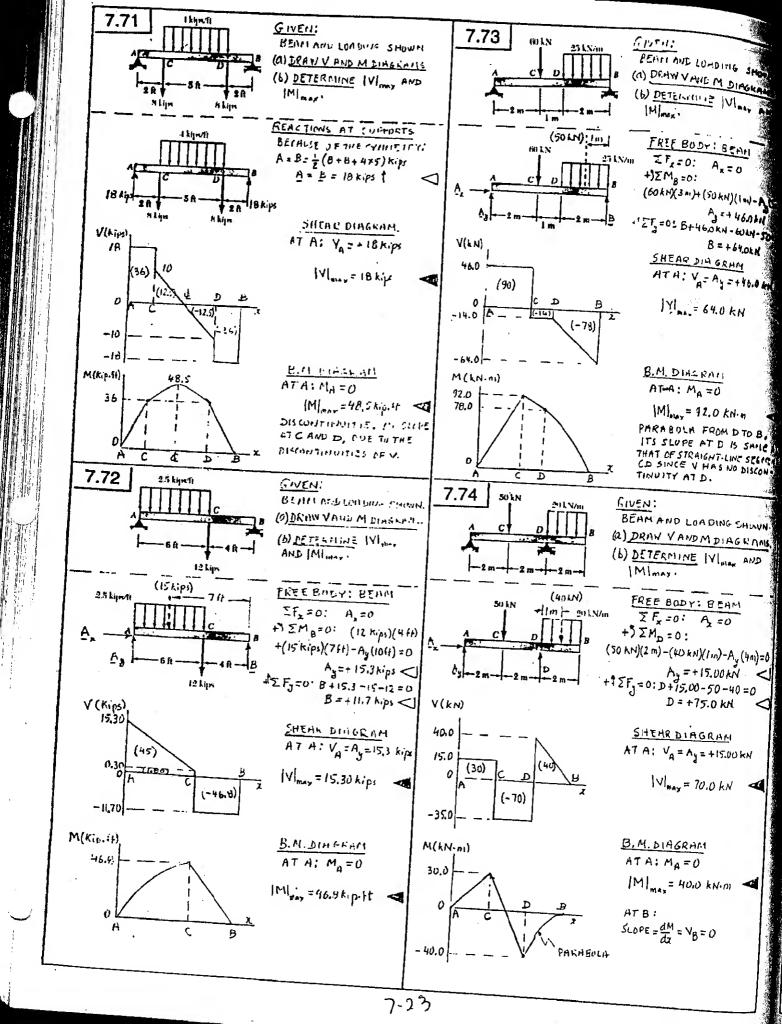


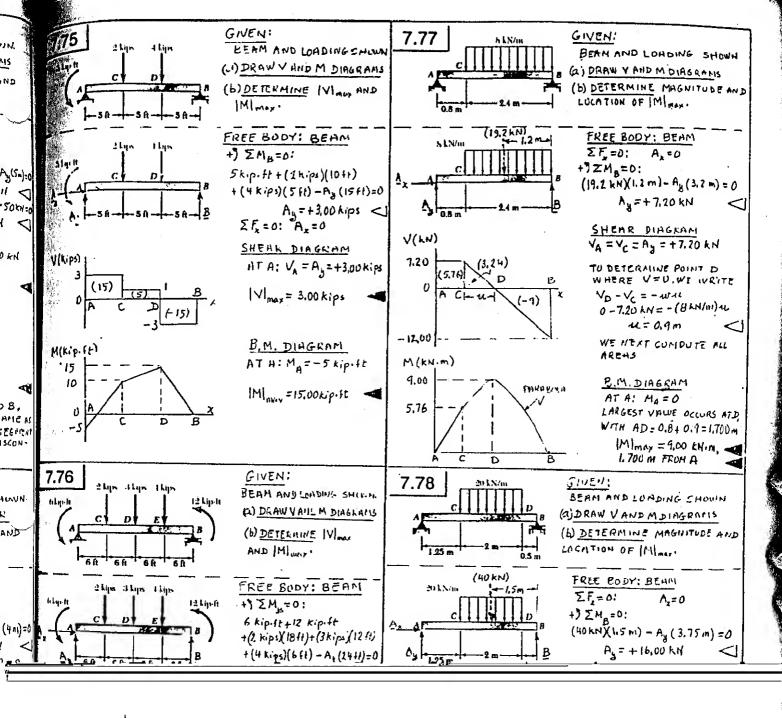


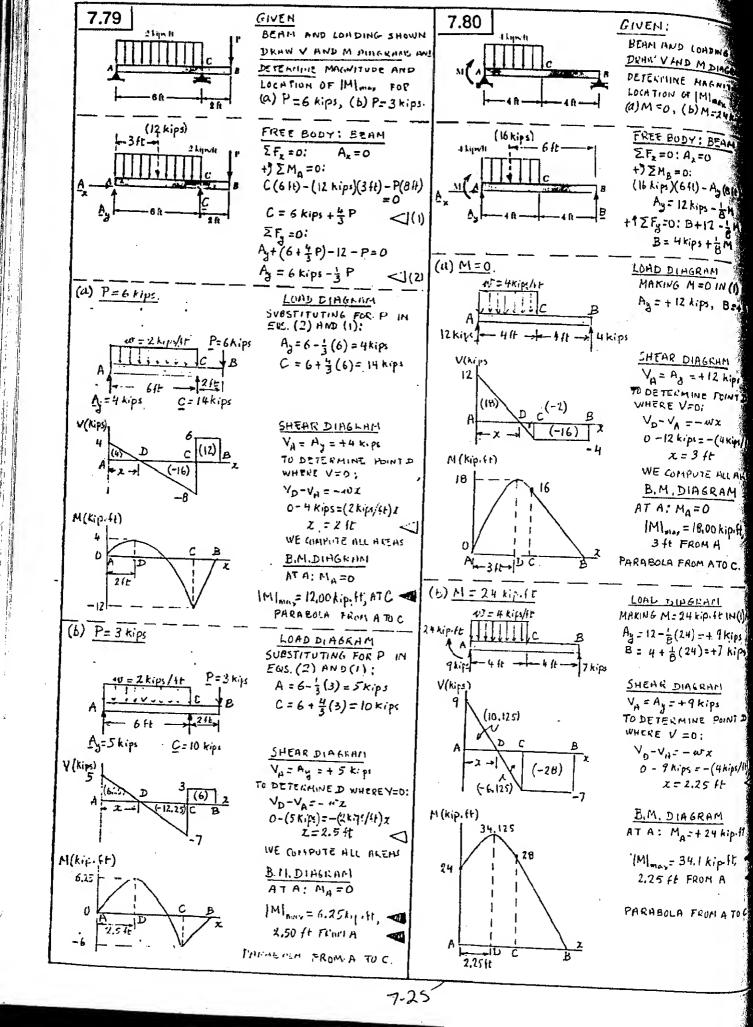


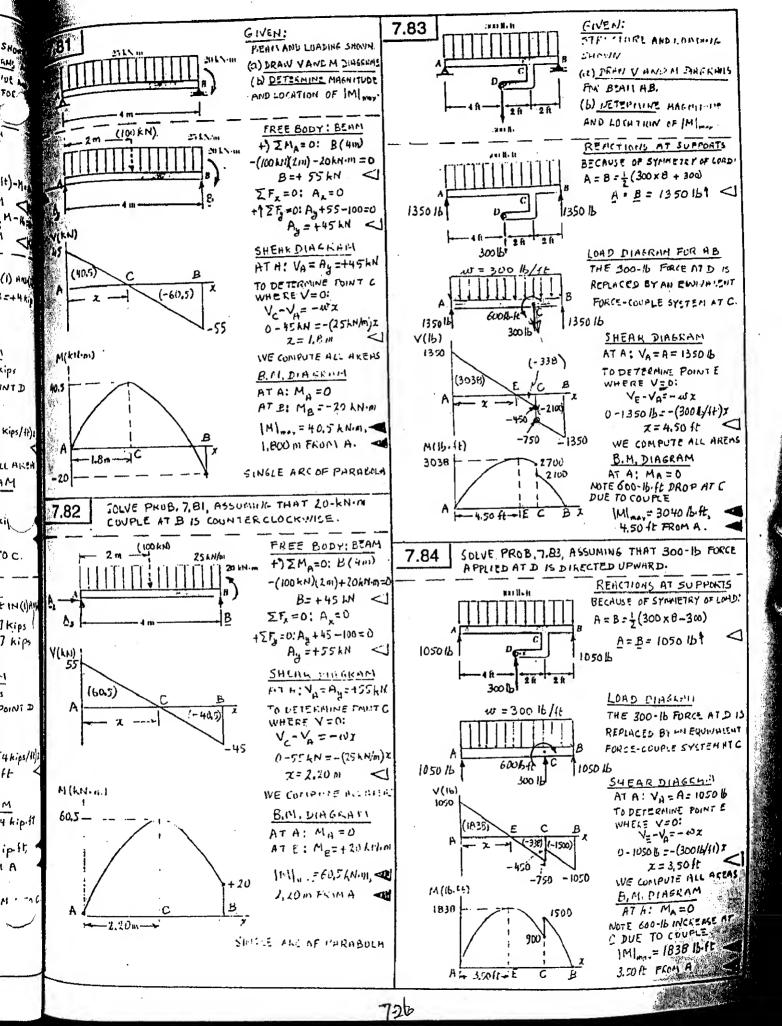


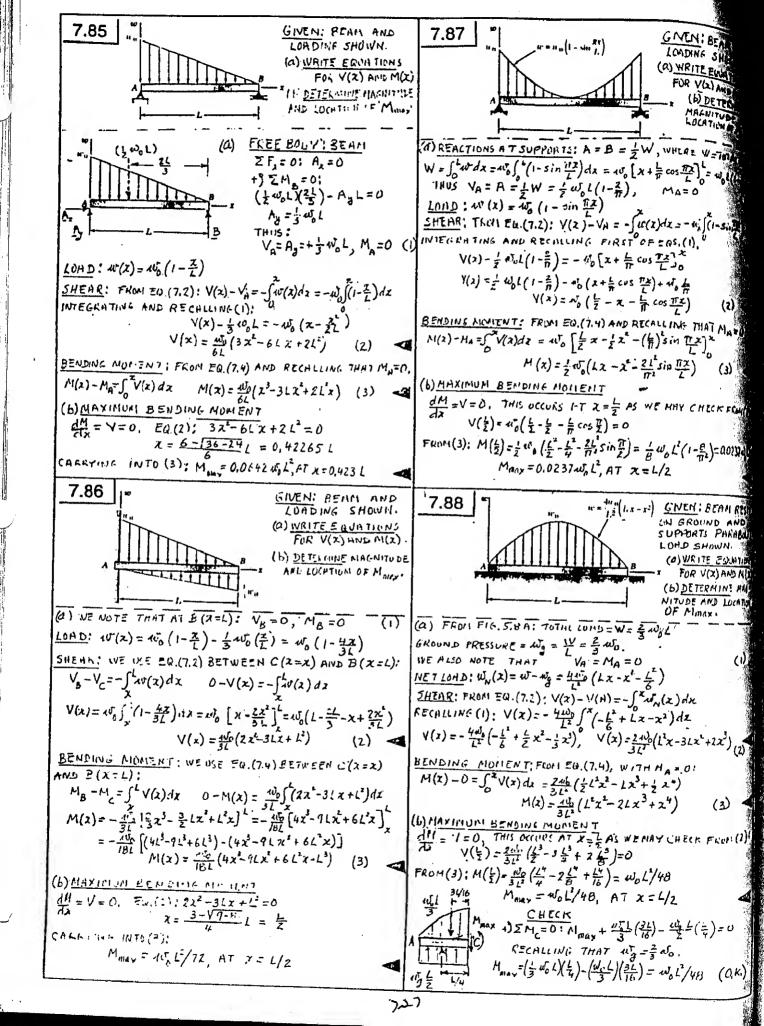


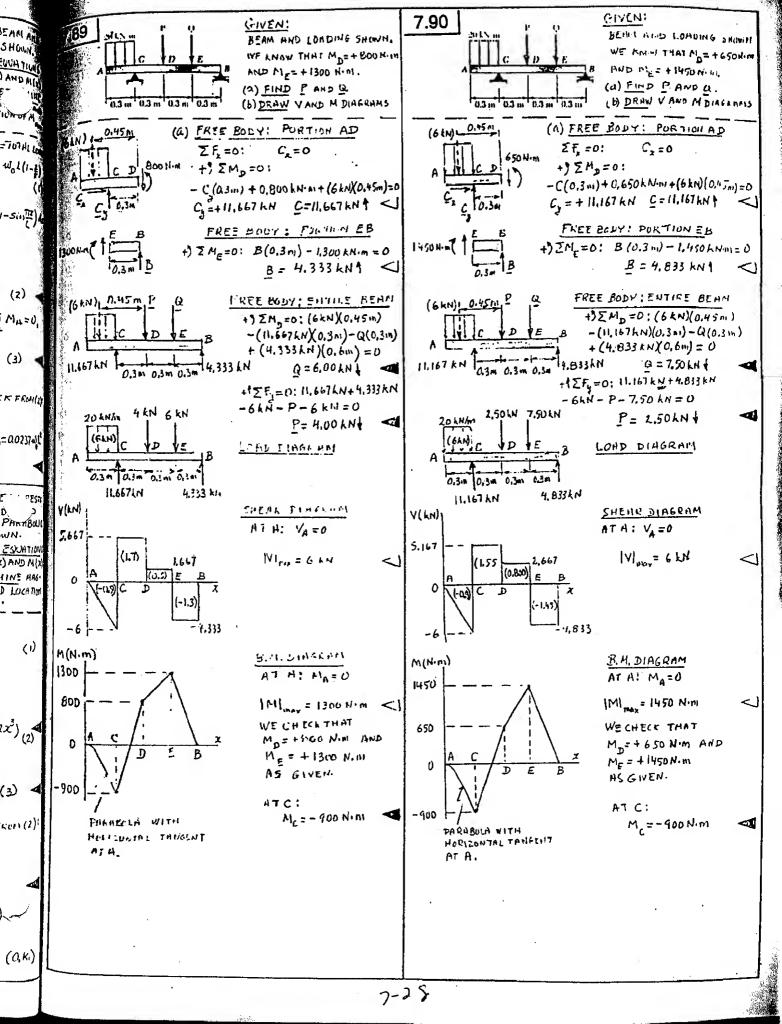


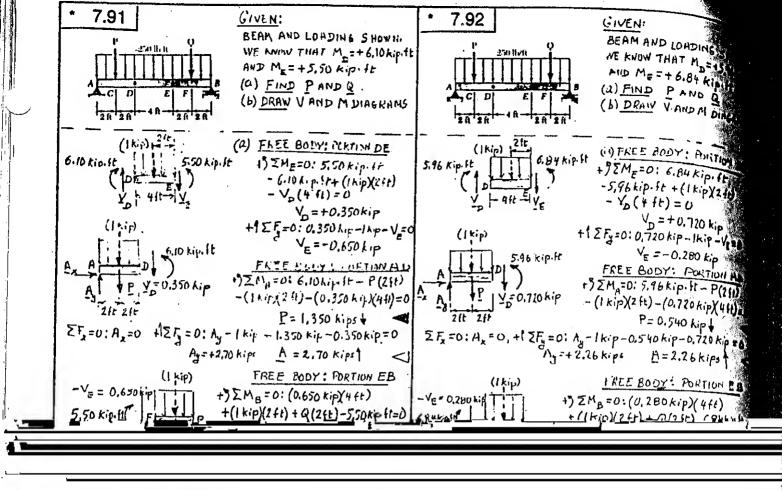


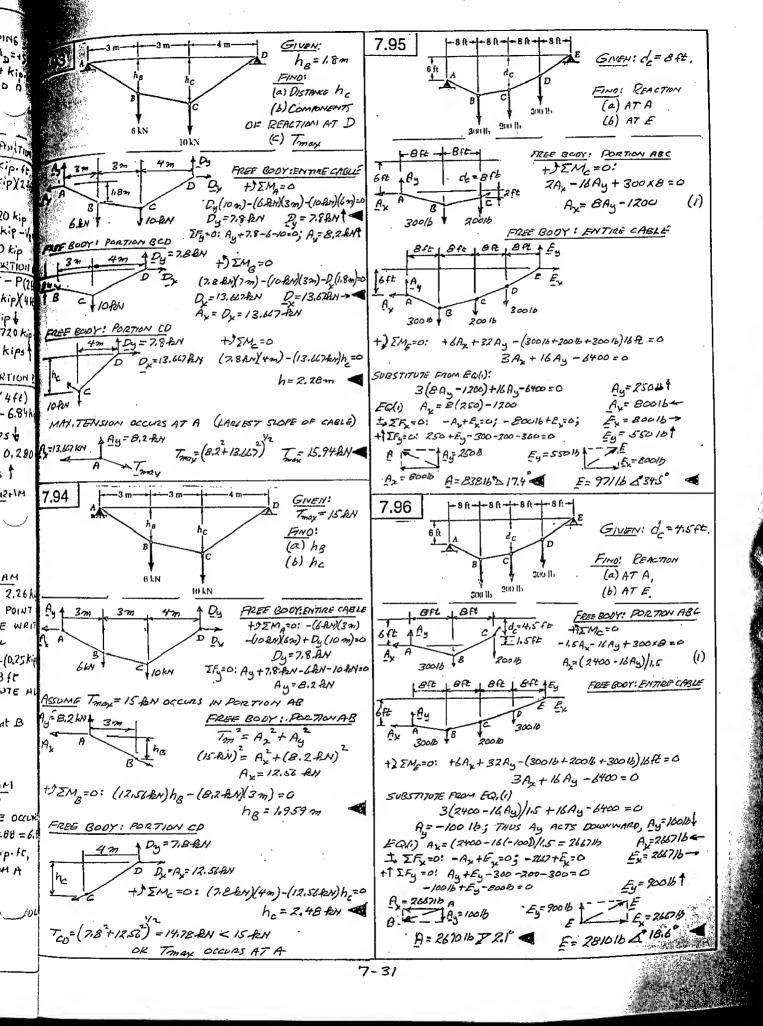


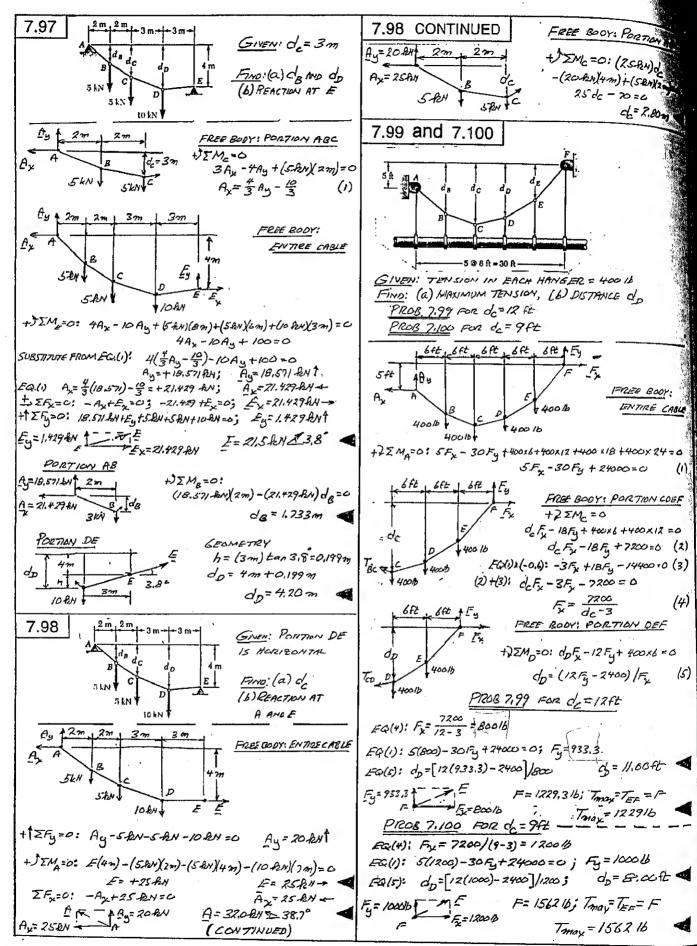


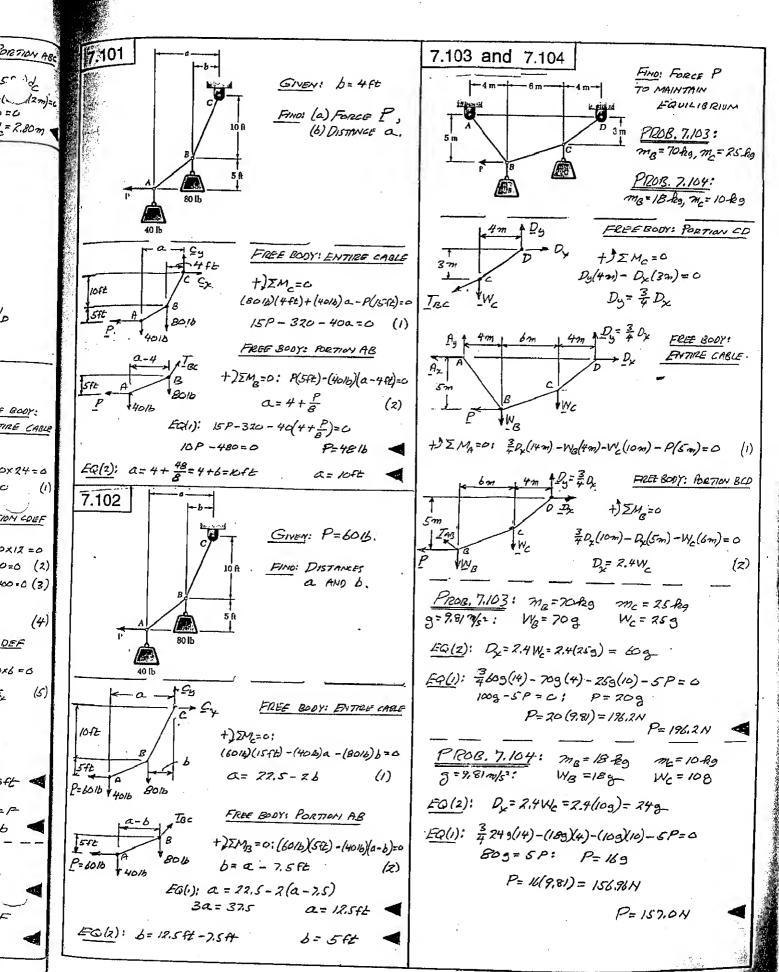


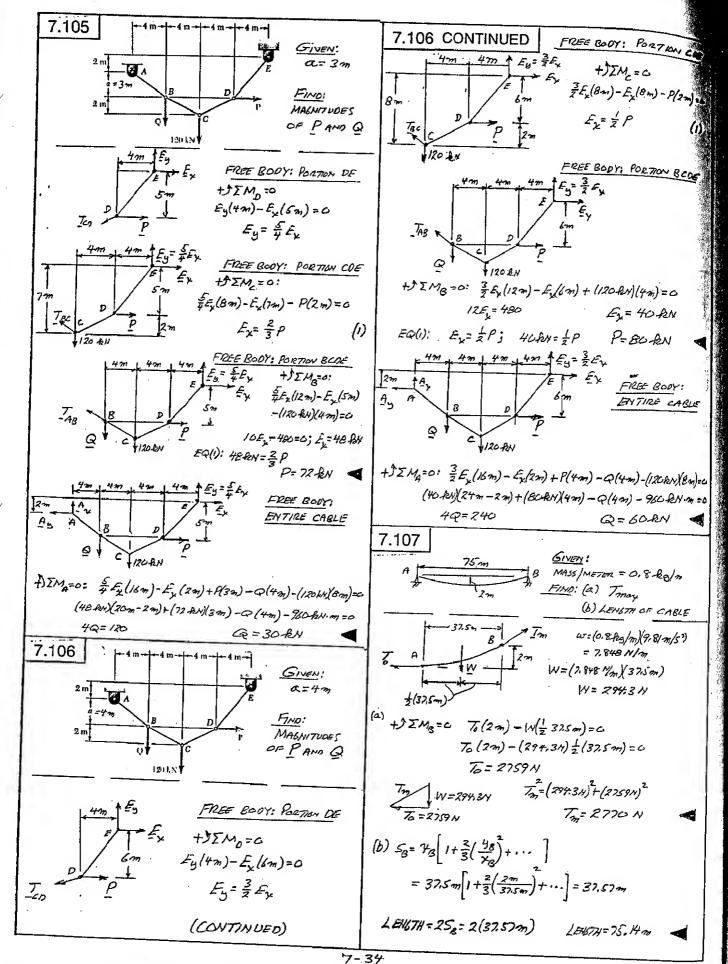


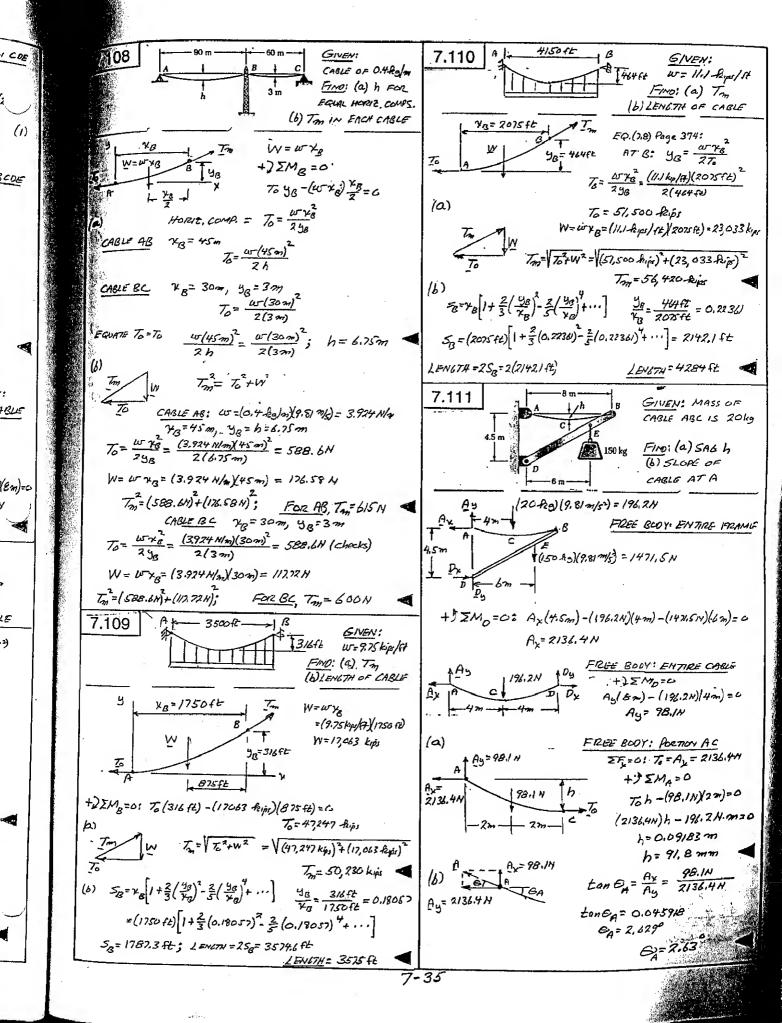


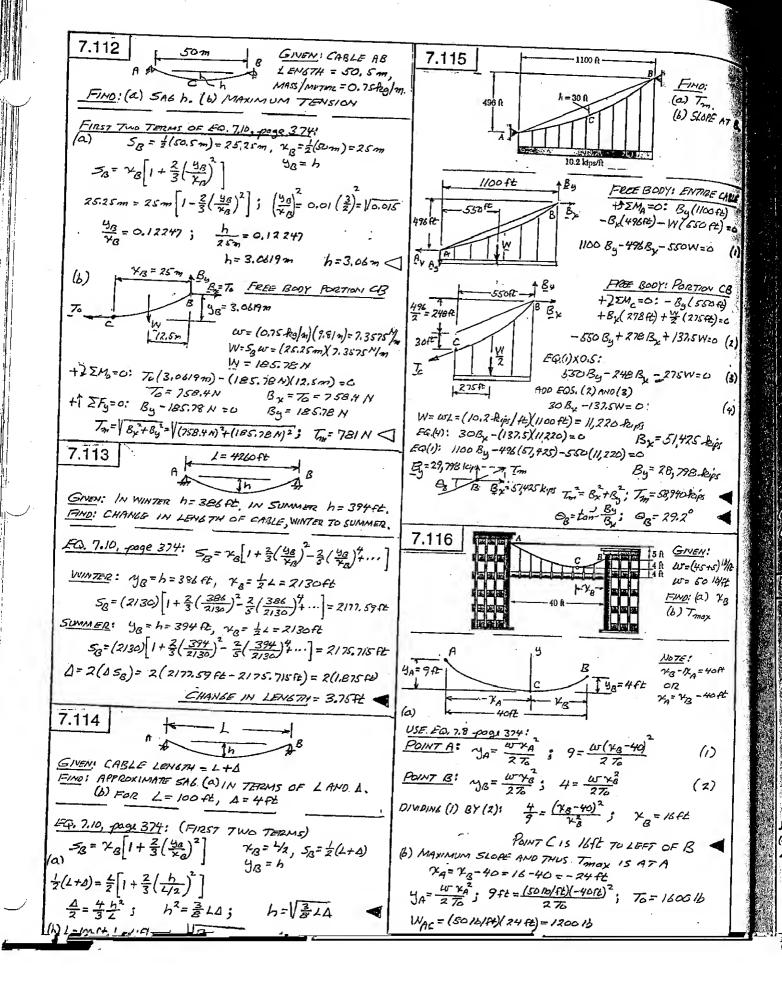


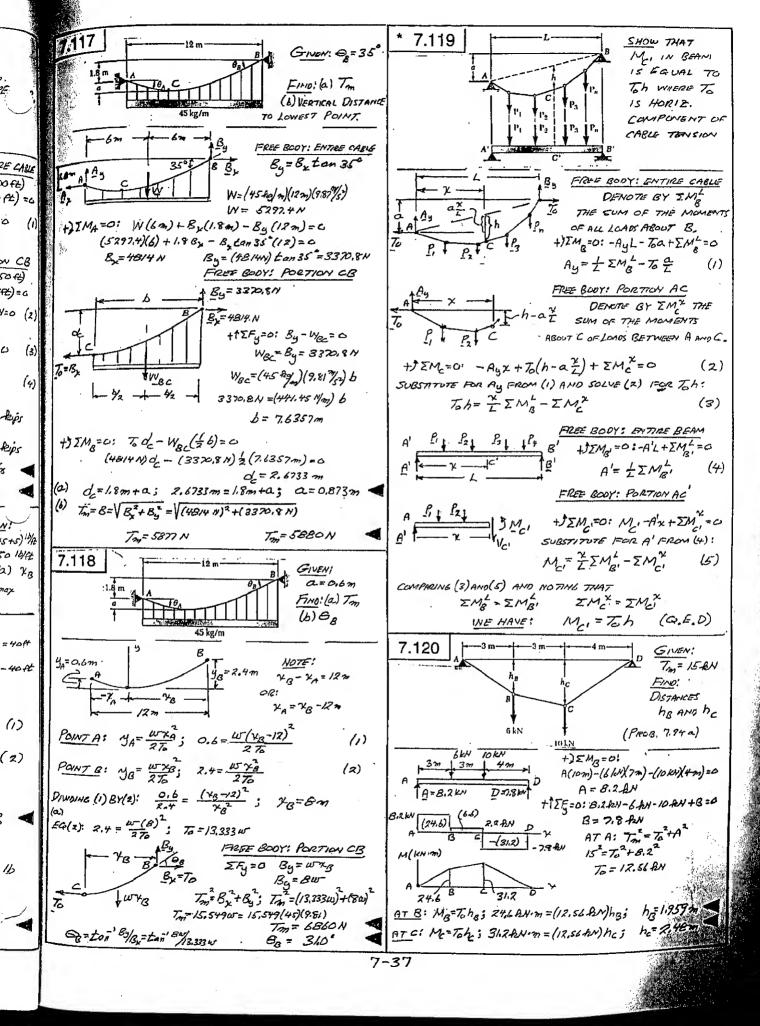


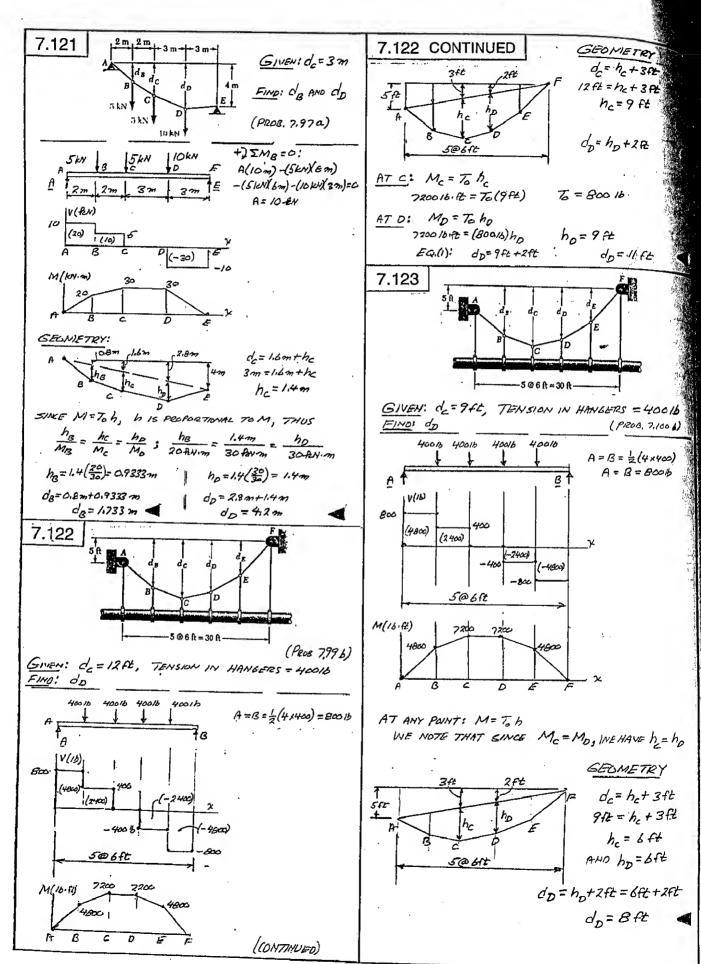




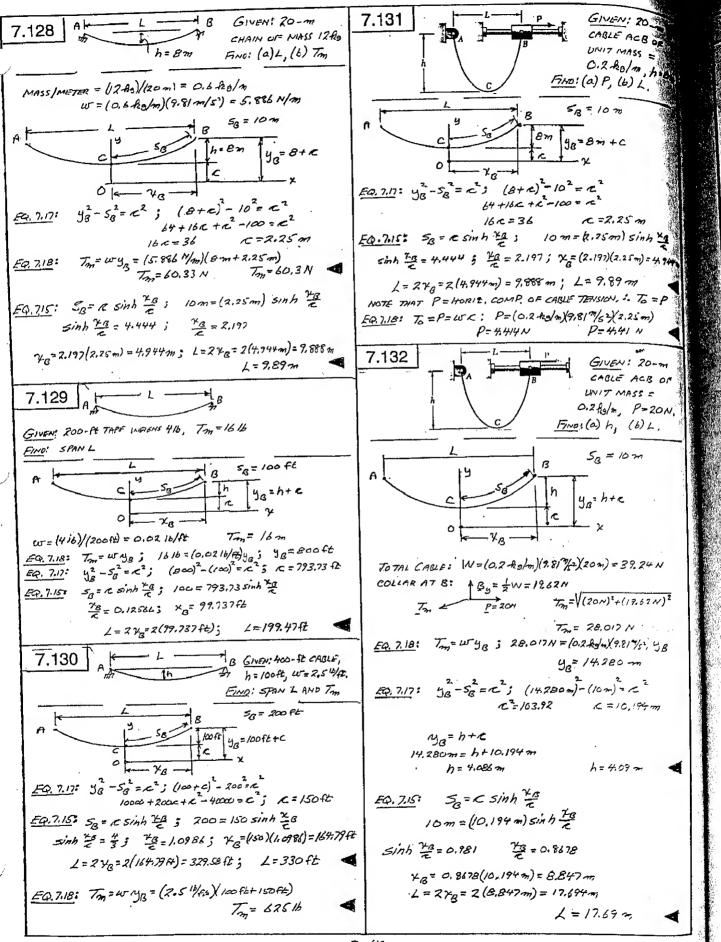








7.124 FOR A CARLE PROVE THAT $\frac{d_1^2}{d_2^2} = w(x) T_0$ FORMED BY A CARLE IS A CIRCULAR ARC. $\frac{d_2^2}{d_2^2} = w(x) T_0$ FORMED BY A CARLE IS A CIRCULAR ARC. $\frac{d_2^2}{d_2^2} = w(x) T_0$ FORMED BY A CARLE IS A CIRCULAR ARC.



133

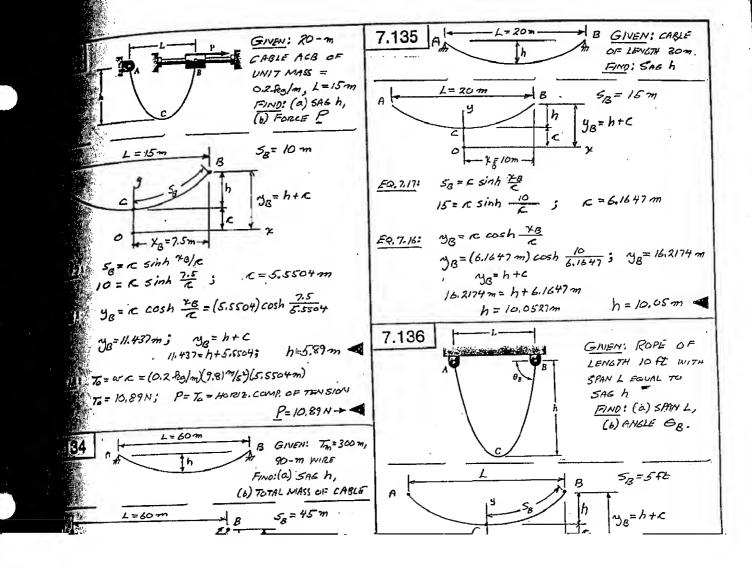
EQ. 7.1

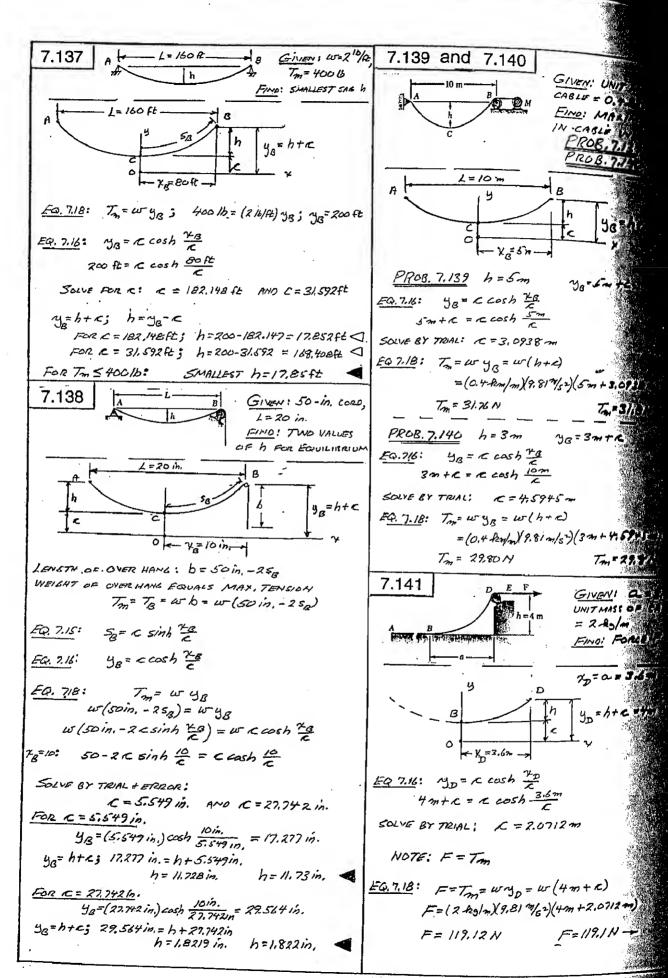
FQ.7.16

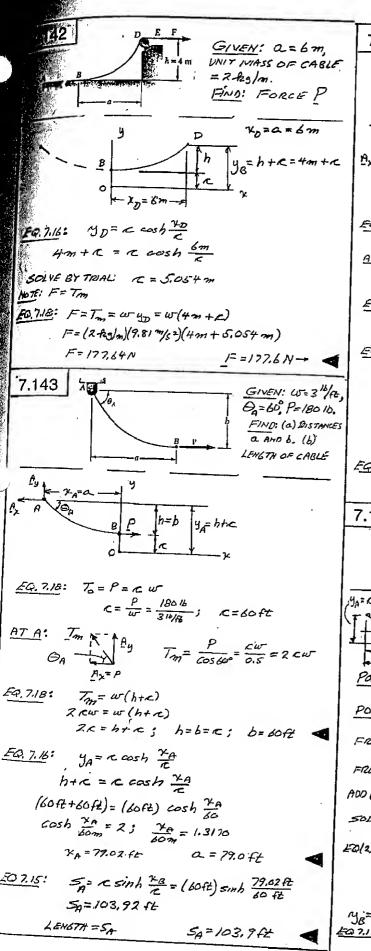
FQ. 7.1

7.1

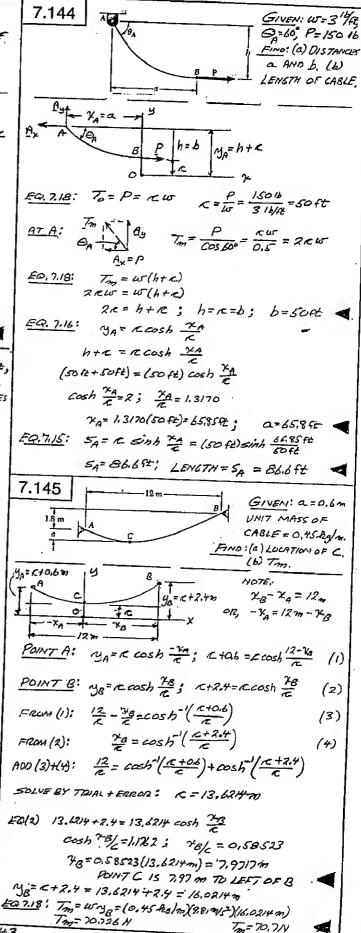
£φ.

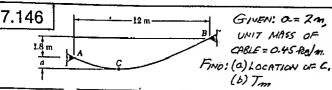


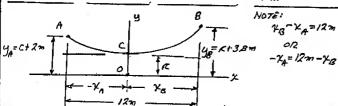




7-43







From (1):
$$\frac{12}{E} - \frac{4g}{E} = \cosh^{-1}\left(\frac{E+2}{E}\right)$$
 (3)

FROM(2):
$$\frac{\gamma_B}{C} = \cos h^{-1} \left(\frac{C + 3B}{C} \right) \tag{4}$$

$$ADD(3)+(4): \frac{12}{c}=cosh^{-1}\left(\frac{c+2}{c}\right)+cosh^{-1}\left(\frac{c+3B}{c}\right)$$

SCLUE BY TRIAL AND ENROR: K=6,8154 m

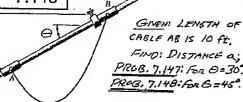
EQ.(2):
$$6.8154m + 3.8m = (6.8154m) \cosh \frac{7.8}{6}$$

 $\cosh \frac{7.8}{6} = 1.5576 \qquad \frac{7.3}{6} = 1.0122$

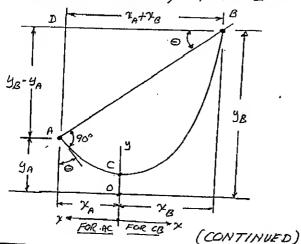
POINT (15 6.90 m TO LEFT OF B

MB= K+3.8 = 6.8154+3,8 = 10.6154m EQ(7.18): Tm = 15 yB = (0,45-ho/m)(9,81 9/52)(10,6154 m) Tm= 46,86 N Tm=46.9N

*7.147 and 7.148



COLLAR AT A: SINCE y=0, CABLE I ROD



*7.147 and 7.148 CONTINUED

$$\frac{Point A: \quad y = c \cosh \frac{x}{c}; \quad \frac{dy}{dx} = \sinh \frac{x}{c}}{tan \Theta = \frac{dy}{dx} \Big|_{x} = sinh \frac{xA}{c}}$$

$$tan \Theta = \frac{dy}{dx} \Big|_{x} = sinh \frac{xA}{c}$$

$$\sinh \frac{x_3}{c} = \frac{10}{c} - \sinh \frac{x_4}{c}$$

$$x_3 = c \sinh^{-1} \left[\frac{10}{c} - \sinh \frac{x_4}{c} \right] \qquad (2)$$

$$y_A = \cosh \frac{y_B}{\kappa}$$
 $y_B = \kappa \cosh \frac{x_B}{\kappa}$ (3)

$$\frac{1/4 \text{ ABD}}{\text{MBD}}: \quad \pm a_{B} = \frac{y_{B} - y_{A}}{y_{B} + y_{A}} \tag{4}$$

METHOD OF SOLUTION:

FOR GIVEN VALUE OF B, CHOOSE TRIAL

VALUE OF IC AND CALCULATE: FROM EC(1): XA

USING VALUE OF XA. AND K, CALCULATE:

1720M EQ(2): 2B

FROM EQ(3): YA AND YB SUBSTITUTE VALUES OBTAINED FOR TA, TB, JA, JB

INTO EQLA) AND CALOULATE &

CHOOSE NEW TRIAL VALUE OF & AND REPEAT ABOVE PROCEDURE UNTIL CALCULATED VALUE OF G IS EQUAL TO GIVEN VALUE OF G.

PROB.7.147: GIVEN VALUE: 6=30 RESULT OF TRIAL AND EIRIOR PROCEDURG C=1.803 m

74= 2.3745 m 7-8=3.6937 m JA = 3.606 m

a= y= y4 = 7.109m - 3.606m = 3.503 m a= 3,50 m

PROB. 7.148: GIVEN VALUE: @ = 45° RESULT OF TRIAL AND ERROR PROCEDURE C= 1.8652m

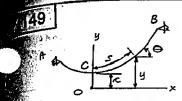
XA= 1.644 m

72=4.064m

MA= 2.638 m

7B= 8.346 M

a= y8 - y4 = 8,346m - 2.638m = 5.708m a=5.71 m



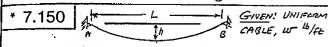
GIVEN: UNIFORM CABLE

Prove: (a) S= c tan 6.
(b) y= c sec 6.

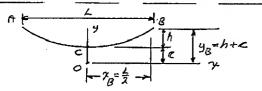
$$\cosh \frac{x}{E} = \sqrt{1 + \sinh^2 \frac{x}{E}} = \sqrt{1 + \tan^2 \Theta}$$
 (1)

$$1+\tan^2\theta$$
 $\tan \theta$ $\cos \theta = \frac{1}{\sqrt{1+\tan^2\theta}}$ (2)

SUBSTITUTE (2) INTO (1):
$$\cosh \frac{v}{c} = \frac{1}{\cos \theta}$$
 (3)



FIND: (a) MAXIMUM SPAN FOR GIVEN VALUE Tom
(b) MAXIMUM SPAN FOR W=0,2516/ft AMO Tom BOOGIB



WE SHALL FIND RATTO (+B/L) FOR WHICH Tom IS MINIMUM

$$\frac{dT_m}{d(x_{a/2})} = \omega x_{B} \left[\frac{1}{x_{a/2}} \sinh \frac{x_{B}}{c} - \left(\frac{1}{x_{B/2}} \right) \cosh \frac{x_{B}}{c} \right] = 0$$

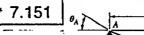
SOLVE BY TRULL AND ENRON FOR:
$$\frac{\chi_{B}}{\kappa} = 1.200$$
 (1)

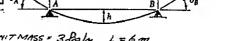
$$\frac{E0.7/7}{9B^{2}-S_{B}^{2}-E^{2}} M_{B}^{2} = \kappa^{2} \left[1+\left(\frac{S_{B}}{E}\right)^{2}\right] = \kappa^{2} \left(1+1.509^{2}\right)$$

$$4B^{2} 1.810 \kappa$$

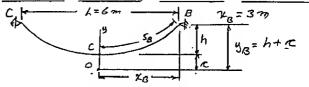
EG(1): 4 = 1.509 C= 1.509 Tay/1.8100 = 0.6630 Tom

(b) FOR W= 0.25 HA AND Tom= 800016,





GIVEN: UNITMASS = 3 Aglar, L=6 m FINDS TWO VALUES OF h FOR WHICH Ton= 350 N



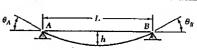
iv=(3/2/2)(9,81 m/s2)= 29.43 N/m

SOLVE BY TRIAL AND ERROR FOR TWO VALUES OF R

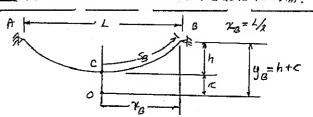
K = 11.499.m h=yB - K

h=11.893m-11.499m h=0.394m





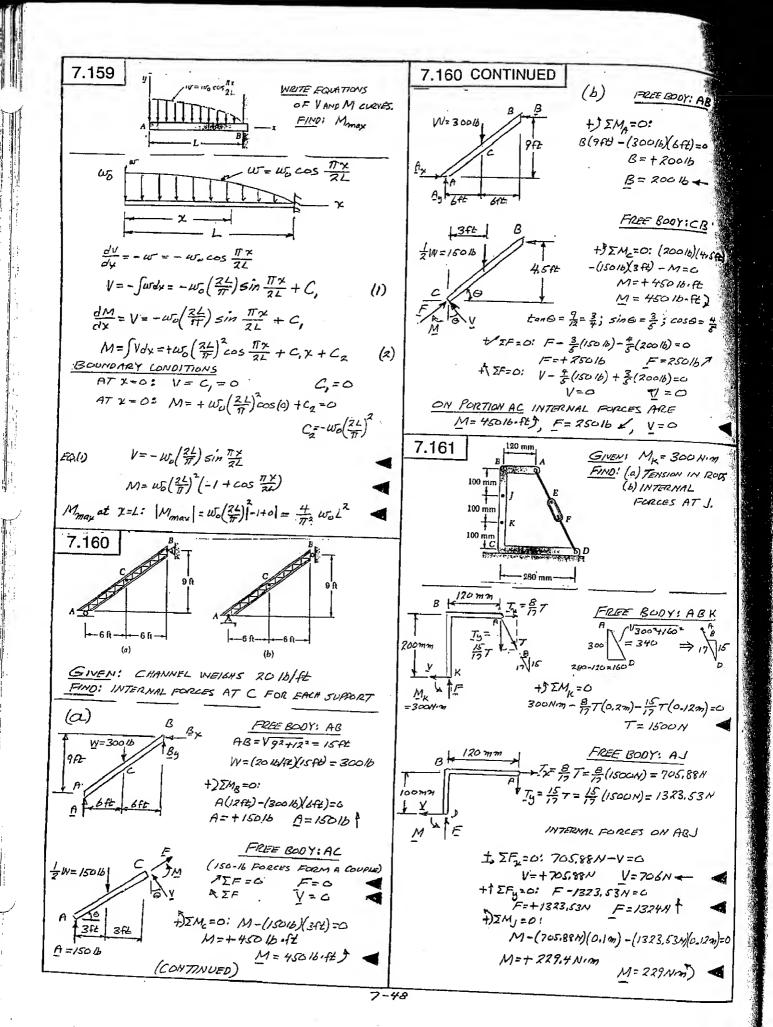
FIND THE ML RATIO FOR TOTAL WEIGHT EQUAL TO Tom.

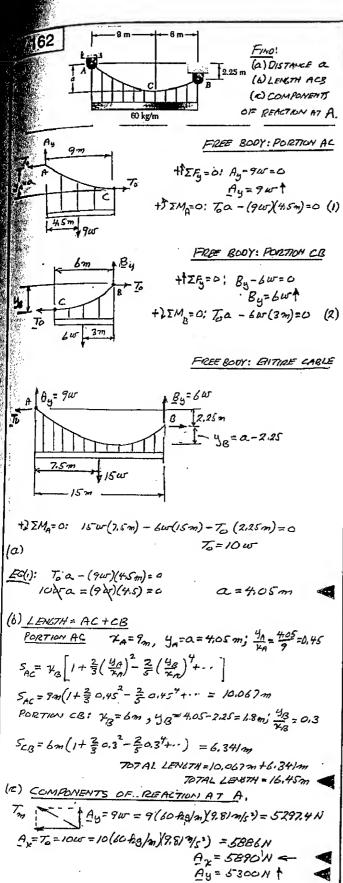


TOTAL WEIGHT: W= (250) W; : Ton= 250 W

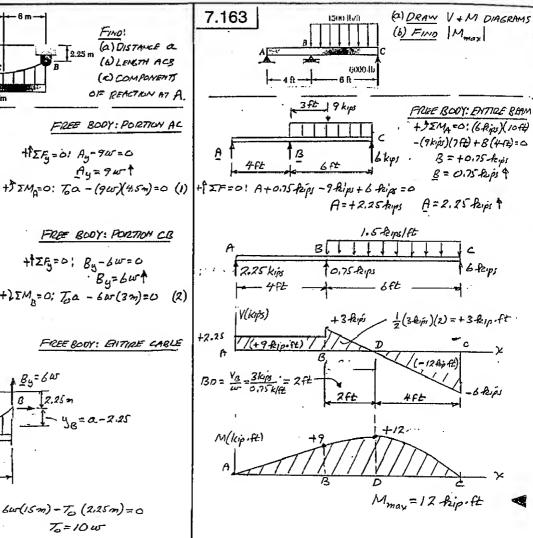
$$h = y_B - \kappa = \kappa \cosh \frac{\gamma_a}{\kappa} - \kappa = \kappa \left[\cosh(0.5493) - 1 \right]$$

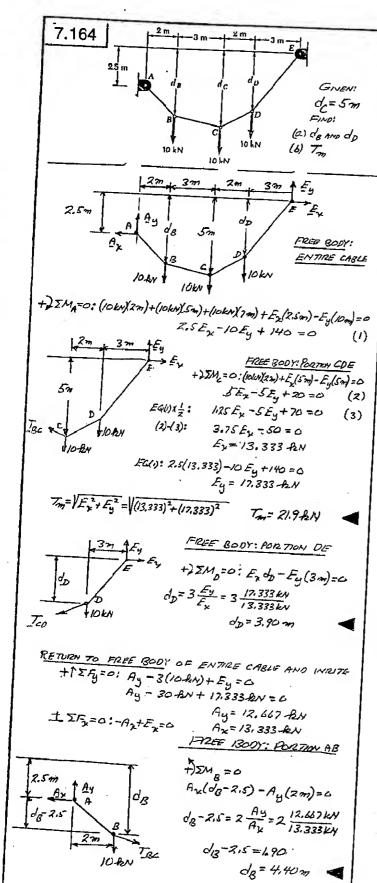
THUS:
$$h = (0.1547) \frac{\gamma_B}{0.5493} = 0.2816 \gamma_B$$

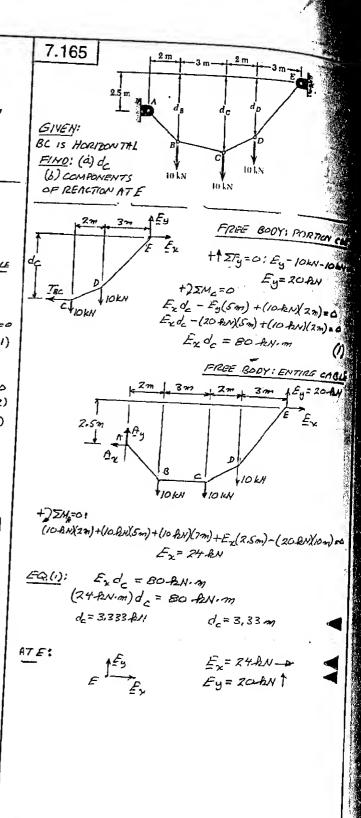


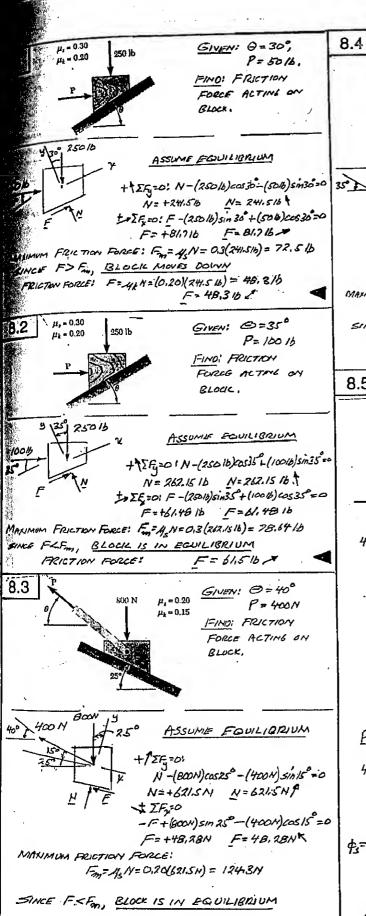


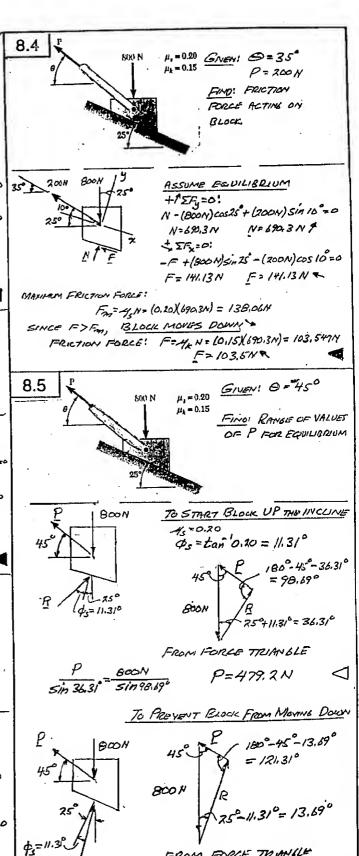
('-}'



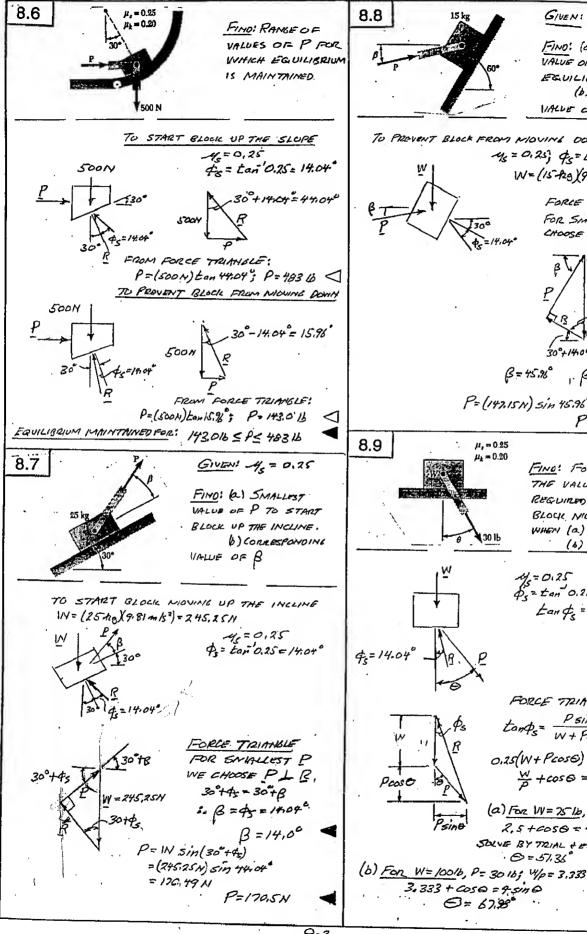


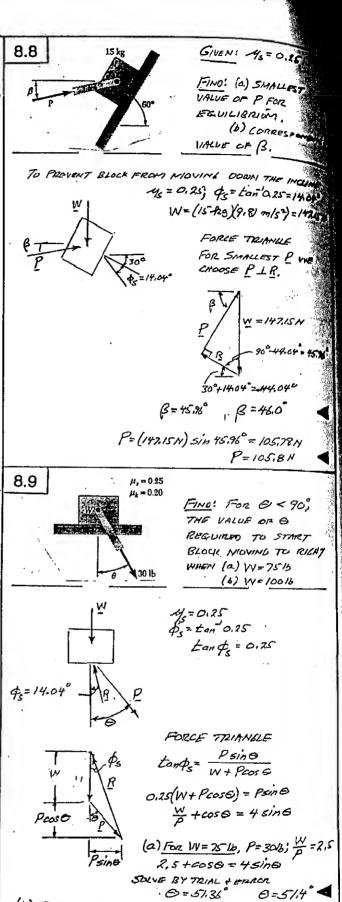






F=48.3NK



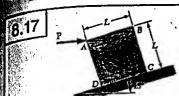


0=51.4°

G=68.0°

AND B, 45=0.8
AND B, 45=0.8
AND INCLINE, 72
DILLE OF O

WHICH MOTOR
IMPERIPING



GIVEN: MASS OF

CRATE = 30Ag.

Fino: (A) LARGET AS FOR:
WHICH CRATE CAN BE

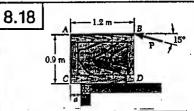
STARTED UP WITH HO

TIPANG. (b) CORRESPONDING:

MALHMUDE OF HORIZONTAL FUNCE ?.

FOR THPPING TO BE IMPENDING REACTION IS AT C.

FREE BODY! CRATE THREE-FORCE BODY, REACTION S



GIVEN: MASS OF

CRATE = 50 RO

FOR 0=0.2m TIPANS

IMPENOS

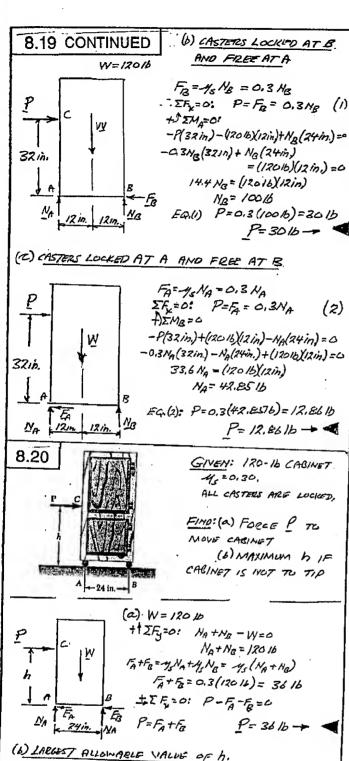
FIND (0) 45

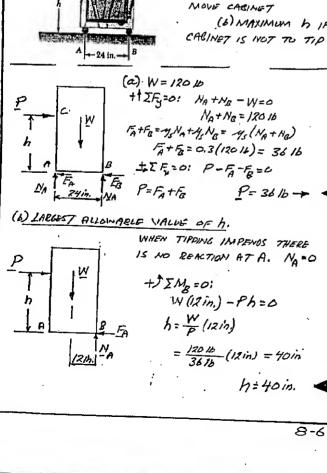
(6) MAGNITUDE OF P

PRIE BODY: CRATE THREE-FORCE BODY,

REACTION E MUST PASS THROUGH K WHETE

PANO W INTERSECT BECMETTRY





8.21

FB

r = RADIUS GIVENI W= WEIGHT, 45 IS SAME AT A AMO &

FIND: LARGET MIF CYLINDER IS NOT TO ROTAL

SINCE MOTION INILL IMPENO FB=45NB FA=45NA **t**_r

DEM =0: M- r = - r N = 0 M=rN+rE= rN+rys NA M= rHA(1+46)

+, IF, = 0: NA-F8 = 0; NA = MS NB (2) +1 IF4=0: NB+FA-W=0; NB=W-15NA

SUBSTITUTE FOR NB FROM (3) INTO (2): NA=45 (W-45 NA) NA(1+4,2) = 4/5 IN

SUBSTITUTE FOR INA INTE (1): M= Wrys (1+45) M= r -45 W (1+45)

8.22

GIVEN: Y = RADIUS W=WEIGHT . FIND! LARGEST M IF CYLINDER IS NOT TO ROTATE

SINCE MIGTION WILL IMPEND

(a) FOR 4,=0, 48=0.30, (b) For 4=0.25, 4=0.30.

F=4ANA F=40NB +) IMB=0: M-rf-rN=0 M=rNA+rFA=rNA+ryANA M= rnp(1+MA) (i)

+ [F=0: NA-FB=0 NA=MBNB (2)+ 1 IFy=0: NB + FA - VY=0 NB=W-YANA (3)

SUBSTITUTE FOR No FROM (3) INTO (2) NA=48 (W-4A NA)

NA = 40W NA (1+1/A/B) = 4BW

EQ.(1): M= + 1+4948 (1+49) M=WY 48(1+49)

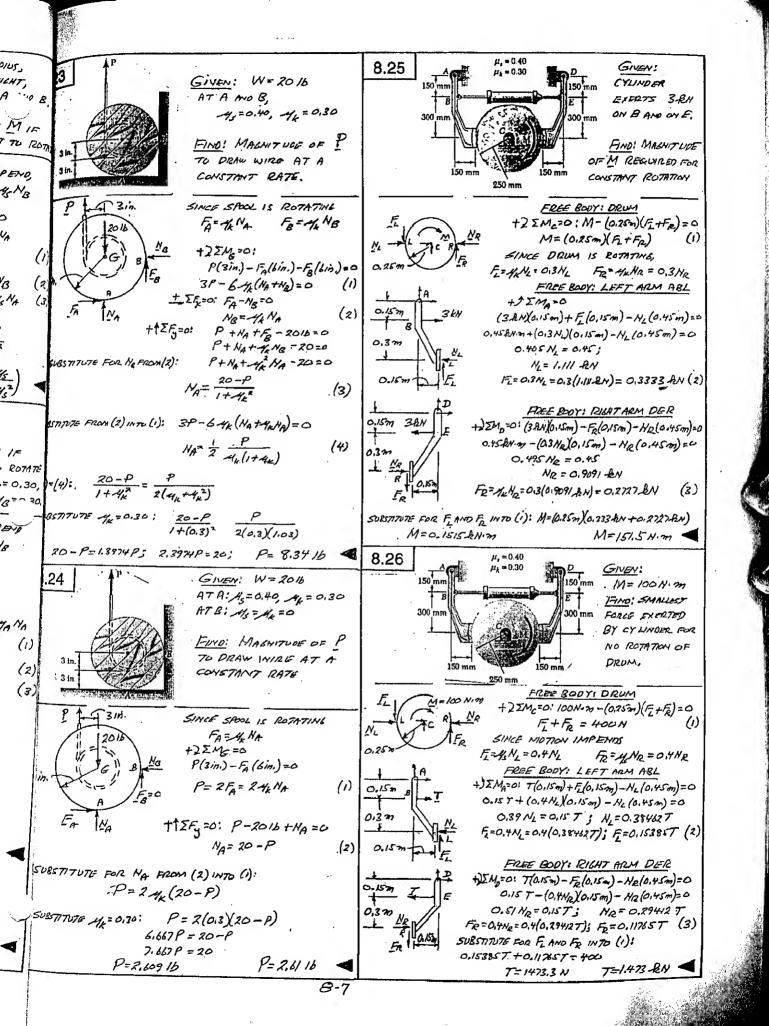
(a) FOR MA = 0. AND MB = 0.30:

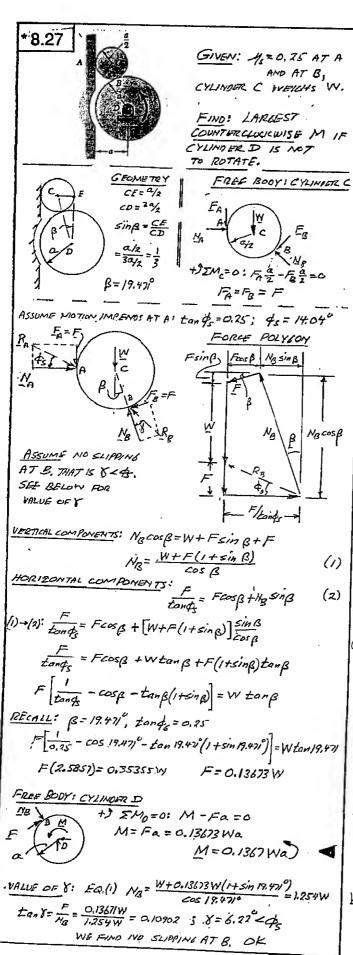
M=Wr 0,30 M=0,300 Wr

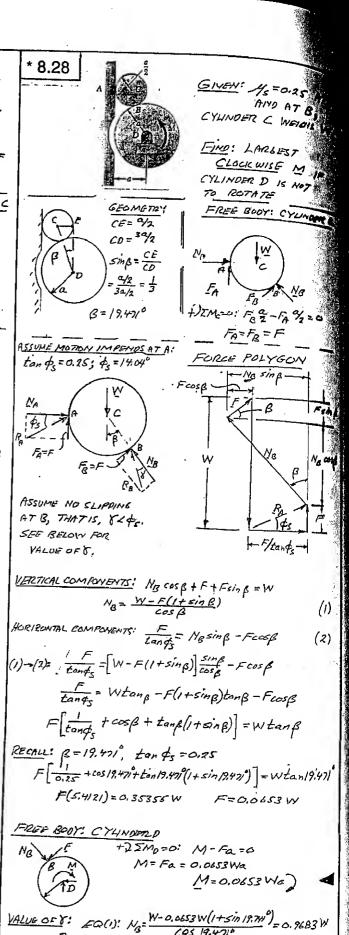
(b) FOR 4=0.25 AND MB=0.30:

M= Wr (0.30)(1+0.25) = Wr (0.30)(1.25) 1+(0.25)(0.30)

M=0,3488Wr M=0,349Wr



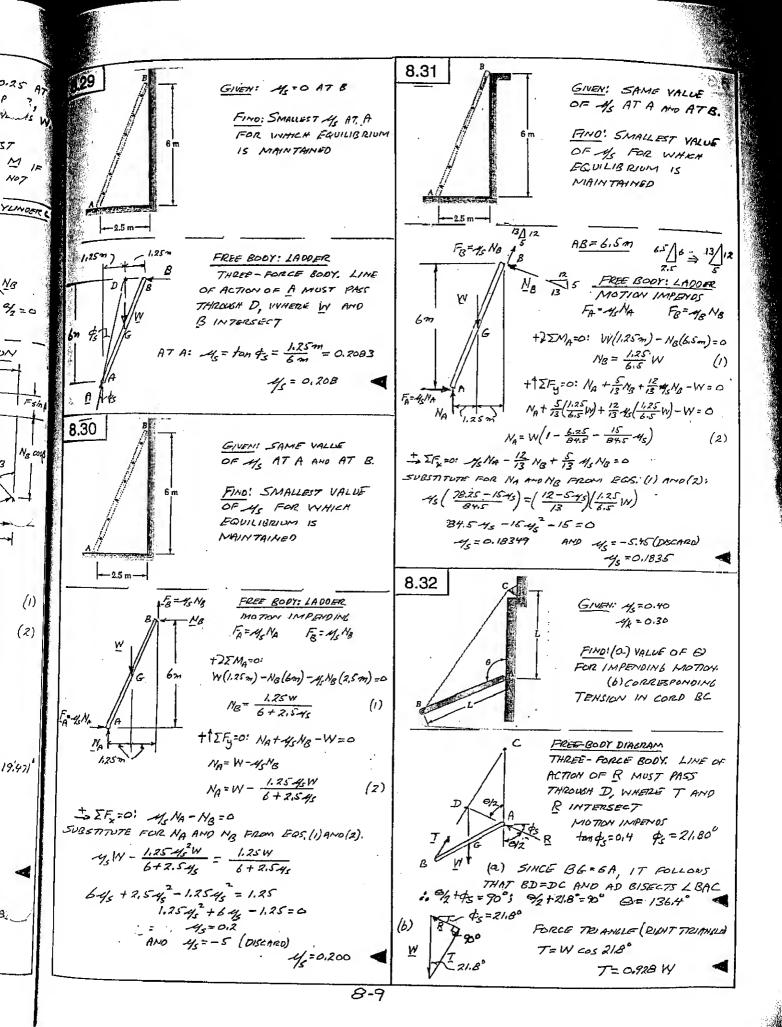


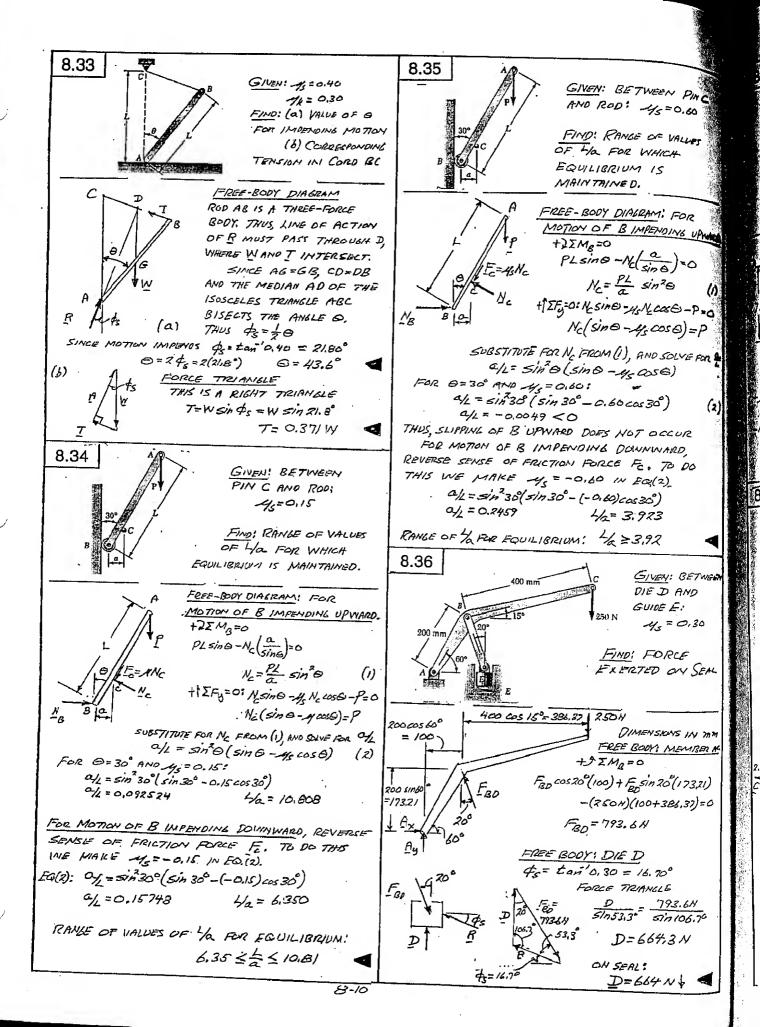


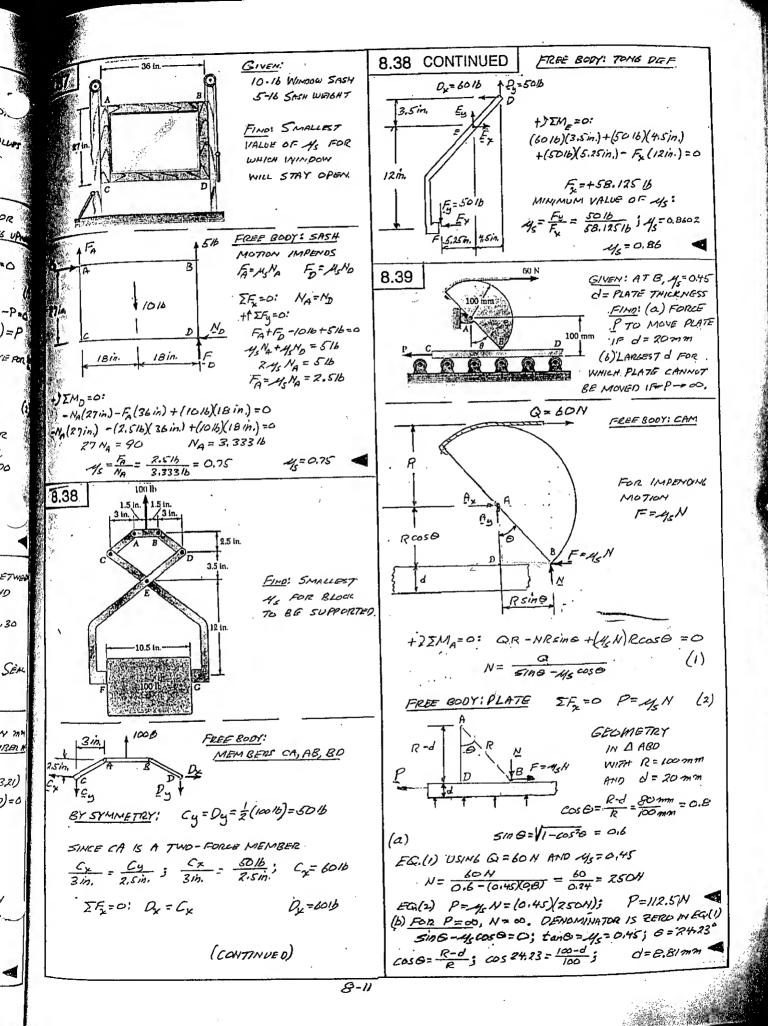
COS 19.4710

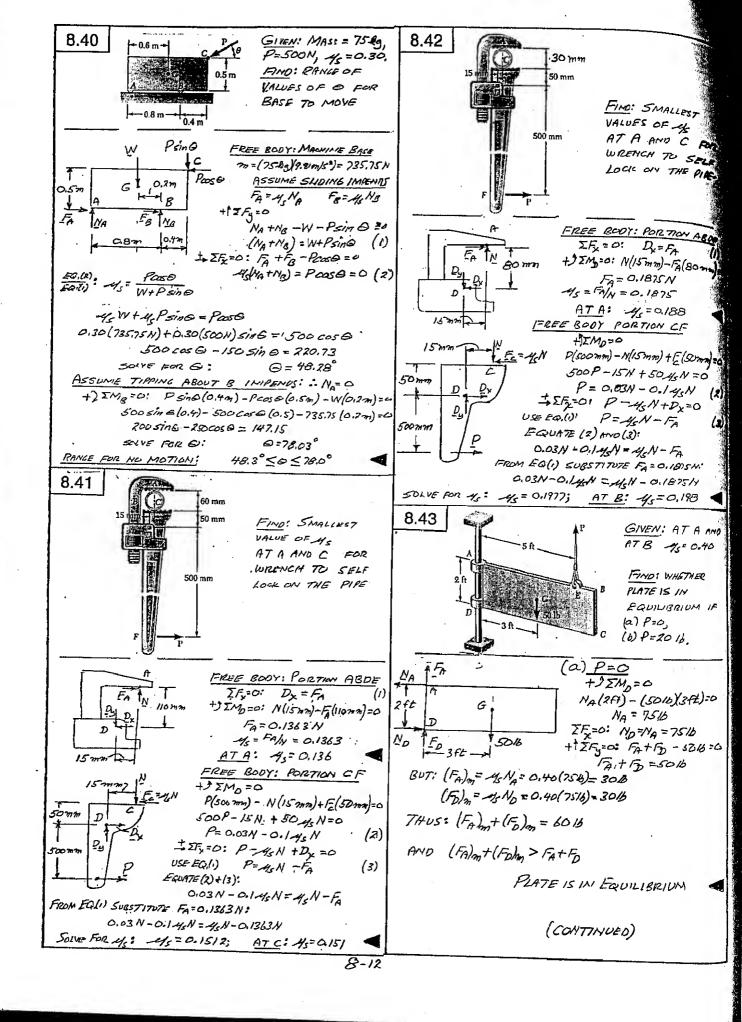
WE FIND NO SLIPANG AT B. OK

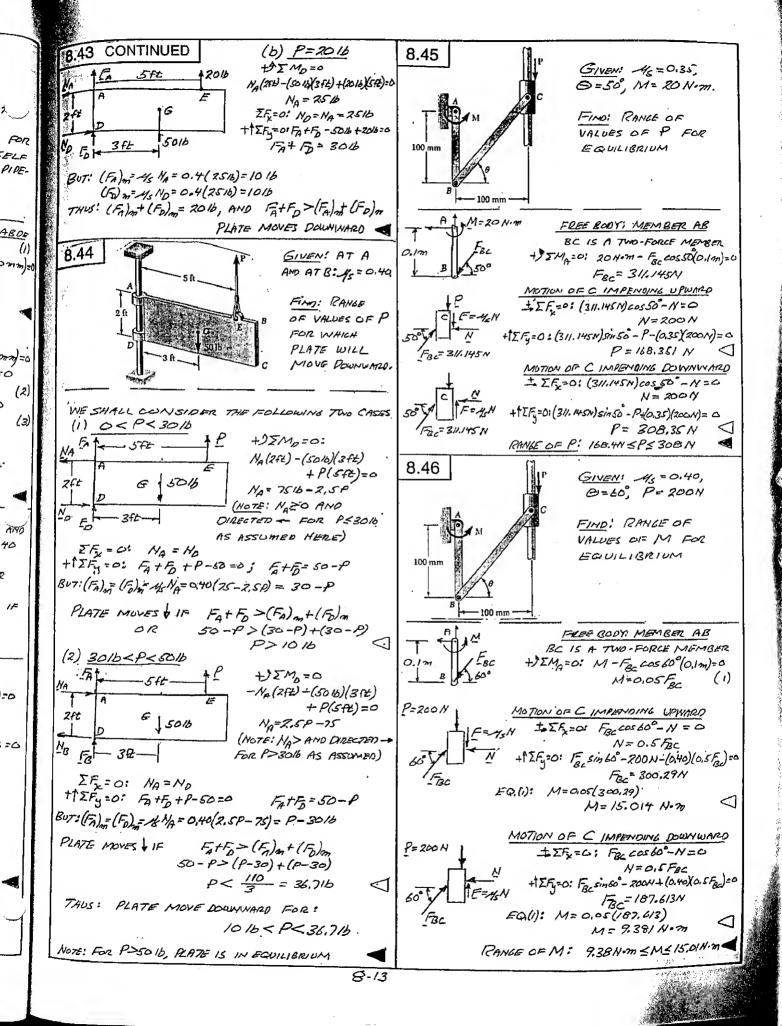
Land = F = 0.0653W = 0.0674; Y= 3.86°< \$

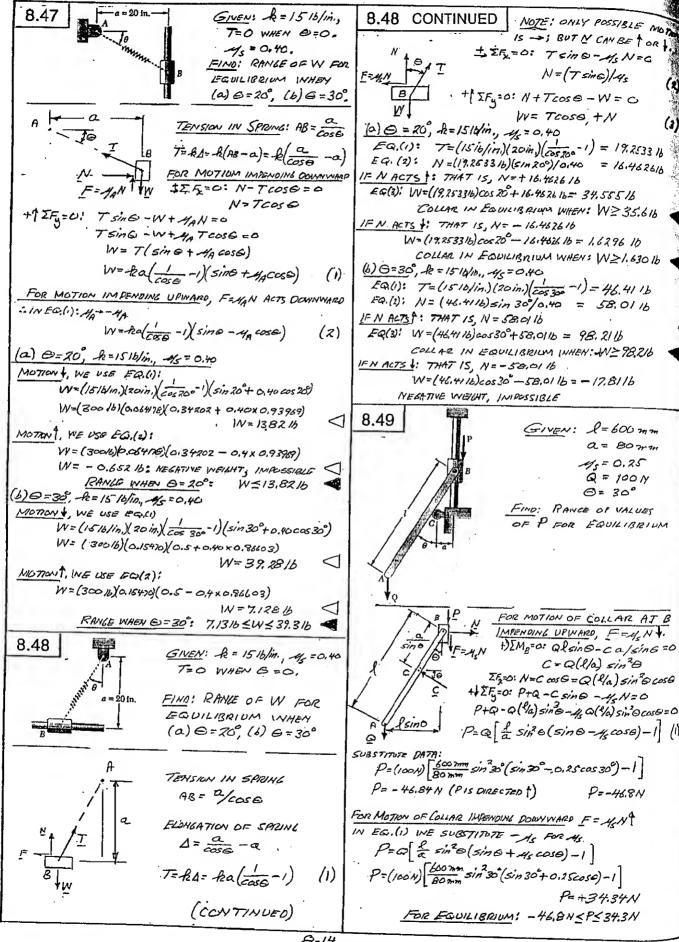


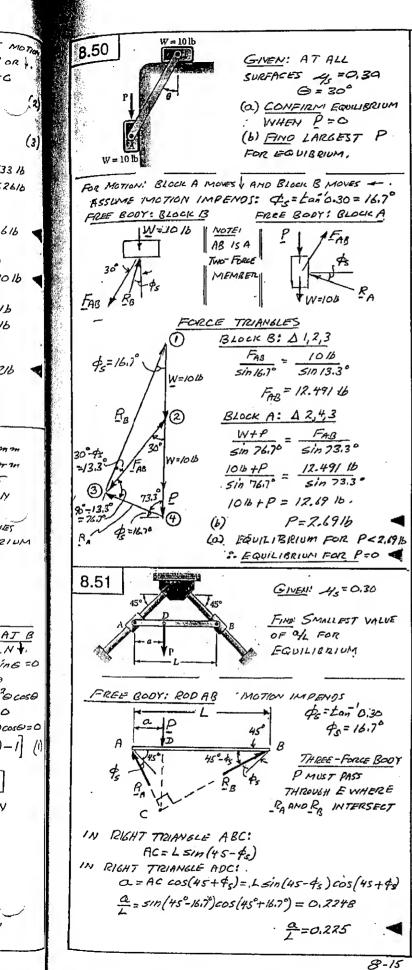


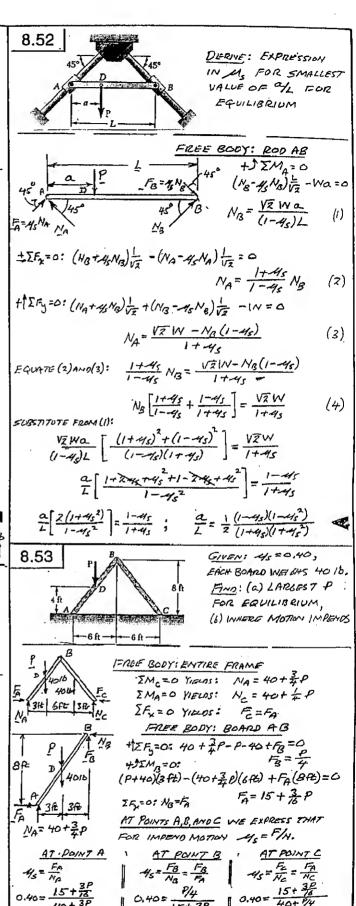












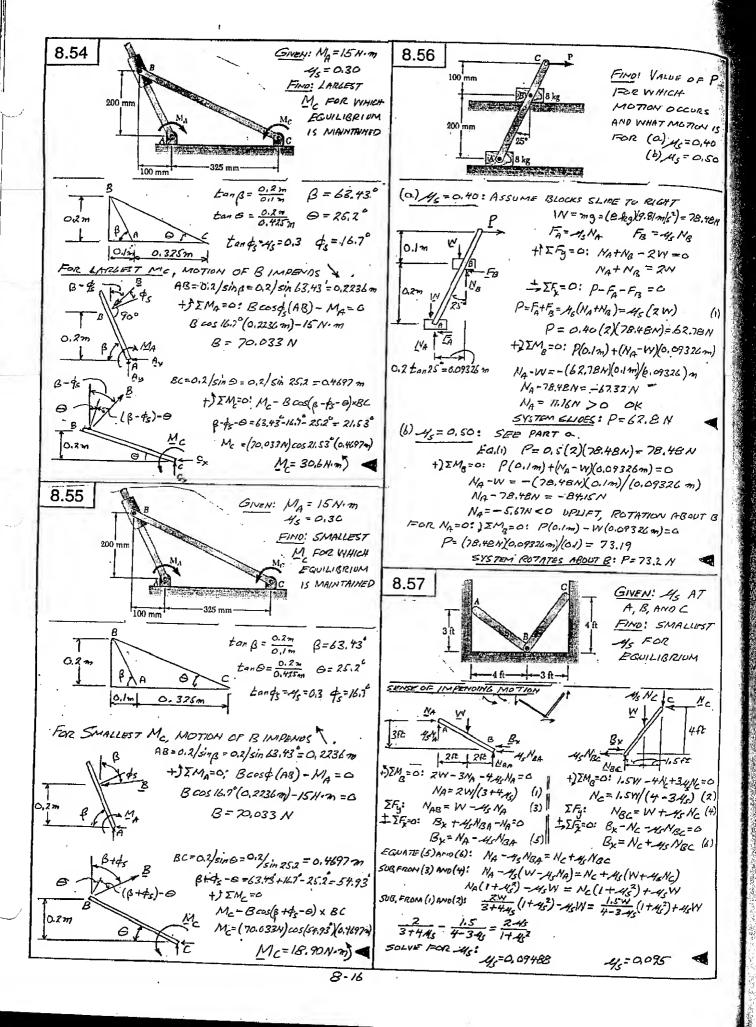
P= 34.291

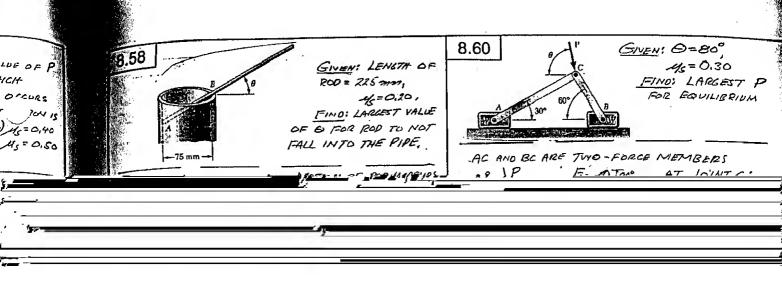
(a) PMAX = 11.4316 (b) MOTION IMPENOS AT C

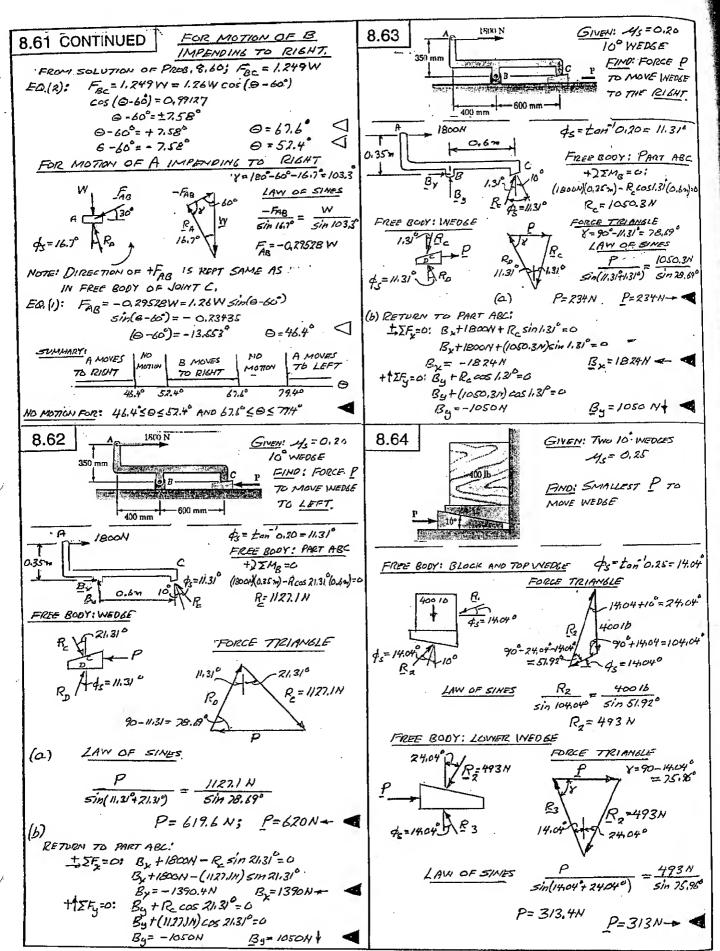
P= 11.429 16

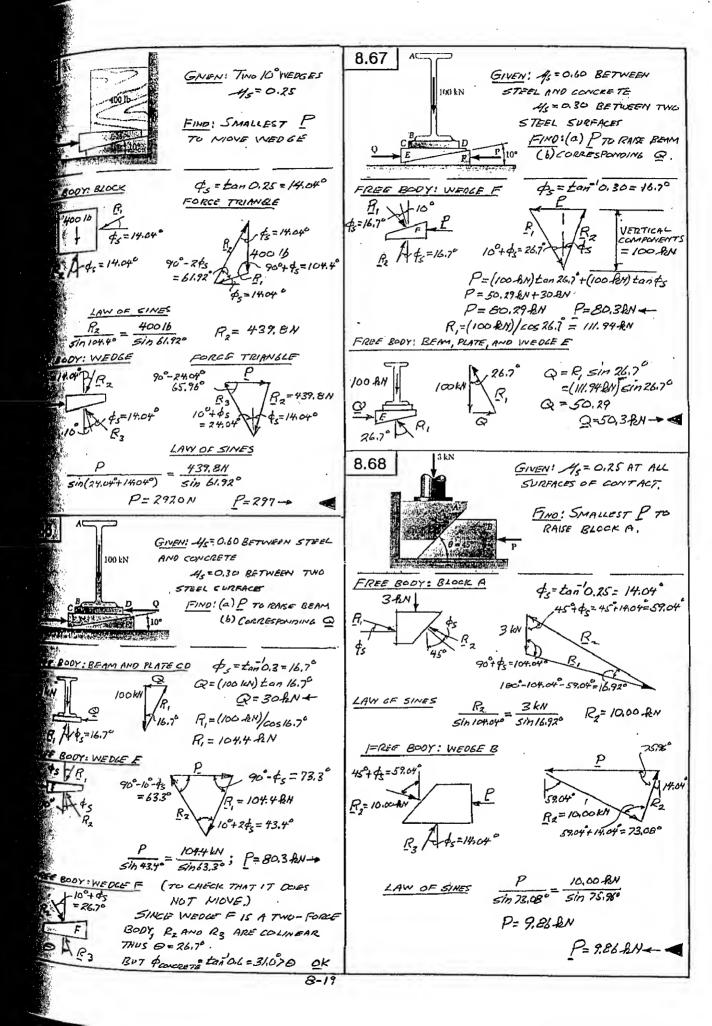
40+嬖

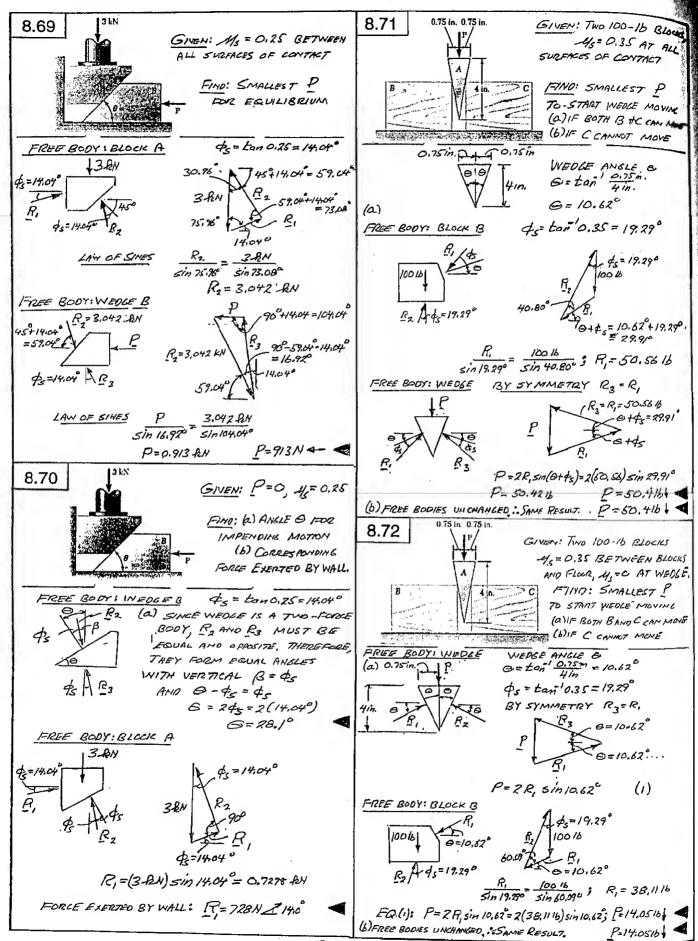
P=-8.88913

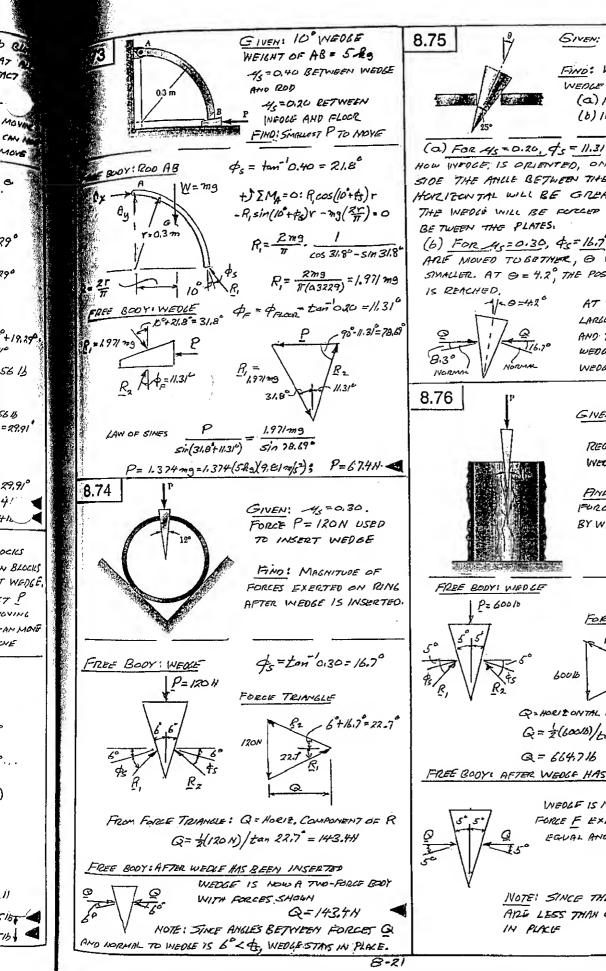












GIVEN: PLATE MOVE TOSETHER

FIND: WHAT HAPPENS TO

(a) IF 45=0,20.

(b) IF ys=0.30.

(a) FOR 45=0.20, \$= 11.31°, PEBARDLESS OF HOW INFOCE, IS OPLENTED, ON AT LEAST ONE SIDE THE ANGLE BETWEEN THE FACE AND THE HORIZONTAL WILL BE GREATER THAN OF. THE WEDGE WILL BE FORCED UP AND OUT FROM

(b) FOR 45=0.30, \$5=16.7°. AS THE PLATE ARE MOVED TUBETHER, O WILL BECOME SIMALLER. AT 0 = 4.2°, THE POSITION SHOWN

> AT THIS POSITION THE LARGER ANGLE BETWEEN Q AND THE NORMAL TO THE WEDGE IS 16.7", THE WEDGE WILL SELF LOCK,

GIVEN: 45 = 0.35 Force P=60016 REGULTED TO INSERT WEOCE

AND: MAGNITUOF OF FURCES EXERTED ON WOOD BY WEDGE AFTER INSURTION

FORCE TRIANGLE Rz_5419,29 = 24,290

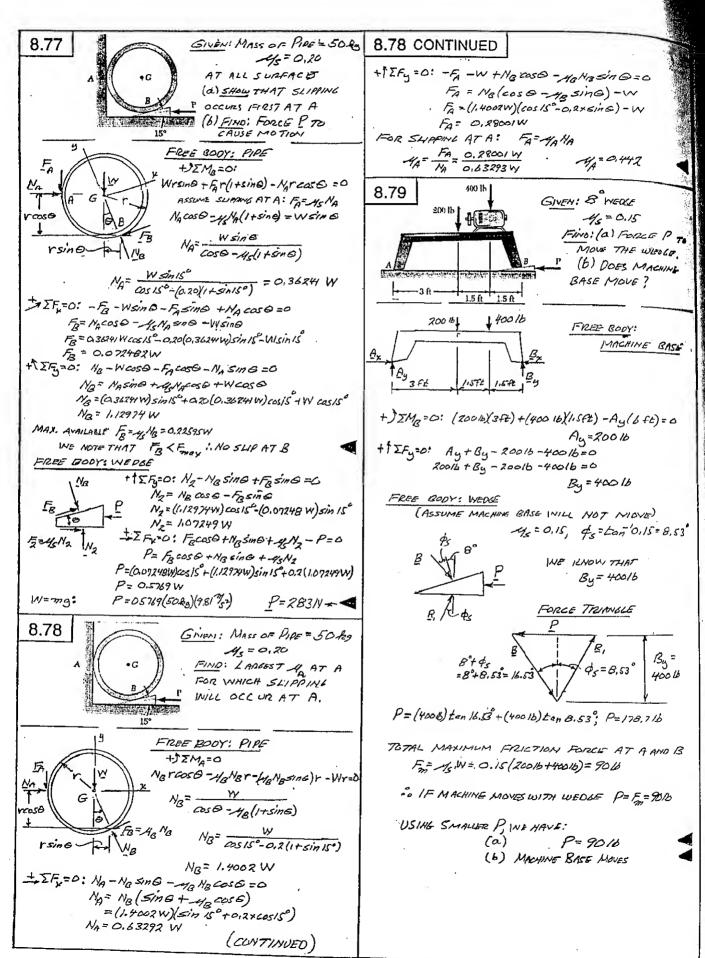
\$= tan-10.35=19.29°

Q=HORIZONTAL COMPENENT OF P. & Rz Q= = (600/6)/tan 24.290

FREE BODY AFTER WEOGE HAS BEEN INSENTED

INFORF IS NOW A TWO-FORE BODY. FORCE F EXERTED ON WOOD IS EGUAL AND OPPOSITE TO Q.

NOTE: SINCE THE & ANGLES SHOWN ARE LESS THAN OS. INFOLE STAYS



8.80 400 lh Gran

GNEH: E'WEDGE

-45 = 0.15

FIND: (a) FORCE P TO

MOVE THE WEDGE

(b) DASS MACHINE

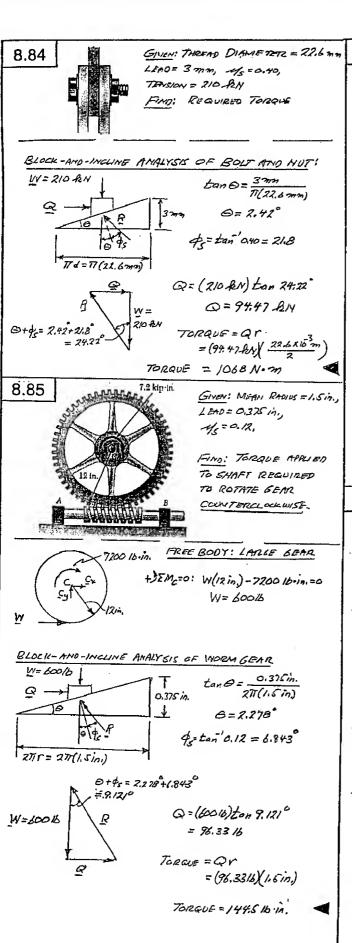
* 8.81 and 8.82 CONTINUED

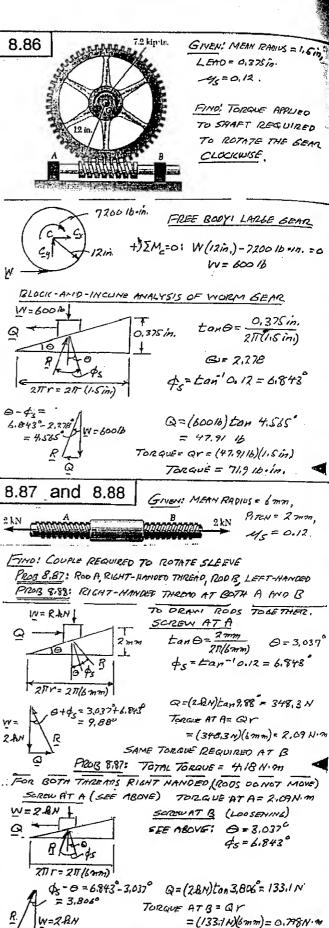
PROB 8.81: FREE BODY : BLOCK (ROLLERS REMOVED)

FORCE TRUMVELE

200 \$ 1 45

R. A. 15°+4

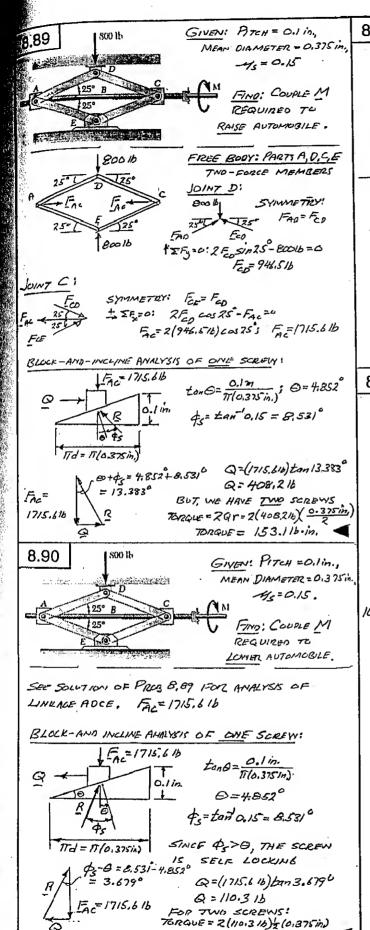




TOTAL TORQUE = 2.09 N. m + 0.798 N-m

TOTAL TORQUE = 2.89 N.m

PROB.8.88:



2

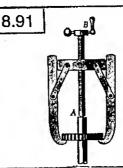
Ž.

0370

Nim

ve)

=0



GIVEN: LEAD = 4 mm,

MEAN RADIUS = 15 mm,

MS = 0.10,

FORCE TO BE APPLIED

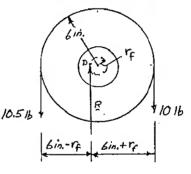
TO GEAL = 3 ARN.

FINO! TORQUE THAT MUST BE APPLIED TO SCREW.

8.92 1.5 in.

GIVEN: PULLET WEIGHS 516

FIND: COEFFICIENT OF STATE FRICTION IF A O.S-16 WEIGHT ADDED TO BLOCK A STARTS ROTATION.



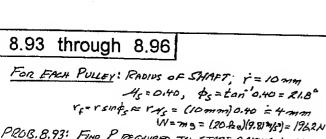
+) $\sum_{k=0}^{\infty} = 0: (10.516)(6in.-r_f) - (1016)(6in.+r_f) = 0$ $(0.516)(6in.) = (20.516)r_f$ $r_f = 0.14634in.$

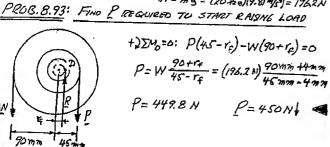
 $Y_f = r \sin \phi_s$ $\sin \phi_s = \frac{0.14634 \text{ in.}}{1.5 \text{ in}} = 0.09756$ $\phi_s = 5.5987^\circ$ $\phi_s = tan\phi_s = tan 5.5987^\circ$

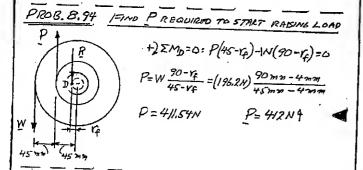
Ms=0,09B

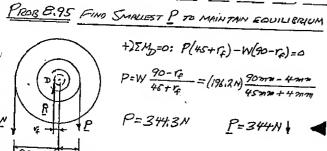
45=0,09003

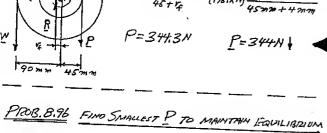
TORSUE = 41.416 . in.

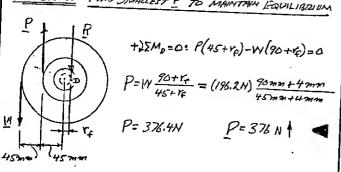


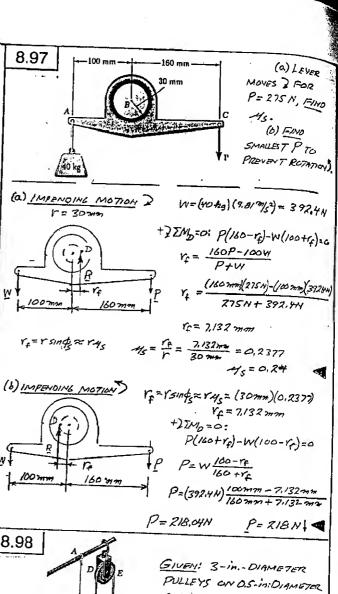












8.99

FOR

PUL

+12+

PU

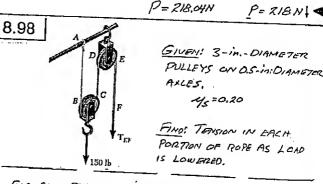
TEF

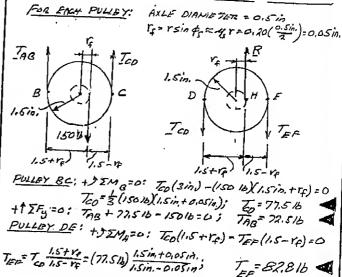
8.

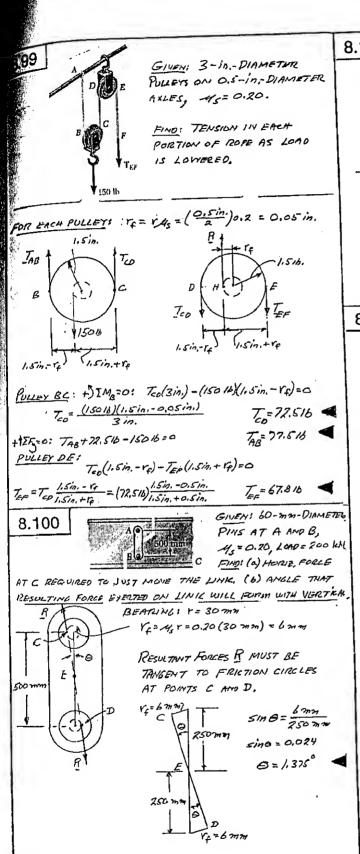
ΑT

IZE:

VE







Px=Ryton 0

= 4.80 PM

= (200ALN) tanl. 375°

HORIZ, FORCE = 4.80 RM

2.44

4)00

3724m)

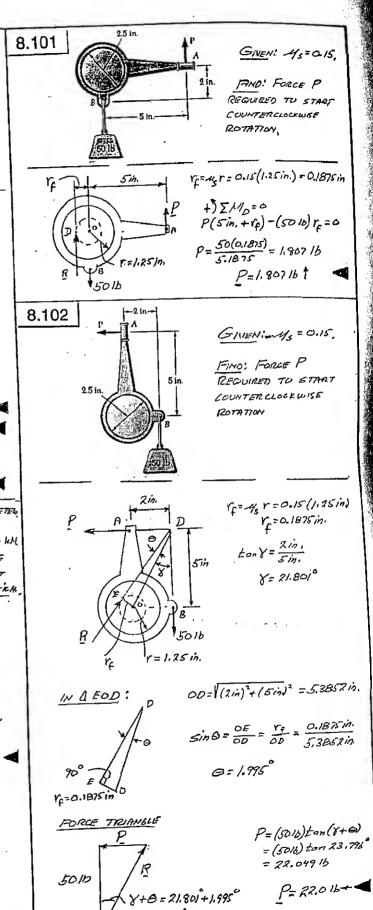
Ry=

WERT.

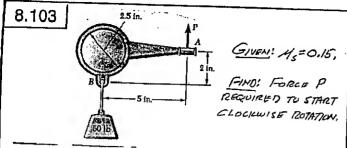
COMPONENT

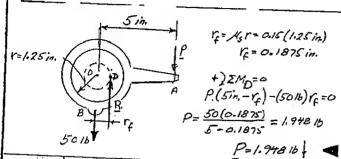
= 200 kN

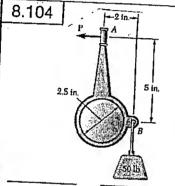
£0=1,375°



= 23,796

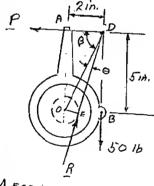






GIVEN: M5=0.15.

FIND: FORCE P REQUIRED TO START CLOCKWISE RUTATION

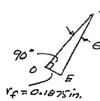


 $r_f = 4/s r = 0.15 (1.25 in)$ = 0.1875 in.

$$\tan \beta = \frac{5 \ln n}{2 \ln n}$$

$$\beta = 68.198^{\circ}$$

IN A EOD:



 $00 = \sqrt{(2in_1)^2 + (5in_1)^2}$ 00 = 5.3852 in.

 $\sin \Theta = \frac{OE}{OD} = \frac{0.1875 \text{ in.}}{5.3852 \text{ in.}}$

875in. @=1,994°

FORCE TRIANGE



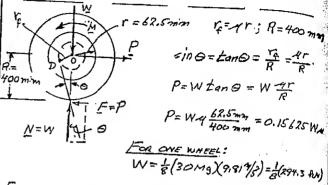
 $P = 68.198^{2} + 1.994^{0}$ $= 70.193^{0}$ $P = 50/\tan(\beta + 0) = \frac{5016}{\tan 70.192^{0}}$ P = 18.0116

B.105 GNEN: RAILROAD CAR OF MASS 30 Mg of KHT 600- mm - DIAMETER WHEEL WITH

125-mm-DIAMETER AXIES. HE = 0.000, MK = 0.015.

[FIND: HORIZONTAL FORCE REQUIRED(a) TO STATE

CAR MOVING (b) TO KEEP ITMOVING.



FOR EIGHT WHEELS OF RAIL ROAD CAR EF = 8(0.15625) = (294.3 PM) y = (45.984 y) LIN

(a) TO START MOTTON: MS=0.020 EP=(45.984X0.020)=0.9197 LW; EP=920N

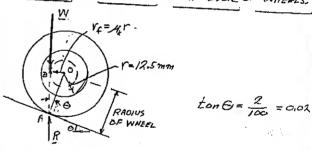
(b) TO MAINTAIN MO TION: MK = 0.015 EP=(45.984)(0.015) = 0.6297 for; EP=690N

8.106 GIVEN! SCOOTER IS TO ROLL DOWN

A 2 PERCENT SLOPE AT CONSTANT SPEAD.

AXLES OF WHEELS ARE 25 MM IN DIAMETER, 4/2 = 0.10.

FIND: REQUIRED DIAMETER OF WHEELS.

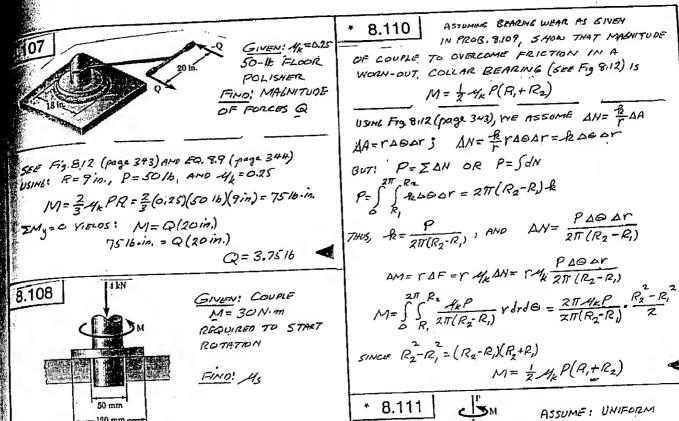


SINCE SCOOTER ROLLS AT CONSTANT SPEED, EACH WHEEL IS IN <u>EQUILIBRIUM</u>. THUS W AND R MUST HAVE <u>COMMION LINE OF ACTION</u> TANSENT TO THE FRICTION CIRCLE.

Vf= 14, V= (0.10)(12.5mm) = 1.25mm

 $CA = \frac{OB}{\tan \Theta} = \frac{V_4}{\tan \Theta} = \frac{1.25 \, \text{mm}}{0.02} = 62.5 \, \text{mm}$

DIAMETER OF WHEEL = 2(OA) = 125mm



SEE FIB. B.12 (page 343) AND EQ. B. B (page 344).

**USING! R;= 25mm = 0.025m

Rz=60 mm = 0.060 m

P=4,000 N, M = 30 Nim

 $M = \frac{2}{3} \mathcal{I}_S P \frac{R_2^3 - R_1^3}{R_2^2 - R_1^2}.$

25 W.

1.3 PM

A).

0,10,

=45_

30N·m= 2 45 (4000N) (0.060m)3- (0.025m)3
(0.060)2-(0.025m)2

ASSUME: UNIFORM
PRESSURE BIETWEEN
SURFACES OF CONTACT

SHOW THAT $M = \frac{2}{3} \cdot \frac{4kP}{\sin 0} \cdot \frac{R_2^3 - R_1^3}{R_2^2 - R_1^2}$

1 N= R 1A

8.112

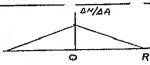
GIVEN: POLISHER OF WELLAT = 5016 4/x = 0.25

ASSUMES NORMAL FORCE

BETWEEN FLOOR AND DISK LIARIES LINEARLY FROM A MAXIMUM

AT CENTER TO ZERD AT EOGE

FIND: MAGNITUDE. Q OF FORCES TO PREVENT MOTION.



AN= & (1-F)

DA- rab ar

$$P = \sum \Delta N = \int dN = \int \int \frac{1}{R} \left(1 - \frac{r}{R}\right) r d\theta dr = 2\pi A \left[\frac{r^2}{2} - \frac{r^3}{3R}\right]^R$$

$$P = R \frac{\pi R^2}{2}$$

$$\Delta M = r \Delta F = r \sqrt{k} \Delta N = \frac{3PM_b}{\pi R^2} \left(1 - \frac{r}{R} \right) r^2 \Delta \omega \Delta r$$

$$M = \sum_{n} \Delta M = \int_{0}^{2\pi} \int_{R^{2}}^{R} \frac{3PA}{\pi R^{2}} \left(r^{2} - \frac{r^{3}}{R}\right) d\theta dr = \frac{2\pi}{\pi} \cdot \frac{3PA}{R^{2}} \left[\frac{r^{3}}{3} - \frac{r^{4}}{4R}\right]_{0}^{R}$$

$$M = \frac{1}{2} M_{L} PR$$

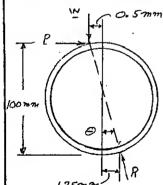
4=0.25, P=501b, R=9in

8.113



GIVEN: 900-kg BASE; 100-mm DIAMETER PIPES, ROLLING RESISTANCE IS

0.5m BETWEEN PIPES AND BASE + 1,25mm BETWEEN PIPES FIND: PTOMAINTAIN MOTION AND CONCRETE FLOOR.



tan 8 = 0,5 mm +1.25 mm

tane=0.0175

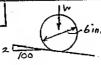
P=Wtane P=0.0175 W

W=mg=(900 kg) (9.81 m/s)

P= (0.0175)(900 frg)(9.81 m/s2). P= 154.51 N

P=154.4N

8.114



GIVEN: DISK ROLLS AT CONSTANT VELOUTY FIND: COEFFICIENT OF ROLLING RESISTANCE

DIEK IS IN EQUILIBRIUM

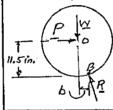
SIMILAR TRIANGLES

$$\frac{b}{r} = \frac{2}{100}$$

b= 2 v = 2 (6 in.); b= 0,060 in.

8.115 GIVEN: 2500-16 AUTOMOBILE WITH 23-in .- DIAMETER TIRES, COEFFICIENT OF ROLLING RESISTANCE = 0.05 in.

FIND: HORIZONTAL FORCE TO MOVE AUTOMOBILE CY HORIZONTAL ROAD AT CONSTANT SPEED

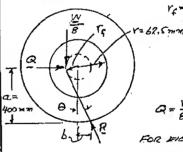


+) IM= = 0: P(11.5in.) -W b=G P(11,5in)=(2500 16)(0.05in) P= 10.869 lb

P=10.8716

8.116 GIVEN: 30-Mg RAILROAD CARE ON EIGHT BOO-mm-DIAMETER WHEELS WITH 125-mm ALLES,

M3 = 0,020, 44 = 0.015, COFFFICIENT OF ROLLING RESISTANCE 0.5mm FINDS HORIZ. FORCE (a) TO START MOTION, (b) TO MAINTAIN MOTION.



FOR ONE WHEEL

tand = sind = T+b

tono= ur+b Q= Wtan 0 = W 4r+b

FOR EIGHT WHEELS OF CAR P=W=4r+b

W=mg=(30Mg)(9.8) 7/5) = 294.3 AN a=400 mm, r= 67.5 mm, b=0.5 mm

(a) TO START MOTION: 4 = 45=0,02 P= (294.3-124) (0.020) 62,5mm) +0.5mm

P= 1.2876 KN

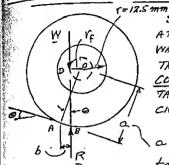
P=1.288 LN

(b) TO MAINTAIN CONSTANT SPEED M=MK=0.015 P= (294,3 &N) (0.015)(62,5 mm) +0.5 mm

P=1.0576-BN

P=1,058&N

GAVEN! SCOOTER IS TO ROLL DOWN A 2 PERCENT SLOPE AT CONSTANT SPEED, YLES OF WHEELS ARE 25 mm IN DIAMETER. 1 = 0.10, COEFFICIENT OF ROLLING RESISTANCE = 1.75 mm. FIND: REQUIRED DIAMETER OF WHEELS.

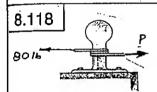


SINCE SCOOTER ROLLS AT CONSTANT SPEED, EACH WHEEL IS IN EQUILIBRIUM. THUS WAND R MUST HAVE COMMON LINE OF ACTION TANGENT TO THE FRICTION CIRCLE.

a = RADIUS OF WHEEL tano= 2 = 0.02

SINCE & ANDY, ARE SMALL COMPARED TO Q, tan 6 = V++b = Mur+b = 0.02 DATA: Mx = 0.10, 'b = 1.75 mm, Y=12.5 mm (0.10)(12,5mm)+1,75mm = 0.02

a = 150 mm; DIAMETER = 20 = 300 mm.



(a) FOR TWO FULL TURNS OF HAWSER AND P = 5000 10, FIND MS (b) FIND NUMBER OF TURKS, IF P= 20,000 10.

(a)
$$\beta = 2 \text{ TURNS} = 2(2n) = 4\pi$$

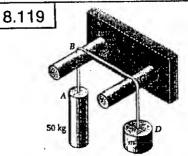
 $T_1 = 8016$ $T_2 = 500016$
 $l_1 \frac{72}{7} = 1/5 \beta$ $N_5 = \frac{1}{\beta} l_1 \frac{72}{7} = \frac{1}{4\pi} l_1 \frac{500016}{8016}$

$$\ln \frac{T_2}{T_1} = M_0 f$$
 $\beta = \frac{1}{9} \ln \frac{T_2}{T_1} = \frac{1}{0.329} \ln \frac{20,000 \text{ ib}}{809}$

$$\beta = \frac{1}{c,329} ln(250) = \frac{5.5215}{0.329} = 16.783$$

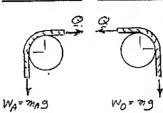
NUMBER OF TURNS = 16.783

NUMBERS OF TURNS = 2.67



GIVEN: 1/5=0.40

FIMD: RANGE OF MASS ON FOR EQUILIBRIUM



FOR MOTION OF A IMPENDING DOWNWARD

FOR EACH ROD B = T/2, Ms = 0.4

$$\frac{\alpha}{\alpha_0} = e^{-M_S \beta}$$
 $\frac{m_0}{\alpha} = e^{-M_S \beta}$

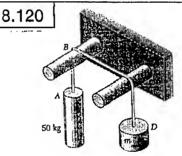
MULTIPLY EQUATIONS MEMBER BY MEMBER

THEY EQUATIONS MEMBERS BY MEMBERS
$$\frac{Q}{m_{A9}} \cdot \frac{m_9}{Q} = e^{4/5} (\beta + \beta) \cdot \frac{m}{m_A} = e^{0.4/2} \cdot \frac{\pi}{2} = 3.514$$

FOR MOTION OF A IMPENDING UPWARD, WE FIND IN A GIMILAR WAY

$$\frac{m_A}{m} = c^{0.4(2)\frac{\pi}{2}} = 3.514; \quad m = \frac{50 \text{ Åg}}{3.514} = 14.23 \text{ Åg}$$

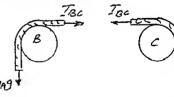
RAHGE FOR EQUILIBRIUM: 14.23 kg ≤ m≤ 175.7 kg



GIVEN: MOTION OF D IMPENOS UPWARD WHEN m=20kg,

Fing: (a) 4/5 (b) TENSION IN BC

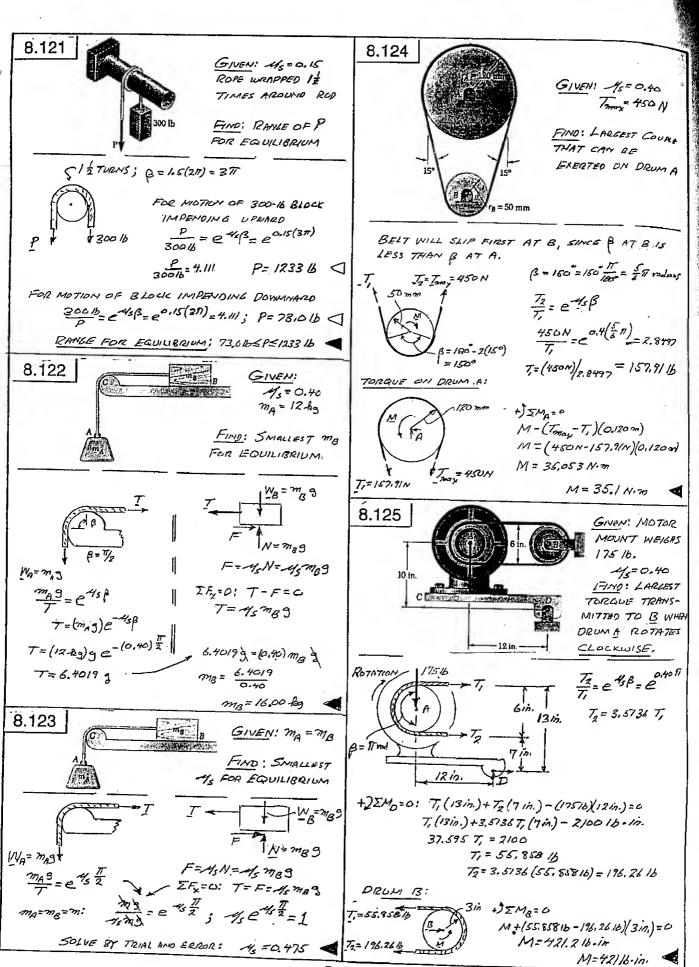
FOR EACH ROD: R= 1/2



$$F(\omega)$$
: $\frac{m_A 9}{T_{BC}} = C^{4S\beta}$

MULTIPLY FOURTIONS MEMBER BY MEMBER

FG(2) Tec 0.217() Tec=310N



g.12

ROTAT

β=77 -

+2

DRI

72=14

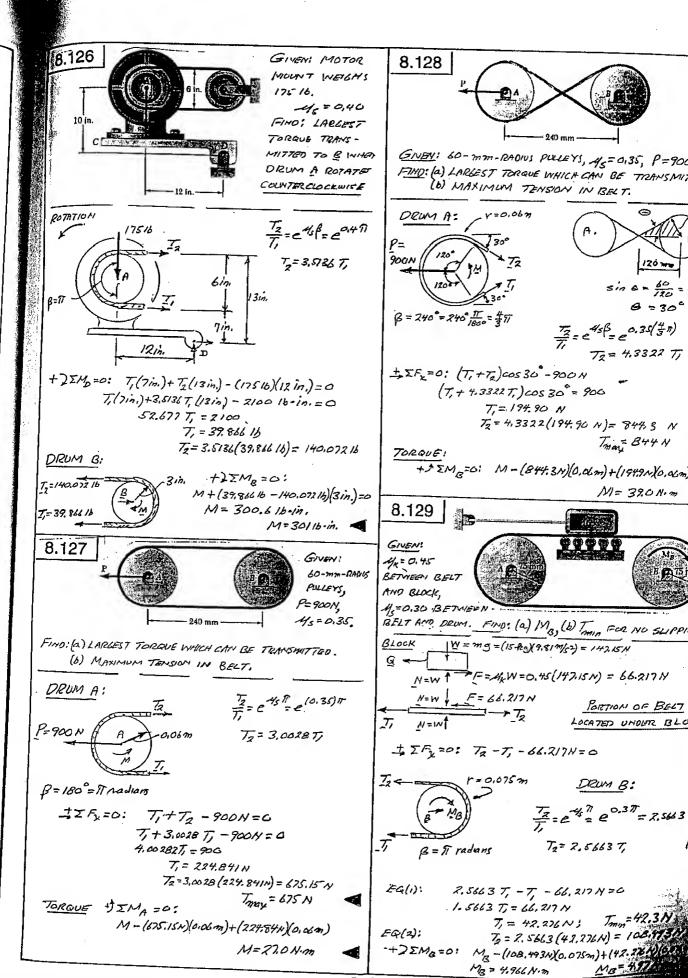
T,= 39

8.

Fin

P

8-32



40

COUPLE

PUM A

15

radions

8497

1/16

onl

4

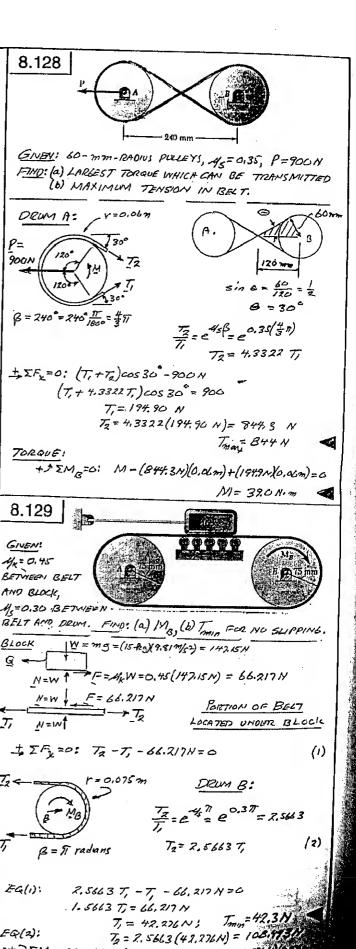
37

'S-

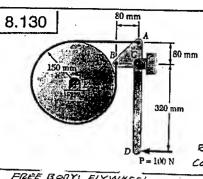
2=5

n

57



MB = 4.966 N.m

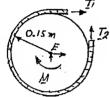


GIVEN: 1/2 = 0.25

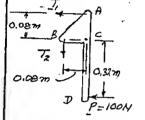
FIND: MAGNITUDE OF COUPLE APPLIED TO FLYWHEEL FOR CLOCKWISE ROTATION SHOW THAT RESILT IS SAME FOR COUNTERCLO CILLUSE ROTATION

FREE BODY: FLYWHEEL

FOR CLOCKWISE ROTATION OF FLYWHELL TO AND TI ARE LOCATED AS SHOWNI.



B= 3(360)= 3(20)= 31 radians $\frac{T_2}{T} = e^{4\pi\beta} = e^{0.25\left(\frac{3}{2}T\right)} = 3.7482$ 万=3.2482 T (1)



FREE BODY: HANDLE

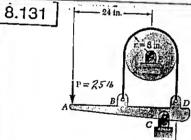
+) EM_ =0 (2) (T,+T2)(0,08m)-(100N)(032m)=0 (T, +3.2487 T,) = 400 N T,= (400 N)/4.2482 = 94.157N

To=3,2482(94,157N)=305.842 N

RETURN TO FREE BODY OF FLYWHEEL

+) \(M_E=0: M+(T_1-T_2)(0.15m)=0 M+(94.157N-305.842N)(0.15m)=G

M= 31.752N·m M=31.8 N.m -IF ROTATION IS REVERSED (TO BE)) TO AND I, ARE INTERCHANGED; EQS,(1) AND(2) ARE NOT CHANGED, THUS VALUES OF TI, T2, AND MI ART THE SAME.



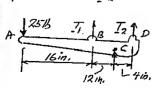
GIVEN. 4 = 0,25

FIND: MAGNITUDE OF COUPLE APPLIED TO DRUN FOR ROTATION (a) COUNTER CLOCKENT (b) CLOCKWISE

(a) COUNTER CLOCK WISE ROTATION FREE BODY DRUM r=8in, B= 180= Tradions



T2=e1/2 e 0.25 T = 2.1933 T= 2.1933 T



FREE BODY: CONTROL BAR +JIMG=0 T, (12 in.) - 7 (410)-(2516)(28in)=c T, (12) - 2.1933T, (4) - 700 = 0 T1=216,9316 Tz=2.1933 (216.93 16)=475.80 16 (CONTINUED)

8.131 CONTINUED

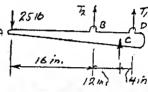
RETURN TO FREE RODY OF DRUM +) & M=0: M+T, (Bin.) -T_2(Bin.) = 0 M+ (216.96 16) (0 in.) - (475.80 16)(8 in.)=0 M=2070 1bin M=2070.9/b.in.

(b) CLOCKWISE ROTATION



r= Bin. B=Trad Tz======= 2.1933 To= 2.1933 T,

FREE BODY: CONTROL ROD

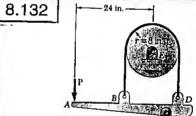


+) IM= 01 Tz (12in.) - T, (4in.) - (25%)(28in) = 2.19337,(12)-7,(4)-700=0 T,= 31,363 16 Tz=2.1933 (31.363 16) To = 68.788 16

RETURN TO FREE RODY OF DRIM +) EM=0: M + T, (Bin.) - T2 (Bin.) =0 M+(31.36316)(ein.)-(68,78816)(8in.)=c

M=299,416-in.

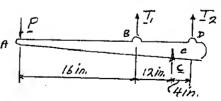
M=29916in.



FIND: MAXIMUM H. FOR BRAKE TO BE SELF LOCIUNG FOR COUNTERCLOCKWISE ROTATION OF DRUM

B =180 = TT radians $\frac{T_2}{T_1} = e^{M_S \beta} = e^{M_S \pi}$

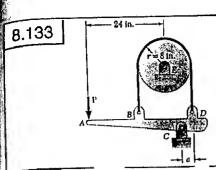
FREE BODY! CONTROL 1200



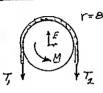
+ \$\(\Sigma = 0: P(28 in) - T_1(12 in) + T_2(4 in) = 0

28P - 12T, + e^47 T_1(4) = 0

FOR SELF-LOCKING BRAILE PEO 12T= 4Tem ens = 3 M.TT = In 3 = 1.0986 Ms= 1.0986 = 0.3497 -95=0,350

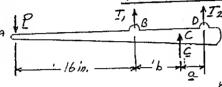


GIVEN: ME = 0.30 ROTATION D. FIND: MINIMUM VALUE OF ON FOR INHIGH BRAICE IS NOT SELF-LOCKING.



r=Bin .. B= 17 radias T2 = e 45 \$ = e 0,30 \$ = 2.5663 T2 = 2,5663 T,

FREE BODY: CONTROL ROD



b=16in-a

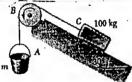
+) IMc=0: P(16in+b)-T,6+T2a=0 FOR BRAKE TO BE SELF LOCKING, P=G Ta= T,b; 2.5663 x a = x (16-a)

2.5663a = 16-a 3,5663a=16

a=4.49in.

8.134

7,=719



GIVEN: 4/5=0.35 4k = 0.25 PANO: SMALLEST m FOR WHICH BLOCK C (a) REMAINS AT REST, (b) STARTS

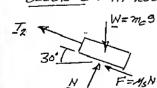
MOVING UP, (C) CONTINUES MONNG UP.

ROTATION

B=120°= \$11 rad. FREE BODY: DRUM T2 = e. 43 T 72=mge 247/3 (1)

(a) SMALLEST ON FOR BLOCK C TO REMAIN AT REST CABLE SLIPS ON ORUM 2(0.25) 7

EG(1) WITH Mx = 0.25; T2=mge = 1.688/mg BLOCK C: AT REST, MOTION IMPENDING



W=meg + / EF=0: N-meg cos 30° N= Mcg cos 36 F = 45N = 0.35 mcg cos30 mc=100 kg

(CONTINUED)

+ X IF=0; 72+ F-meg sin30=0 1.6001 mg+ 0.35 mg cos36 - neg sin36 = 0 1.6881m = 0.19689 mc m=0.11663 mc=0.11663(100 kg); m=11.66 kg

8.134 CONTINUED

(b) SMALLEST on TO START BLOCK MOVING UP

NO SLIPPING AT BOTH DRUMI AND BLOCK 45 = 0,35 Eali): Tz = mg e 2(0.25)T/3 = 2.08/4mg

BLOCK C: W=mcg

MOTION IMPENDING TO ME = 100 kg +/ SF=0; N-ng cos 300 N= meg cos 30° F=1,N=0.35 meg cos 300

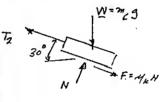
+ IF=0: T2-F-meg sin 30°=0 2.0814mg - 0.35 mg cos36 -mg sin30 =0 · 2.0814 m = 0.80311 Mc m=0,38585 mc = 0,38585 (100 Rg) m=38.6-29

(C) SMALLEST OM TO KEEP BLOCK MIONING UP

DRUM: NO SLIPPING M5=0.35

EQ(1) WITH M = 0.35 245T/3 = 2(0.35)T/3 ファニ ツァダ T2 = 2.08/4 mg

BLOCK C: MOVING UP PLANE, THUS OF = 0.25



MOTION UP +12F=0 N-mg cas 30°= 0 N=meg cos 30" F=1/4 N=0,25mcgcos 30°

+ TF=0: T2-F-mg sin 30 =0 2.0814mg-0.25mg cos30-mg sin30=0 2.0814 m = 0.71651 711c ..

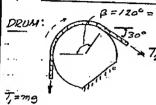
m = 0.34424 mc = 0.34424 (100 fee) m=34.4-29



GIVEN: DRUM B

FIND: SMALLEST M FOR WHICH BLOCK C (a) REMAINS AT REST, (b) STARTS MOVING UP, (E) CONTINUES MIGNING UP.

(a) BLOCK C REMAINS AT REST, MOTION IMPENDS > B=1200 = 3 11 radians



 $\frac{T_2}{m_0} = e^{4/k} \beta = e^{0.35 \left(\frac{2\pi}{8}\right)}$ Tn= 2.0814 mg

15 FIXED.

45=0.35 4K = 0,25

BLOCK C .W=mc9

MOTION IMPENOS 1 IF=0: N-mg cos30 =0. N= 71/2 9 cos 300 F=15N=0.35 mg cos 300

+ K ΣF=0: 72 + F - 72 g sin 30 = 0 2.0814 mg + 0.35 mg cos30 -meg sin 30 =c 2.0814 mg = 0.19689 mc m = 0.09459 m = 0.09459 (10020) m= 9.46 Rg

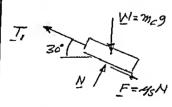
(b) BLOCK C STARTS MOVING UP / B = 1200 = 2 TI radians. DRUM:

4=0.35 INDENDING MOTION OF CABLE F

 $\frac{mg}{T} = e^{0.35\left(\frac{2}{3}\pi\right)}$

Ti = mis = 0.48045 mg

BLOCK C MOTION IMPENIES



TEF=0: N-meg cas 30 N= meg cos 300 F=45N=0,35mag cas30°

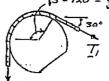
+ IF=0: T, -F-meg sin 30°=0 0,48045 mg - 0.35 mg cos30 -0,5 mg =0 0,48045m=0.80311MC m=1.67158-mc=1.67158 (100.Ag)

m=167.2 feg (CONTINUED):

8.135 CONTINUED

(c) SMALLEST m To KEEP BLOCK MIOVING

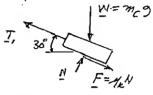
DRUM: MOTION OF CABLE (ME = 0.25 B = 120 = 3 T radians



 $\frac{T_2}{T_1} = e^{4/\mu} \beta = e^{0.25(\frac{2}{3}n)}$ mg = 1.6881

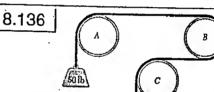
T= mg = 0.59238 mg Ta=mg.

BLOCK C! BLOCK MOVES &



+P IF=0: N-mag cas 30.0 N= mcg coszos F=4,N=0.25mg cos30

+ IF=0: T, -F-mag sin30=0 0.59238 mg - 0.25mg cos30 -0,5 mg =0 0,59238 m = 0.71651 mc m = 1.20954 mc = 1.20954(100 kg) m=121,0 Rg



(W)

GIVEN: 1/5=0,25 1/K=0.20 FIND: (a) SMALLET ' IN FOR EQUILIBRIUM (6) LARGEST W THAT

CAN BE RASED IF PIPEB .15 120747ED HUTH A+C FIXED.

(a) 4 4 5 = 0.25 AT ALL PIPES

To = Tec 50B 0.25 T TA-

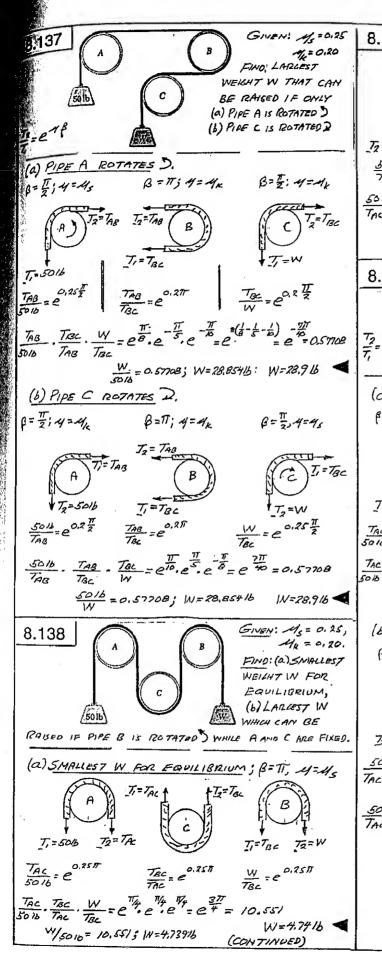
50 10 TAB TRL W = CB . ET. C = CB . ET. C = CB . ET. CB CB . ET 1 50 B = 4.8015 3 W= 10.3941B

(b) PIPE B ROTATED 5 B=# 4=42 B=11; 4=4. A TETAS TETAS

Tz=5016

5016 = 0.85464; W= 5016 = 58,504 16

W=58.515



કુ*વ્*લૐ**.** કુવ્લ્

4530°

45=0.25

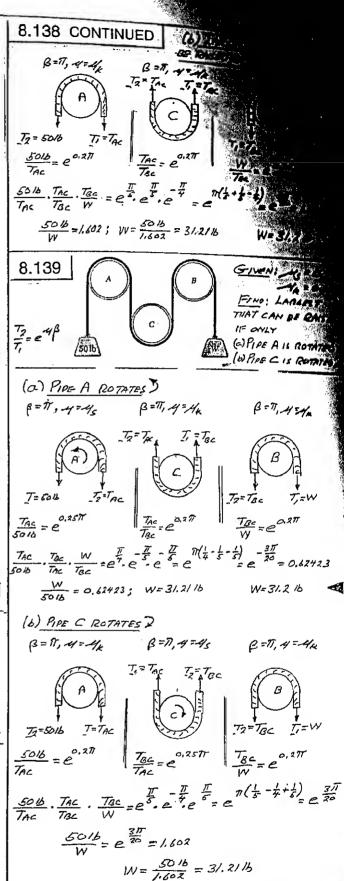
SMALLET

ILIBRIUM THAT

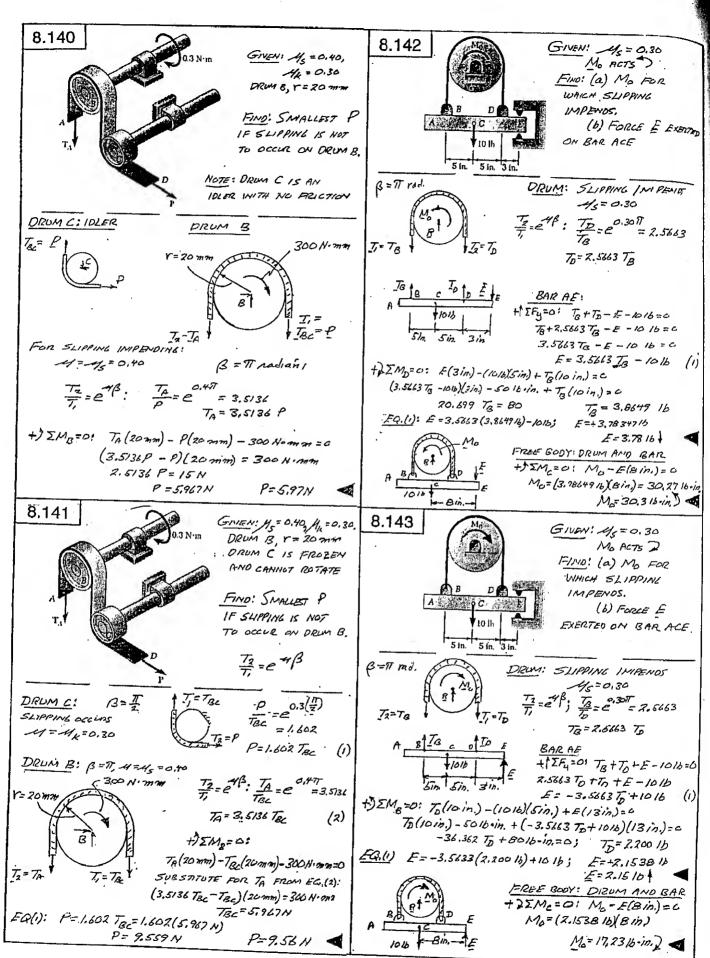
= TBC + B = 17

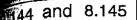
1/4

-TBC



W=31.216







GINEN: a=200 mm, V=30 mm. I

ASSUME VALUE OF M₅ IS THE SAME
AT ALL SURFACES OF CONTACT

FIND: SMALLEST VALUE OF M₅ FOR WHICH

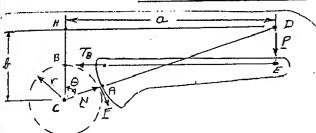
THE WRENCH IS SELF-LOCKING IF IN

PROB. 8.144 B=65°.

PROB. 8.145 B=75°.

FOR WHENCH TO BE SELF-LOCKING (P=0), THE YALVE OF MY MUST ITLEVENT SLIPPING OF STEAR WHICH IS IN CONTACT WITH THE PIPE EROM POINT A TO POINT B AND MUST BE LARGE ENOUGH SO THAT AT POINT A THE STRAP TENSION CAN INCREASE FROM ZERO TO THE MINIMUM TENSION REGUIRED TO DEVELOP BELT PRICTION BETWEEN STRAP AND PIPE.

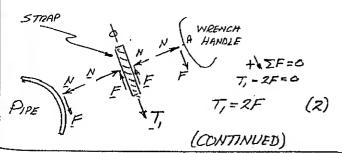
FREE BOOY: WRENCH HANDLE



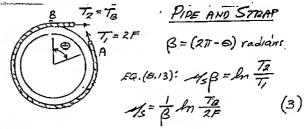
GEOMETRY IN ACDH: CH=Q-/tan G, CD=Q/sin G DE=BH=CH-BC $DE=\frac{a}{ton G}-r$ $AD=CD-CA=\frac{a}{sin G}-r$

 $\frac{GN \text{ INDENCH HANDLE}}{+ \sum M_D = 0}; \quad T_B(DE) - F(AD) = 0$ $\frac{T_B}{F} = \frac{AD}{DE} = \frac{\frac{\Delta}{SINB} - r}{\frac{\Delta}{F} - r} \qquad (1)$

FREE BOOY: STRAP AT PONTA



8.144 and 8.145 CONTINUED



NOTE: FOR A GIVEN SET OF DATA, WE SEEK THE LARGER OF THE VALUES OF MS FROM EQS. (3) AND (4)

PROB. 8.144: a = zoomm, r=30mm, 6=65°

 $FO(1): \frac{T_B - \frac{200 \text{ mm}}{5 \text{ ln } 65^{\circ}} - 30 \text{ mm}}{\frac{700 \text{ mm}}{63,262 \text{ mm}}} = \frac{190.676 \text{ mm}}{63,262 \text{ mm}} = 3,017$

B = 211-0=211-65-17 = 5.1487 radiais

Ea(3): 45 = 1 Pm 2 = 0.41015 = 0.0797

EQ(4): $-4s^{2} = \frac{\sin 6s^{6}}{3.0141 - \cos 6s^{6}} = \frac{0.90631}{2.1595} = 0.3497$

WE CHOOSE THE LARGER VALUE: 45=0,350

PROB. 8.145: a=200 mm, r=30 mm, B=75°

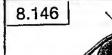
 $FQ_{1}(1): \frac{7B}{F} = \frac{\frac{200 \, \text{mm}}{s \ln 75^{\circ}} - 20 \, \text{mm}}{\frac{200 \, \text{mm}}{t \, \text{an} \, 75^{\circ}}} = \frac{177.055 \, \text{mn}}{23,570 \, \text{mm}} = 7,5056$

B=211-6=211-750 # 49742

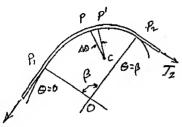
L=Q.(3): 45= 1 1,5056 = 1.3225 = 0.2659 <

Eq.(4): $9/5 = \frac{\sin 75^{\circ}}{7.5056 - \cos 75^{\circ}} = \frac{0.96953}{7.2468} = 0./333$

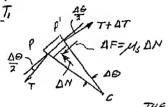
VVE CHOOSE THE LARGER VALUE: 15=0,266



PROVE THAT EOS. (B. 13) AND (B. 14) ARE VALID FOR ANY SHAPE SURFACE



NOTE & IS THE ANGLE BETWEEN BOTH TANGENTS AT P, +P, AND NORMALS AT P, +P,



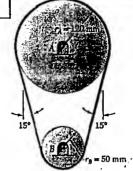
NEXT, NOTE THAT THE DERIVATION OF

dT= Ms de (1)

ON PAGES 436 AND 437
DIO NOT DE PEND ON
THE PADIUS OF CURVATURE
BEING CONSTANT, THEREFORE
THIS ECUATION MAY BE OBTAINED,
FRUM THE FREE-BOOY DIAGRAM
SHOWN HEREE.

INTERRATING EQUI) IN @ FROM O TO B AND IN

8.148



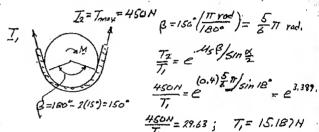
GIVEN: Mg = 0.40

Tmax = 450 N

V-BELT WITH & = 31

FIND: LARGEST COUNTY THAT CAN BE EXERTED ON PULLEY

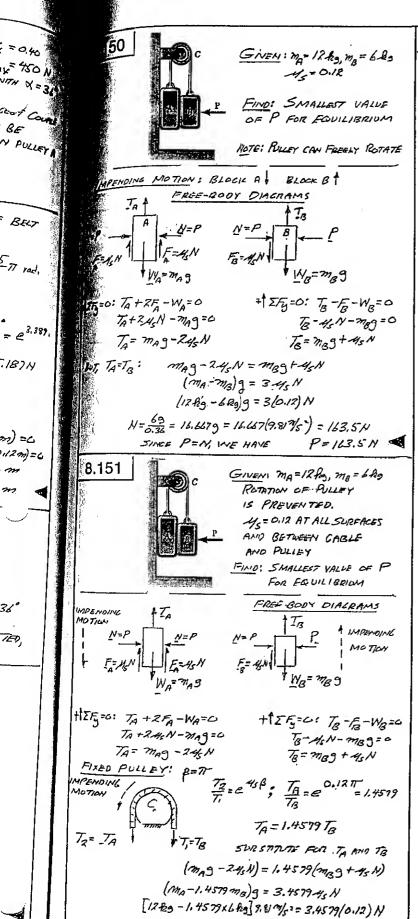
SINCE B IS SMALLER FOR PULLEY B, THE BELT WILL SLIP FIRST AT B.



TORQUE ON PULLEY A



+) IMB=0 M-(Tmax-Ti)(0.12m)=0



= 0,40

BE N PULLEY

BELT

5 77 rad,

= e 3,387.

.187 N

≫) =८

20

36°

120,

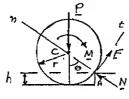
11200)=6

1x 550 N

8.152

GIVEN: A5=0.90 12-in - RADIUS WHEELS 60% OF WHAT 15 ON FRONT WHEELS.

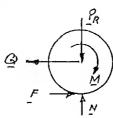
FIND: LARGEST & FOR AUTO TO CLIMB CURB (a) FRONT-WHEEL DRIVE, (b) REAR-WHEEL DRIVE



(a) FRONT-WHEEL DRIVE ONE FRONT WHEEL: Y = 12in. t/ SF,=0: F-Psin B=0 X IF = 01 N-PCOSE = C SLIDING IMPENOS: 45 F = Psing = tane

tan 6=45=0,90; Q=41.987° h=r-rcos 0=r(1-cos 6)=(12in.)(1-cos 41.987) h= 3,0805 in. h= 3.08 in.

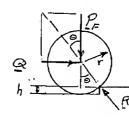
(b) REAR WHEEL DRIVE EACH REAR WHEE CARRIES D. ZW AND EACH FRONT WHEEL CARRIES 0.3W. LET Q BE FORCE EXERTED BY CHASSIS ON EACH WHEEL



FREE BOOY: NEAR INHEEL Po= O.ZW

+1 ZFy=0: N-0.2W=0 N=0.2W F=F=45N=0.90(0.2W) F=0.18W

±Σ=0: F-9=0 Q=F=0,18W



FREE BODY: FRONT WHELEL P==0,3W r= 12 in.

FRONT WHEEL IS A TWO-FORCE BODY tan 0 = 0 = 0.18W = 0.6 G= 30,96°

h=r-rcos 0 = r(1-cos 6) = (2 in,)(1- cos 30,96°) = 1.7101 in h=1.710in,

NOTE: COMPARING PROBS 8.152 AND B.153, WE NOTE THAT -FOR FRONT WHEEL DRIVE THE RESULT IS INDEPENDENT OF WEIGHT DISTRIBUTION FUR REAR-WHEEL DRIVE THE HEAVIER THE LOAD ON THE READ WHEELS, THE LARLER

THE GURB HEIGHT H WILL BE

N=76,898N

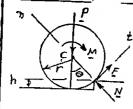
P=76.9 N

SINCE P=N, WE HAVE



GIVEN! 1/5=0.90, 12-in - RADIUS WARDLE FRUAL INDIGHT ON

FIMO: LARGEST h FOR AUTO CLIMB CURB (a) FRONT-WHEEL DRIVE, (b) REAR-WHEEL DRIVE



(a) FRONT-WHEEL ORIVE ONE FRONT WHEEL Y=1214 + PEF=01 F-PsinG=0 Y IF = 0: N-PCOS G = C SLIPPING INIPENDS:

Ms= F= Psine = Land

ton 0 = 45 = 0.90; 0 = 41,987°

h=r-rcos&=Y(1-cosA)=(1210)(1-cos419070) h=3,0805 in. h= 3.08in.

(6) REAR WHEEL DRIVE

FREE BOOY! REAR WHEEL PR=0.25W

LET QUBE FORCE EXERTED BY CHASSIS ON EACH WHEEL + TF=0: N-0,25W=0 N=0.25W

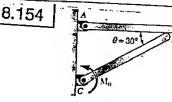
F=195N=0.90(0.25W)=0.225W Σ/2=0: Q = 0.225W

FREE BODY: FRONT WHEEL P==0.25W

r=12in TWO-FORLE BODY tanB = = = 0.226 W = 0,9

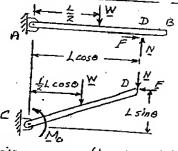
G=41.987° h=r-reos0=r(1-cos6) h=(12in)(1-cos 41.9870)= 3.0806 in

h= 3.08 in. [SEE NOTE AT END OF SOLUTION OF PROB 8.152



GIVEN: EACH ROD IS OF LENGTH L AND WEIGHT W. 1/5= 0.46

FIND: RANGE OF VALUES OF ME FOR EQUILIBRIUM



FOR IMPENDING CLOCKWISE MOTTON 4) [Mz = 0

N(LCOSE) - W(=)=6 N= W

1=45N= 2 cos 6

+) IM=0: M2-W(1/2 LOSE) - W (LOSE) + 45W (LSINE)=5 Mo= 1 WL (cose +1 - 4/5 tand)

Mo= 1 INL (cos 30°+1-0,40 tan 30°) M= 0.81754WL

Mo=0,818WL V (CONTINUED)

8.154 CONTINUED

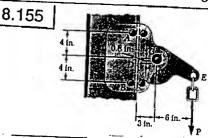
FOR IMPENDING COUNTERCLOCKWISE

MIOTION OF THE ROOS. WE CHANGE THE SILM OF MS IN FQ(1).

-- Mo = 1 WL (COSO +1 + 45 tand) = 12WL(cos 30° +1 +0.40 tan 30°)

Mo = 1.0484WL Mo=1,048WK

RANCE OF MO FOR EQUILIBRIUM; 0.818 WL < MO < 1.048 WL



FIND: SMALLEST A BETWEEN RAIL AND CAM AND BETWEEN RAIL AND PINS FOR EQUILIBRIUM

∮⊆y 0.8in, |₩ FEMSND bin.

FREE BODY: CAM +) IMc =0: No(0.8in)-45 No(3in)-P(6in)00

FREE BODYISLEEVE AND CAM 4in. 厉

\$ 2Fx=0: ND -NA -Ng= 0 NA+NB= ND (2) +1ΣFy=0: FA+F8+F6-P=0

OR 45(NA+NB+NO) = P EUBSTITUTE FROM (2) INTO(3) 45(ZNO)=P No= P

-4=0.0533

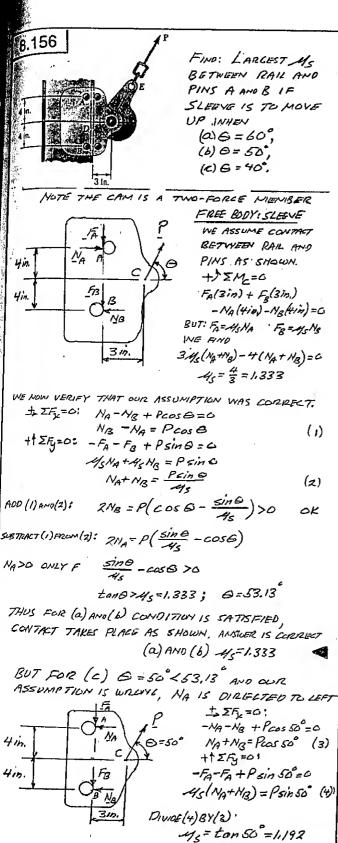
FOURTE EXPRESSIONS FOR My FROM (1) AND(4) P = 6P ; 0.8-345=1245

NOTE: TO VERLIFY THAT CONTACT AT PINS A AMO B TAKES PLACE AS ASSUMED WE SHALL CHECK THAT NASO AND NB=0.

From (4): No = \frac{P}{245} = \frac{P}{2(0.0533)} = 9.375 P

FROM FREE BODY OF CAM AND SLEEVE DEMB=C NA(Bin) - ND(4in) - P(9in) = 6 ENA = (9.375P)(4)+9P NA = 5.8125P>0 OK

FROM (2): NA+HB=HD 5.8125P+HB=9.375P MB= 3.5625P>0 OR



45=0.30. FIND: LARGEST & FOR TUBE TO SLIDE HORIZONTALLY WHEN (a) a=0, (b) a=0.75m. FOR MAY &, SLIDING AND ROTATION ABOUT C BOTH IMPEND (a) THREE-FORCE BODY FORCE P MOST PASS THROWAN POINT D WHERE IN AND C INTERSECT. SINCE SLIPPING IMPENOS & FORM ANGLE OS WITH TUBE \$= tan 45 = tan 0.30 ISOSCELES TRIANGLE Ps = 16.70° = 90 - 45 = 90 - 16,7 @= 73.3 +) ZMc=0: (Pcosps) L-W==0 P= 1/2 cos \$ = (2020)(9.81 7/52), P= 102.4 N (6) THREE-FORCE BODY (See ABOUD IN A CDG: DG = 0.75 m = 2,50 m IN AADG: $tan\Theta = \frac{DG}{AG} = \frac{2.5m}{1.5m}$ tana=1,667, 0=59,04° B=59,0° +) IM =0: (P sin B)(2,25m) - W(0.75m)=0 P= 0.333 W= 0.333 (2029)(9,8/7/6) P= 26,27N P=76.3 M 8.158 GIVEN: Mg=0,30 20-Rg TUBE AB FINO: (a) SMALLEST P TO MOVE TUBE, (6) WHETHER TUBE SLIDES OR ROTATES. ASSUME SLIDING ZF. N=W-Psin60° F=45N= US (W-Psin 66) ZF2: Pcos 60 = F= M5(W-Psin60) P= 45W COS60+45 SIA600 = 0.3 W = 0.3948 W ASSUME ROTATION ABOUT C (c) 45=1.192 +221/2=0 B (Psinka)(2.25m)-W(1.25m)=6 NOTE: FOR G >53,13, MS IS INDEPENDENT OF B.
FOR G < 53,13, MS DEPENDS ON G c / P=0,5249 W 1.25m TUBE SLIDES AND 15 As=tan & FOR SLIDING: P=0,3948W=0.3948(20Re)(9.817/5)

8.157

GIVEN: 20-Ry TUBE AB.

P= 77.5 N

